

Lab 7 is in SCI 136 (!)

Please, login into webassing, locate
LectureMCQ_L16 (PY105)
and answer question 1
(but **ONLY Q1!**).

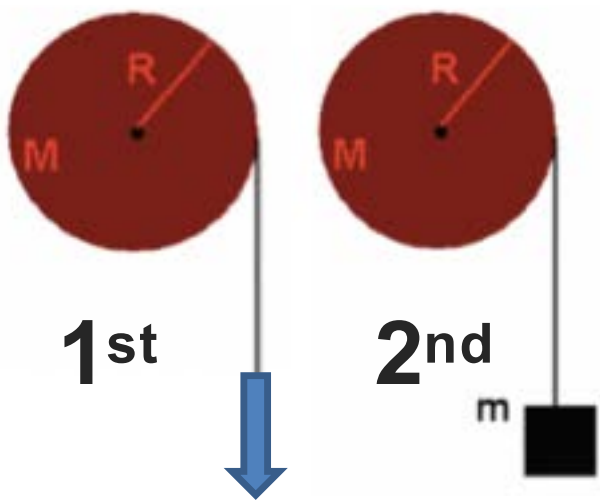
Pleas sign in using the sign-in sheets on
the bench. Thank you



Good morning!



**Note: exam room
change:
Exams 2, 3 take
place in STO B50**



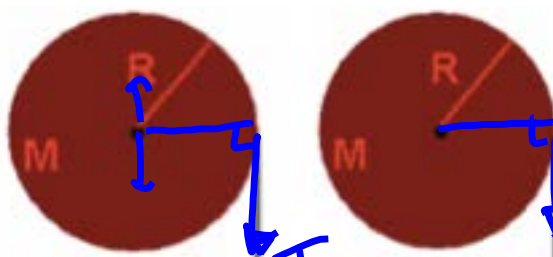
First time we pulled on a string applying a force of 10 N.
Second time we attached to a string a weight of 10 N.

[Webassign: L16 Q2](#)

When did the disc have a higher angular acceleration?

1. 1st time
2. 2nd time
3. It was the same
4. there is not enough information
5. there is too much information



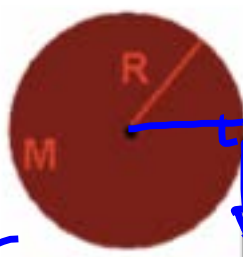


1st

$$T_1 = 10 \text{ N}$$

$$T_1 \cdot R = I \cdot \alpha_1$$

$$\alpha_1 = \frac{T_1 \cdot R}{I}$$



2nd

$$W = 10 \text{ N}$$

$$\alpha_2 = \frac{T_2 \cdot R}{I}$$

$$\alpha_1 = \frac{10 \cdot R}{I} ; \alpha_2 = \frac{9 \cdot R}{I}$$

$\alpha_1 > \alpha_2$

First time we pulled on a string applying a force of 10 N. Second time we attached to a string a weight of 10 N.

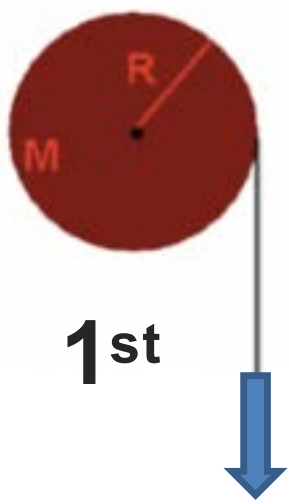
When did the disc have a higher angular acceleration?

$$N2 \text{ (} T_2 - W = m(-a) \text{)}$$

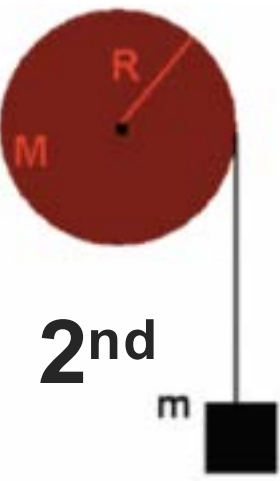
$$T_2 = \frac{10 - m \cdot a}{1}$$

das hat
nichts zu tun

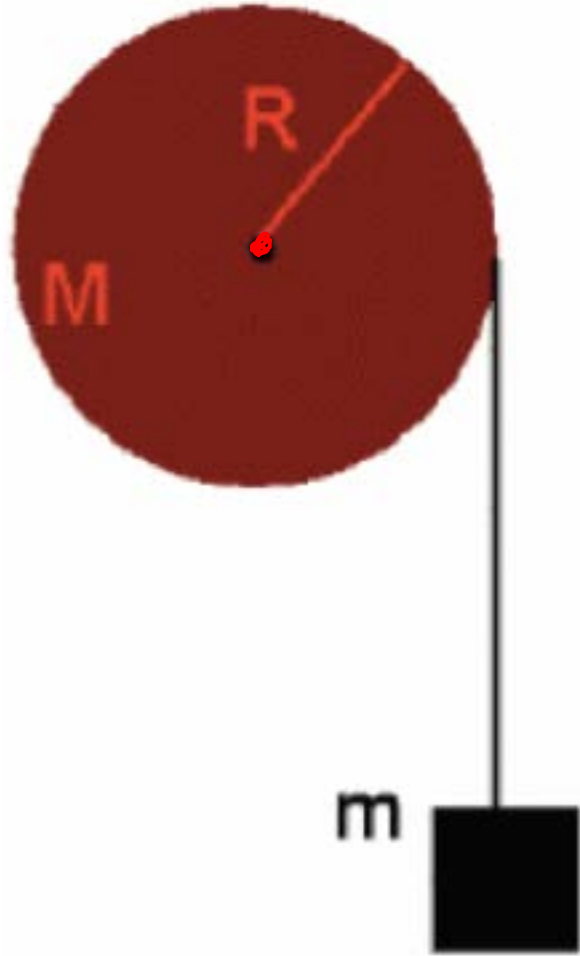
$$\underline{T_2 < 10}$$



First time we pulled on a string applying a force of 10 N. Second time we attached to a string a weight of 10 N. When did the disc have a higher angular acceleration?

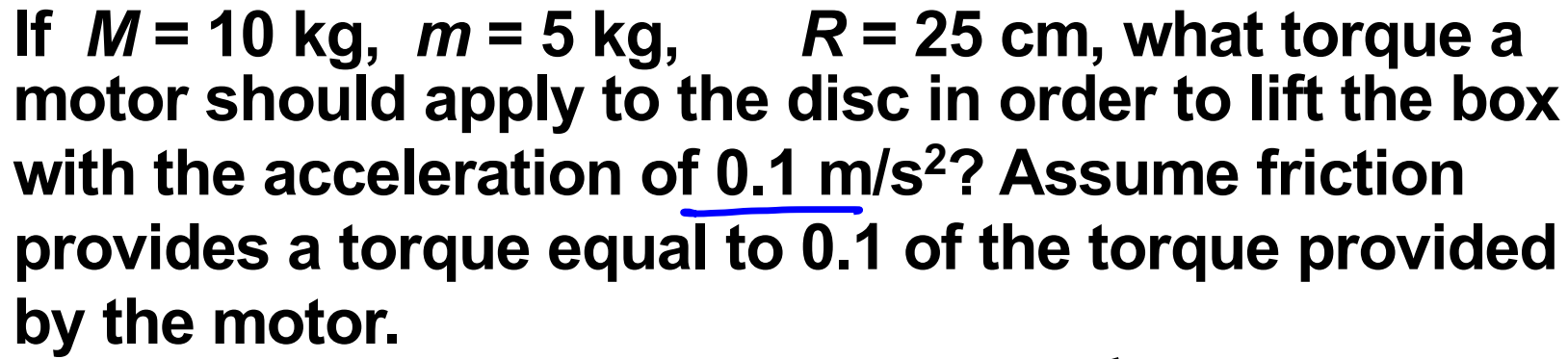


1. 1st time
2. 2nd time
3. It was the same
4. there is not enough information
5. there is too much information



If $M = 10 \text{ kg}$, $m = 5 \text{ kg}$,
 $R = 25 \text{ cm}$, what torque a
motor should apply to the
disc in order to lift the box
with the acceleration of 0.1 m/s^2 ? Assume friction
provides a torque equal to
 0.1 of the torque provided
by the motor.





$$|F_T| = |F_2| = F_T$$

$$\tau_{tr} = 0.1 \cdot \tau_{ap} \quad \tau_{ap} = ?$$

$$N26: F_T - mg = m \cdot (+a)$$

Physics was done!

$$T = mg + ma = m(10 + 0.1) = 50.5 \text{ N}$$

$$\tau_a - 0.1 \cdot \tau_a = T \cdot R + \frac{1}{2} MR^2 \cdot \frac{a}{R}$$

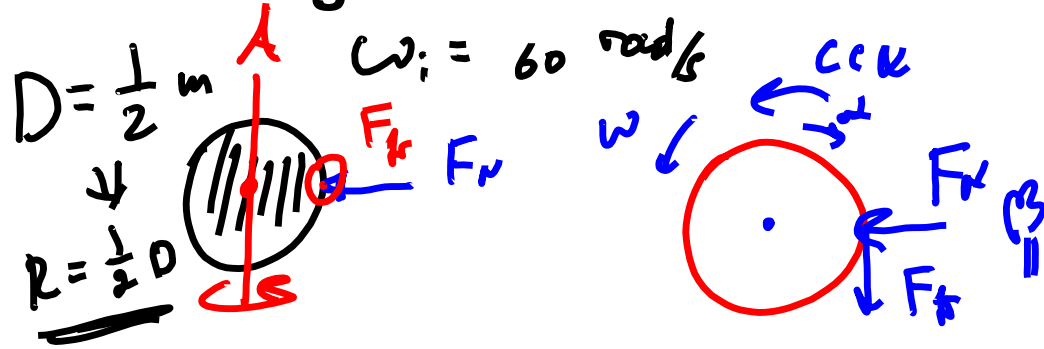
$$\tau_a = \frac{50.5 \cdot 0.25 + \frac{1}{2} \cdot 10 \cdot 0.25 \cdot 0.1}{0.9} =$$

$$= 14.17 \text{ N}\cdot\text{m}$$

A solid sphere with a mass of 10 kg and diameter of 50 cm is rotating with an angular speed of 60 rad/s about an axis passing through its center. By applying a normal force, the rotation of the sphere is slowed down to 2 rad/s. If the coefficient of friction was .8, what was the magnitude of the normal force applied to the sphere, if the slowing down lasted for 10 s?



A solid sphere with a mass of 10 kg and diameter of 50 cm is rotating with an angular speed of 60 rad/s about an axis passing through its center. By applying a normal force, the rotation of the sphere is slowed down to 2 rad/s. If the coefficient of friction was .8, what was the magnitude of the normal force applied to the sphere, if the slowing down lasted for 10 s?



$$I = \frac{2}{5} m R^2 = \frac{2}{5} 10 \cdot \left(\frac{1}{2}\right)^2$$

$$0.8 \cdot F_N \cdot \frac{1}{2} = F_f \cdot R = |\tau_f| = I \cdot |\alpha| = \frac{2}{5} \cdot 10 \cdot \left(\frac{1}{2}\right)^2 \cdot 5.8$$

$$F_f = \mu \cdot F_N = 0.8 \cdot F_N$$

$$\omega_i \rightarrow \omega_f = 2 \text{ rad/s} \quad t = 10 \text{ s}$$

$$\alpha = \frac{2 - 60}{10} = -5.8 \text{ rad/s}^2$$

$$I \cdot |\alpha| = \frac{2}{5} \cdot 10 \cdot \left(\frac{1}{2}\right)^2 \cdot 5.8$$

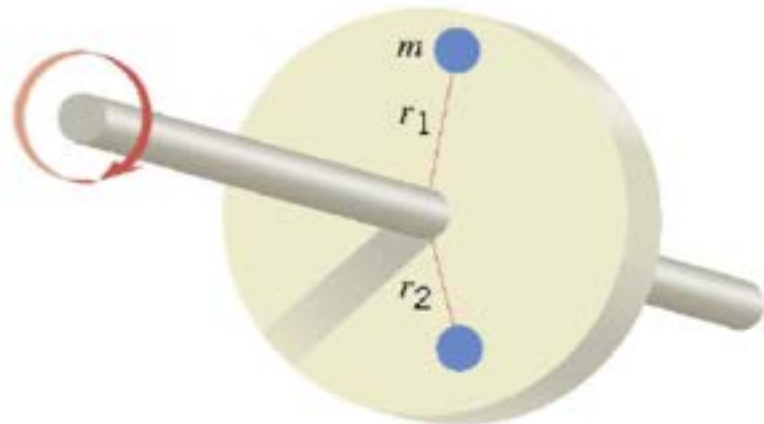
Rotational Energy

For a point-like object

$$KE = \frac{1}{2} m v_T^2 = \frac{1}{2} m r_1^2 \omega^2$$



$$v_T = r_1 \omega$$

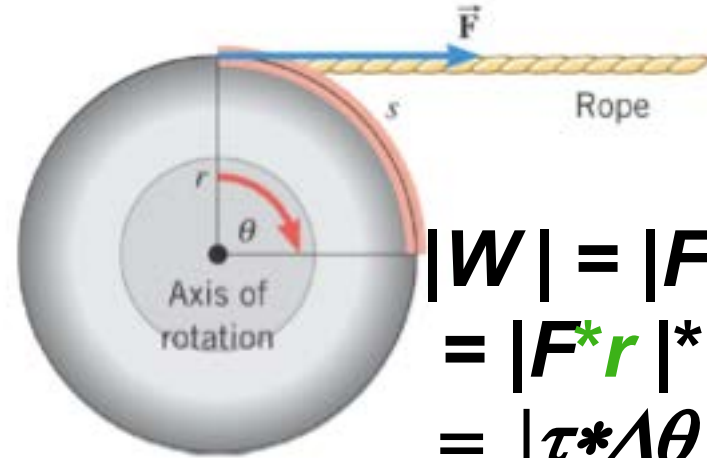


For a solid object

$$\underline{KE} = \sum \left(\frac{1}{2} m r^2 \omega^2 \right) = \frac{1}{2} \left(\sum m r^2 \right) \omega^2 = \underline{\frac{1}{2} I \omega^2}$$

Work done by torque

Webassign: L16 Q3



$$\begin{aligned}|W| &= |F|s \\ &= |F^*r|*S/r \\ &= |\tau*\Delta\theta|\end{aligned}$$

Requirement: The angle must be expressed in radians.

Unit of Rotational Work: joule (J)

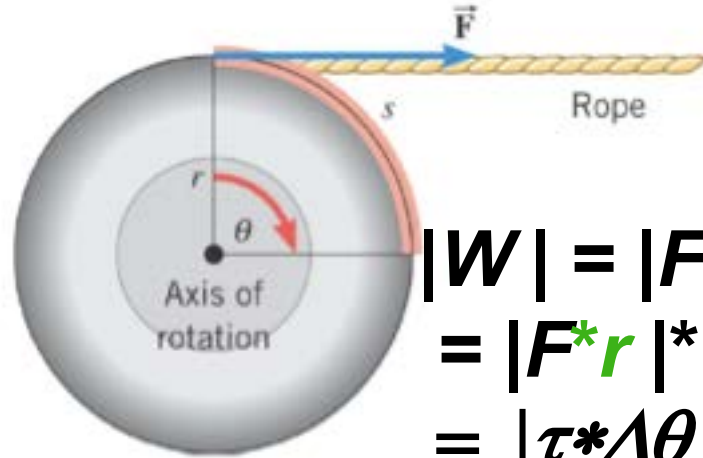
- In this equation θ ...
1. Angle between force and displacement
 2. Always acute
 3. None of the above

$$|W| = |\tau \Delta\theta|$$



Work done by torque

Webassign: L16 Q3



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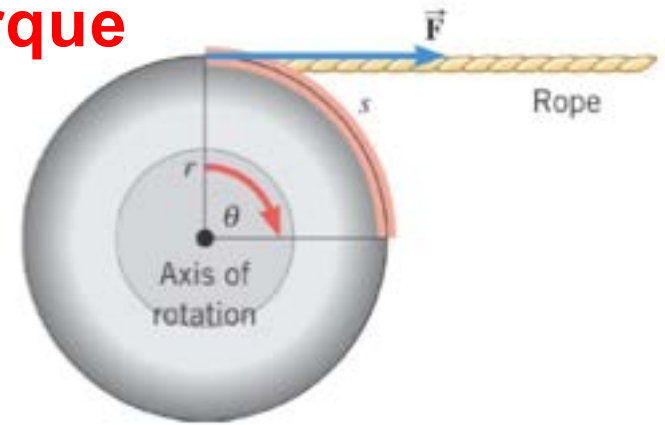
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Work done by torque



Requirement: The angle must be expressed in radians.

SI Unit of Rotational Work: joule (J)

Angular displacement

For 1-D rotation

$$\cos \theta = \pm 1$$

$$W = |\tau \Delta \theta| \cos \theta$$

Actual value

The angle between the torque and angular displacement

Magnitude

$$|W| = |\tau \Delta \theta|$$

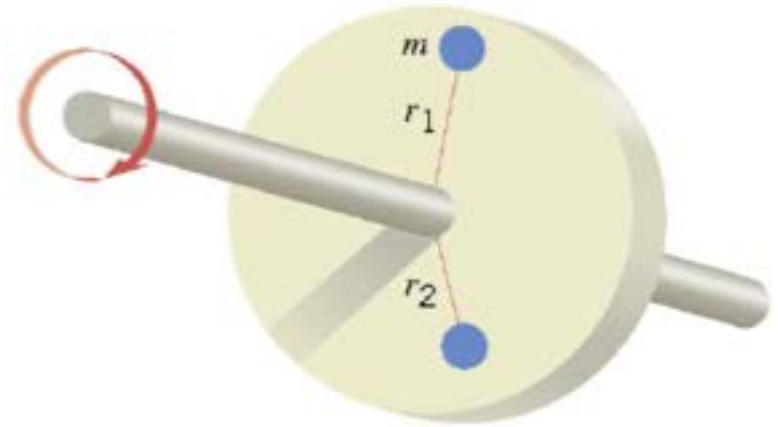
Rotational Energy

For a point-like object

$$KE = \frac{1}{2} m v_T^2 = \frac{1}{2} m r_1^2 \omega^2$$

$$v_T = r_1 \omega$$

$$W = |\tau \Delta\theta| \cos\theta$$



For a solid object

$$\underline{KE} = \sum \left(\frac{1}{2} m r^2 \omega^2 \right) = \frac{1}{2} \left(\sum m r^2 \right) \omega^2 = \underline{\frac{1}{2} I \omega^2}$$

WKET (RM) $K_f - K_i = W_{net}$

What is the minimum amount of work that has to be done to speed up a 5 kg disk with the radius of 10 cm from rest to 100 rev per second?

↪ rad!

$$K_f - K_i = W \Rightarrow K_f = W$$

\downarrow \downarrow \downarrow

ϕ ω_f

$$W = \frac{1}{2} I \omega_f^2 = \frac{1}{2} \cdot \frac{1}{2} 5 \cdot (.1)^2 \cdot (100 \cdot 2\pi)^2 \text{ J}$$

Let's review: **IMT** $\sum \vec{F} \Delta t = \Delta(mv) \Rightarrow$ **LCLM**

As we did for straight-line motion, we can write Newton's second law in a different form:

N2LR

$$\Sigma \tau = I\alpha = I \frac{\Delta\omega}{\Delta t} = I \frac{\omega_f - \omega_i}{t} = \frac{I\omega_f - I\omega_i}{t} = \frac{\Delta(I\omega)}{\Delta t}$$

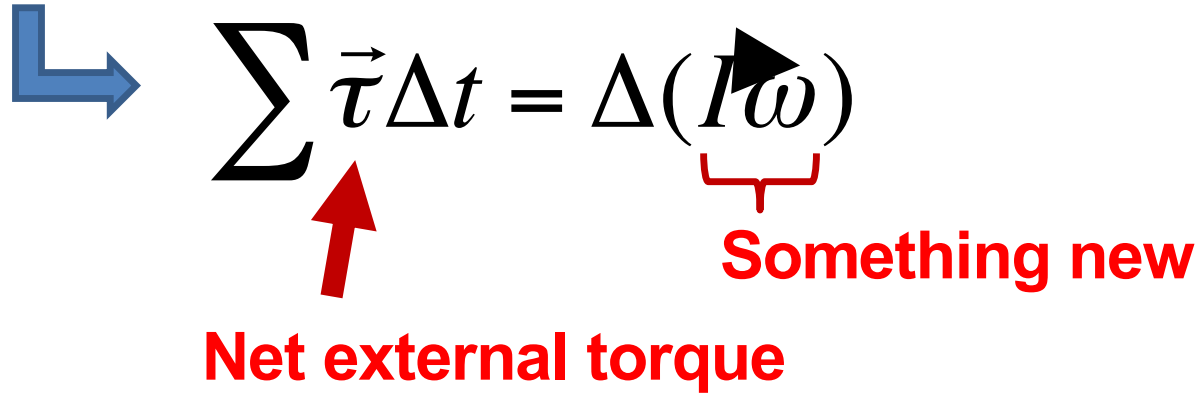
or

$$\Sigma \tau = \frac{\Delta(I\omega)}{\Delta t}$$

$$\sum \vec{\tau} \Delta t = \Delta(I\omega)$$

Net external torque

Newton's second law for rotational motion



The diagram illustrates the derivation of angular momentum. It starts with the equation $\sum \vec{\tau} \Delta t = \Delta(I\vec{\omega})$. A blue arrow points to the left side of the equation, and a red arrow points to the $\vec{\tau}$ term, which is labeled "Net external torque". A red bracket under the $I\vec{\omega}$ term is labeled "Something new".

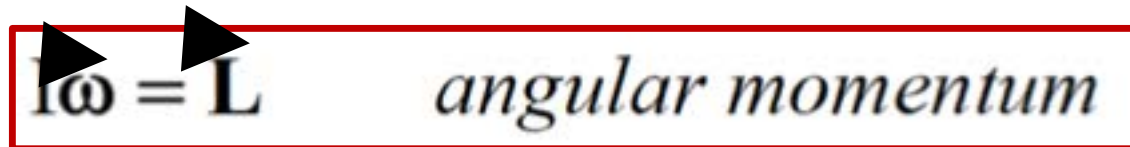
$$\sum \vec{\tau} \Delta t = \Delta(I\vec{\omega})$$

Net external torque

Something new

Angular momentum

New variable \Rightarrow new name and new notation.



The diagram shows the definition of angular momentum. It features the equation $I\vec{\omega} = \mathbf{L}$ inside a red box, with the text "angular momentum" to the right. A black arrow points to the $I\vec{\omega}$ term, and another black arrow points to the \mathbf{L} term.

$$I\vec{\omega} = \mathbf{L} \quad \text{angular momentum}$$

The Law of Conservation of Angular Momentum

$$\sum \vec{\tau} \Delta t = \Delta \vec{L}$$

When no external torques act on a system, the angular momentum of the system is conserved.

$$\tau_{\text{Net}} = 0 \Rightarrow \vec{L} = \text{const}$$

$$\vec{L}_{\text{initial}} = \vec{L}_{\text{final}}$$

Figure Skater



A spinning figure skater starts spinning with her arms outstretched. When she moves her arms close to her body,

[Webassign: L16 Q4](#)

$$L_i = L_f$$

or

$$I_i \omega_i = I_f \omega_f$$

A) She spins faster.

B) She spins slower.

C) The angular velocity stays the same.



Figure Skater

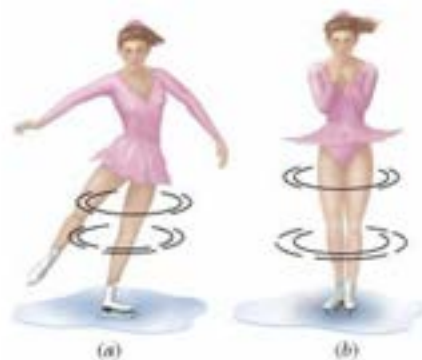
A spinning figure skater starts spinning with her arms outstretched. When she moves her arms close to her body, her moment of inertia decreases $I \downarrow$

Conserving angular momentum says:

$$L_i = L_f$$

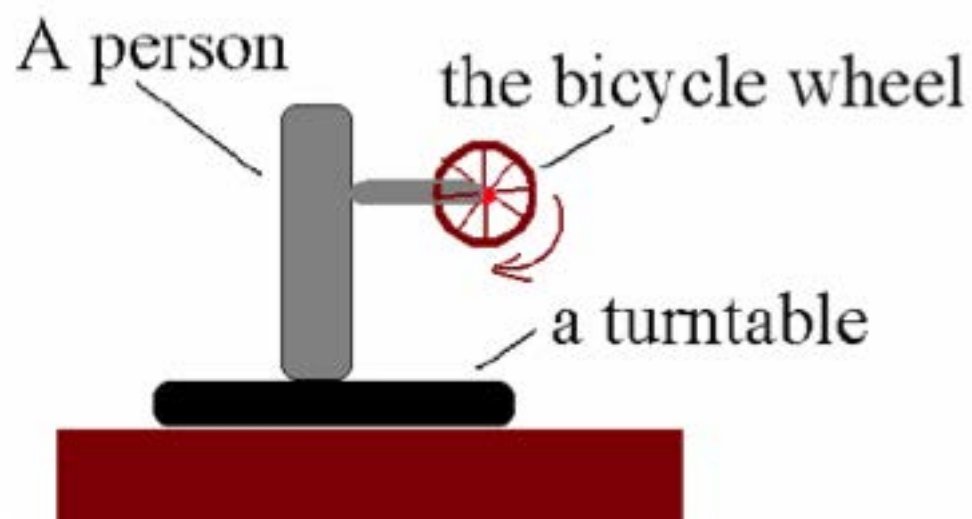
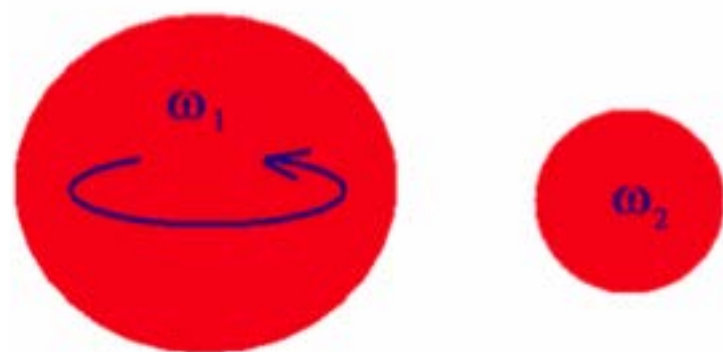
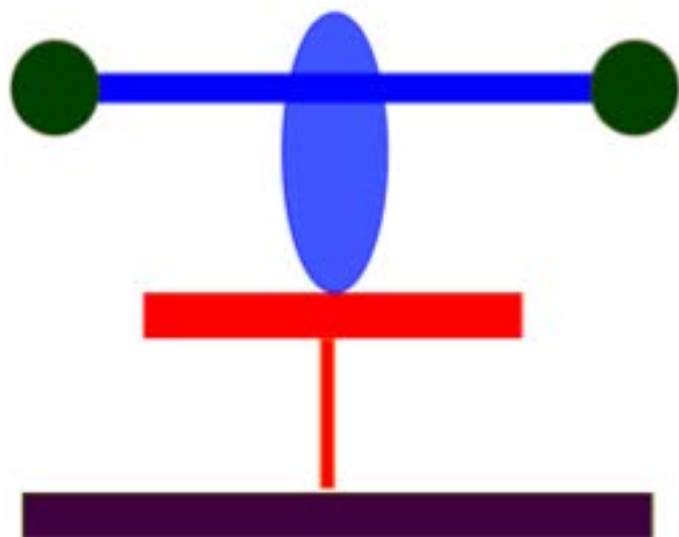
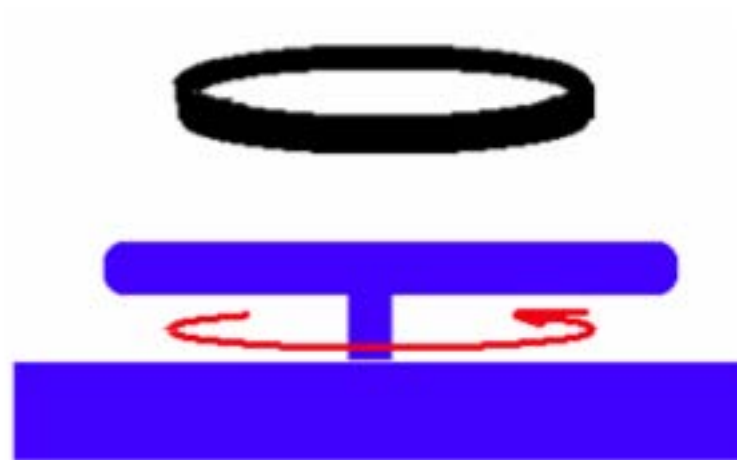
or

$$I_i \omega_i = I_f \omega_f$$



$$I_f < I_i \quad \Rightarrow \quad \omega_f > \omega_i$$

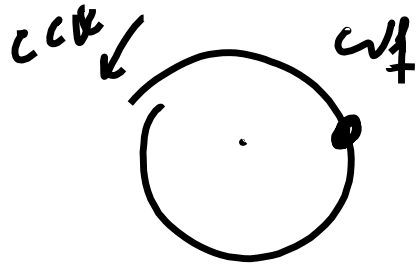
A) She spins faster.



You drop a 1 kg lump of clay on a turning table rotating at 3 rev/s. The clay sticks to the rim of the turntable. Find the new angular velocity of the table (with the clay) if the mass of the table is 5 kg and its radius is 30 cm.



$$L_i = I \cdot \omega_i = \frac{1}{2} M R^2 \cdot \omega_i$$



$$L_f = \left(\frac{1}{2} M R^2 + \underline{m R^2} \right) \cdot \underline{\omega_f}$$

→ $L_i = L_f$

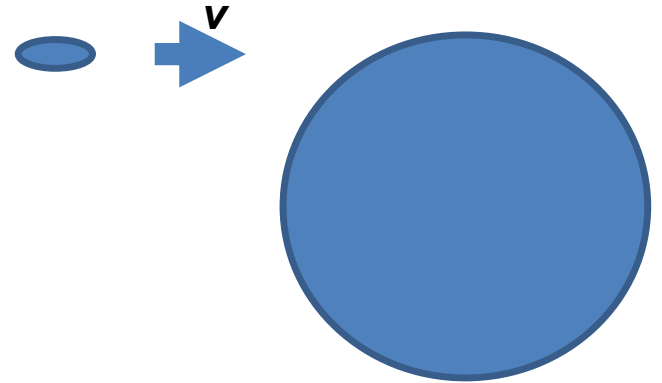
Physics is done!

**A traveling bullet hits a resting disk.
The bullet is stuck in a massless
catcher located right at the rim of the
disc. After the collision the disc ...**

- 1. Remains at rest**
- 2. Spins CW**
- 3. Spins CCW**

**(refer to the picture
on the right)**

Webassign: L16 Q5



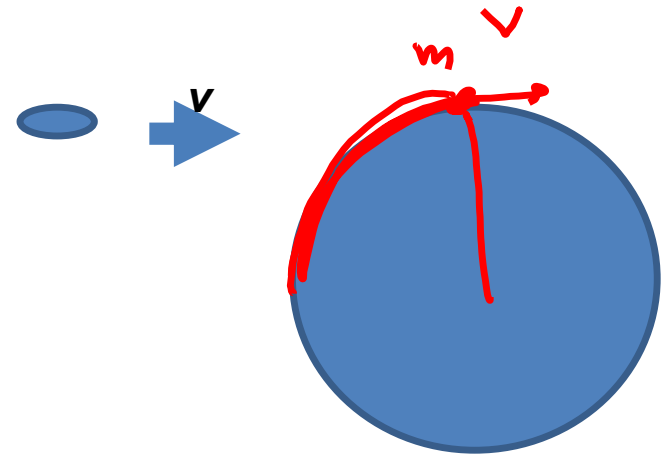
A 100 g bullet traveling at 100 m/s hits a 10 kg resting disk with the diameter of 50 cm. The bullet is stuck in a massless catcher located right at the rim of the disc. Find the angular speed of the disk right after the collision

$$L_{\text{bullet}} = L_i = I \cdot \omega = m \cdot R^2 \cdot \frac{v}{R}$$

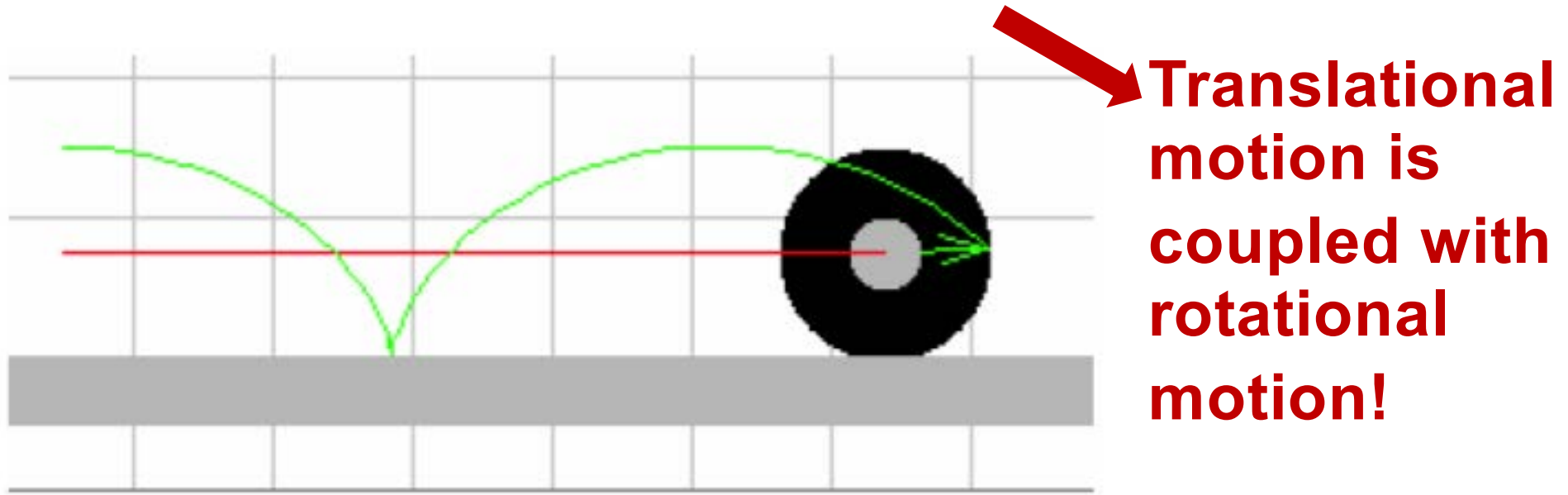
$$\omega = \frac{v}{R}$$

$$L_f = (I_{\text{disk}} + I_B) \cdot \omega_f$$

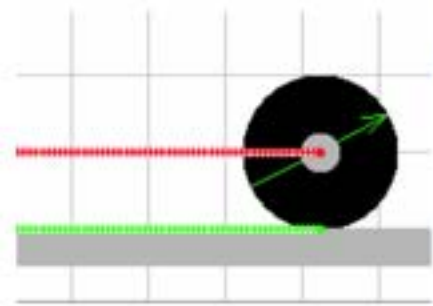
$$L_f = L_i$$



Rolling with NO slipping



Distance traveled by the center relative to the ground is equal to the distance traveled by any point on the rim about the center.



When a wheel rolls without slipping, the straight-line distance traveled by the wheel's center-of-mass (in red on the simulation) is exactly equal to the rotational distance traveled by a point on the edge of the wheel (in green).

If the wheel has a constant angular velocity, the rotational speed is:

$$v_r = \frac{2\pi r}{T}$$

Because the distances and times are equal, the translational speed of the center of the wheel equals the rotational speed of a point on the edge of the wheel.

$$\underline{V_r = V_{CoM}}$$

We say "acceleration" we mean "the acceleration of the center of mass" !

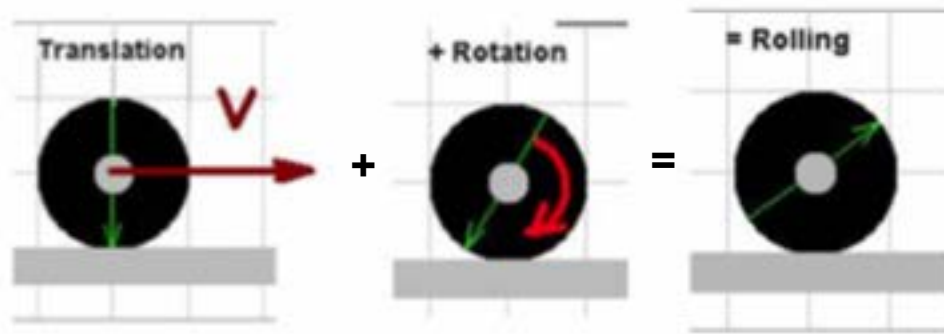
**Angular
speed of
the wheel
relative to
its center**



$$\omega = v / r$$



**Linear
speed of
the center
of the
wheel
relative to
the
ground**



$$\omega = v / r$$

When an object is rolling with *no slipping* its translational motion is coupled with its rotational motion.

$$\underline{V_r = V_{CoM}}$$

Rolling can be viewed as a **combination** of two separate motions, a purely **translational** motion and a purely **rotational** motion.

Rolling involves both of these at the same time - rotation while the wheel is experiencing straight-line motion.

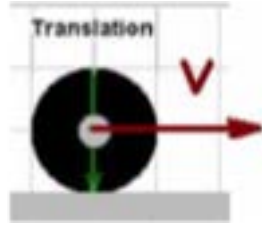
Kinetic Energy

$$I_{cyl} = \frac{1}{2}mr^2$$

$$I_{sph} = \frac{2}{5}mr^2$$

$$I_{ring} = mr^2$$

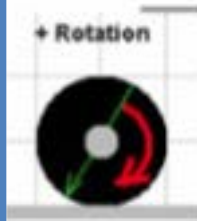
When an object is in a *translational* motion only:



$$K = \frac{1}{2}mv^2$$

 of CofM

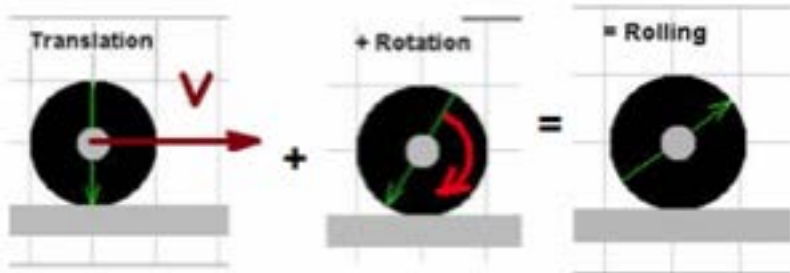
When an object is in a *rotational* motion only:



$$K = \frac{1}{2}I\omega^2$$

 about CofM

When an object is *rolling*:



Total KE

$$K = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$$

NO slipping

$$\omega = v / r$$



Rolling with **NO slipping**

$$\omega = v / r$$

$$\underline{V_r = V_{\text{CoM}}}$$



$$K = \frac{1}{2} m v^2 + \frac{1}{2} I \omega^2 \text{ when an object is rolling}$$


WKET(rolling)

$$K_f - K_i = W_{\text{net}} \quad \text{or}$$

the law of conservation of energy (no slipping)

$$W_{\text{appl}} + U_i + K_i = U_f + K_f$$

 e.g. a hand


 $W_{\text{fr}} = 0$

We have three objects of the same mass and radius; a solid disk, a ring, and a solid sphere.

The moments of inertia:

[Webassign: L16 Q6](#)

$$I_{\text{disk}} = \frac{1}{2}mR^2$$

$$I_{\text{ring}} = mR^2$$

$$I_{\text{sphere}} = \frac{2}{5}mR^2$$

The correct ranking is...

1. $I_{\text{disk}} > I_{\text{ring}} > I_{\text{sphere}}$

2. $I_{\text{disk}} > I_{\text{sphere}} > I_{\text{ring}}$

3. $I_{\text{sphere}} > I_{\text{ring}} > I_{\text{disk}}$

4. $I_{\text{sphere}} > I_{\text{disk}} > I_{\text{ring}}$

5. $I_{\text{ring}} > I_{\text{disk}} > I_{\text{sphere}}$

6. $I_{\text{ring}} > I_{\text{sphere}} > I_{\text{disk}}$

7. I see too many I s

8. What is I ?



A Race: Rolling Down a Ramp

We have three objects of the same mass and radius: a solid disk, a ring, and a solid sphere.

The moments of inertia:

$$I_{\text{disk}} = \{1/2\}mR^2$$

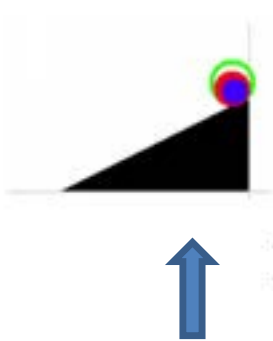
$$I_{\text{ring}} = mR^2$$

$$I_{\text{sphere}} = \{2/5\}mR^2$$

If we release them from rest at the top of an incline, which object will win the race (assume no slipping)?

(In the picture the radii are different for a visibility)

- 1) The sphere
- 2) The ring
- 3) The disk
- 4) Three-way tie



Webassign: L16 Q7 ↑
Which object wins the race?

Webassign: L16 Q6

The correct ranking is...

1. $I_{\text{disk}} > I_{\text{ring}} > I_{\text{sphere}}$

2. $I_{\text{disk}} > I_{\text{sphere}} > I_{\text{ring}}$

3. $I_{\text{sphere}} > I_{\text{ring}} > I_{\text{disk}}$

4. $I_{\text{sphere}} > I_{\text{disk}} > I_{\text{ring}}$

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[Webassign: L16 Q7](#)

The moments of inertia: [Webassign: L16 Q7](#)

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$$I_{\text{ring}} = mR^2$$

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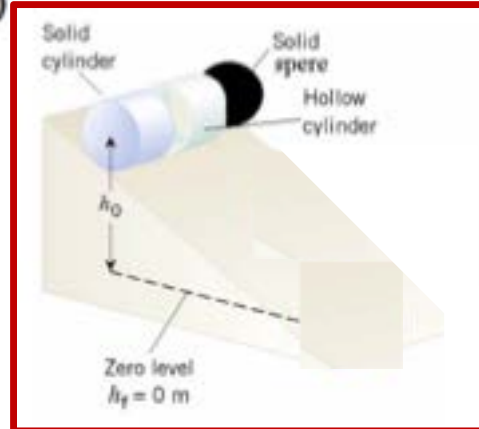
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4. $I_{\text{sphere}} > I_{\text{disk}} > I_{\text{ring}}$
5. $I_{\text{ring}} > I_{\text{disk}} > I_{\text{sphere}}$
6. $I_{\text{ring}} > I_{\text{sphere}} > I_{\text{disk}}$
7. I see too many I s
8. What is I ?

Let's do it!

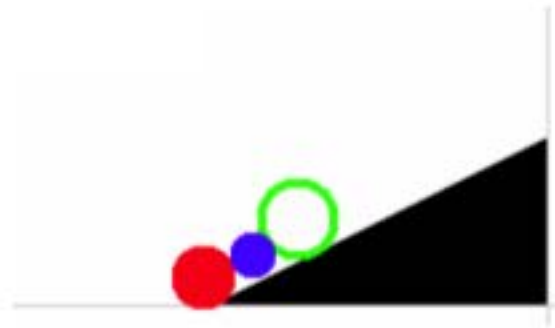
We have three objects of the same mass and radius; a solid disk, a ring, and a solid sphere.

The moments of inertia:

$$1 > \frac{1}{2} > \frac{2}{5} !$$

$$I_{\text{ring}} = mR^2 \quad I_{\text{disk}} = \frac{1}{2}mR^2 \quad I_{\text{sphere}} = \frac{2}{5}mR^2$$

If we release them from rest at the top of an incline, which object will win the race (assume no slipping).



“More inertia” \Rightarrow longer time!

The sphere wins (the disk is next; the ring comes last)



A Race: Rolling Down a Ramp

We have three objects of the same mass and radius: a solid disk, a ring, and a solid sphere.

$$1 > \frac{1}{2} > \frac{2}{5} !$$

The moments of inertia:

$$I_{\text{disk}} = \{1/2\}mR^2$$

$$I_{\text{ring}} = mR^2$$

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Which object wins the race?

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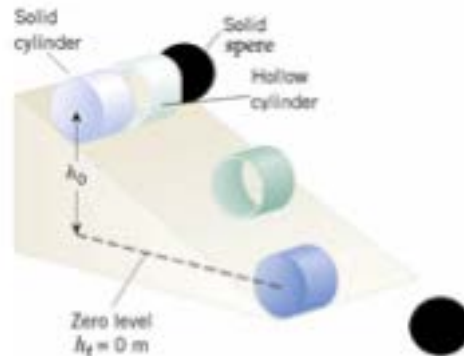
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6. $I_{\text{ring}} > I_{\text{sphere}} > I_{\text{disk}}$

7. I see too many I s

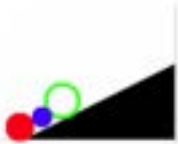
8. What is I ?

We have three objects of the same mass and radius; a solid disk, a ring, and a solid sphere.

The moments of inertia:

$$I_{\text{disk}} = \frac{1}{2}mR^2 \quad I_{\text{ring}} = mR^2 \quad I_{\text{sphere}} = \frac{2}{5}mR^2$$

If we release them from rest at the top of an incline, which object will win the race (assume no slipping).

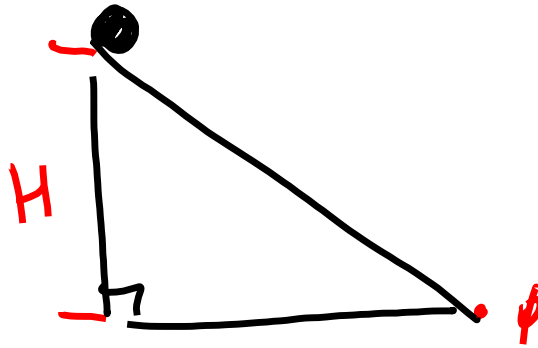


"More inertia" => longer time!

The sphere wins (the disk is next; the ring comes last)

$$\omega = \frac{v}{R}$$

$$I = \underline{C \cdot m \cdot R^2}$$



$$E_i = mgh + \phi$$

$$E_f = \phi + \frac{mv^2}{2} + \frac{1}{2}I\omega^2$$

$$mgh = \frac{mv^2}{2} + \frac{1}{2} \cdot C \cdot m \cdot R^2 \cdot \left(\frac{v}{R}\right)^2$$

$$gh = \frac{v^2}{2} + \frac{1}{2} \cdot C \cdot v^2 = \frac{1}{2}v^2(1+C)$$

$$v_f^2 = \frac{2gh}{1+C} \quad ; \quad v_f = \sqrt{\frac{2gh}{1+C}} \quad ; \quad v_{av} = \frac{0 + v_f}{2} = \frac{v_f}{2}$$

$$t = \frac{2 \cdot 3}{v_f} = \frac{2 \cdot 3 \sqrt{1+C}}{\sqrt{2gh}}$$

A Race: Rolling Down a Ramp

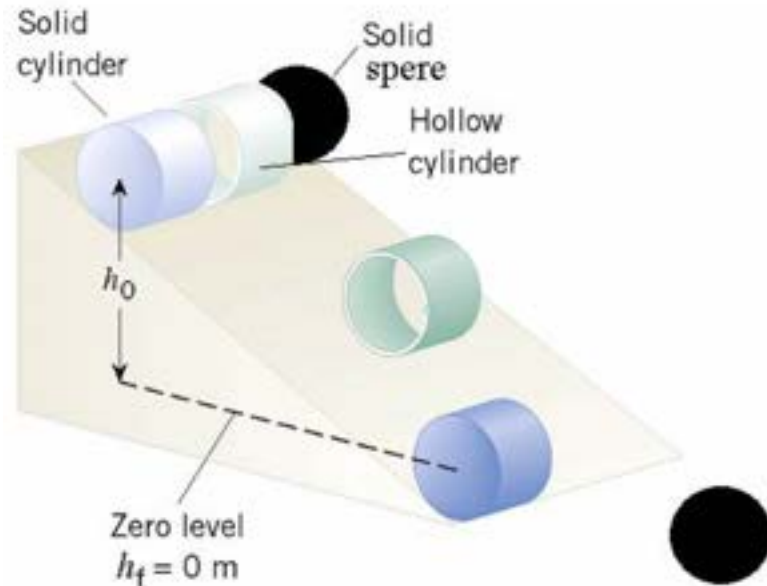
We have three objects of the same mass and radius; a solid disk, a ring, and a solid sphere.

The moments of inertia:

$$I_{\text{disk}} = \{1/2\}mR^2$$

$$I_{\text{ring}} = mR^2$$

$$I_{\text{sphere}} = \{2/5\}mR^2$$



If we release them from rest at the top of an incline, which object will win the race (assume no slipping).

$$U_i + K_i = U_f + K_f$$

Let's apply LCME.

A Race: Rolling Down a Ramp (another solution)

Let's take an object with a mass m and a radius R , and a moment of inertia of CmR^2 .

$$I_{\text{disk}} = \{1/2\}mR^2$$

$$I_{\text{ring}} = mR^2$$

$$I_{\text{sphere}} = \{2/5\}mR^2$$

Hence;

$$I = CmR^2$$

$$C_{\text{disk}} = 1/2$$

$$C_{\text{ring}} = 1$$

$$C_{\text{sphere}} = 2/5$$

(for the sliding block $C = 0$; no rotation!)

Let's apply *the law of conservation of energy* (no slipping)

$$U_i + K_i = U_f + K_f$$

The initial potential energy is mgh . The initial kinetic energy is zero. The final kinetic energy is made up of translational and rotational kinetic energies.



$$mgh = \frac{1}{2} mv^2 + \frac{1}{2} I\omega^2$$

Plugging in $I = CmR^2$: we have

$$mgh = \frac{1}{2} mv^2 + \frac{1}{2} CmR^2 \omega^2$$

or

$$2gh = v^2 + CR^2 \omega^2$$

For rolling without slipping, $v = \omega R$, hence we can write

$$2gh = v^2 + \frac{CR^2 v^2}{R^2}$$

This gives:

$$2gh = v^2 + Cv^2$$

and solving for v

$$v = \left(\frac{2gh}{1+C} \right)^{1/2}$$

So, the larger the value of C (and moment of inertia!), the smaller the speed is ($C \uparrow \Rightarrow v \downarrow$).

The center of mass of each object moves at constant acceleration; hence $S = \frac{1}{2}v \cdot t$

Because the distance S covered by the objects is the same, when $v \downarrow$ the time $t \uparrow$. At the end: $C \uparrow \Rightarrow t \uparrow$ or $C \downarrow \Rightarrow t \downarrow$

The object with the smallest C wins (the sphere or block)!

We have three objects of the same mass and radius; a solid disk, a ring, and a solid sphere.

$$1 > \frac{1}{2} > \frac{2}{5} !$$

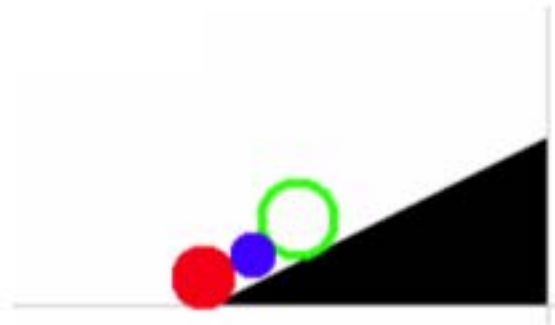
The moments of inertia:

$$I_{\text{disk}} = \frac{1}{2}mR^2$$

$$I_{\text{ring}} = mR^2$$

$$I_{\text{sphere}} = \frac{2}{5}mR^2$$

If we release them from rest at the top of an incline, which object will win the race (assume no slipping).



“More inertia” \Rightarrow longer time!

The sphere wins (the disk is next; the ring comes last)

A sphere rolls down a ramp without slipping and a small piece of ice slides down the same ramp without friction. If they both start from rest from the same height, which object will win the race?

$$t_{\text{sph}} = \frac{2.5 \sqrt{1+c}}{\sqrt{2gh}};$$

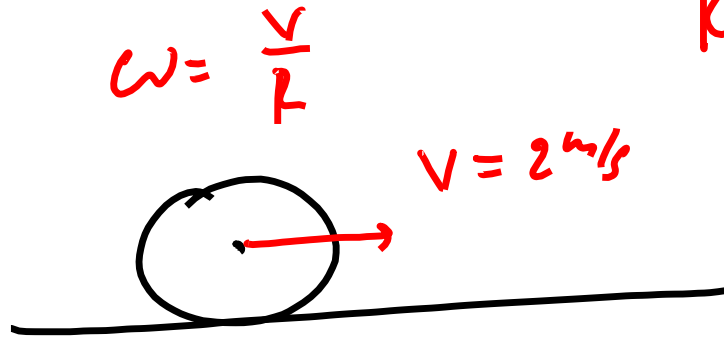
$$c = \frac{2}{5}$$

$$t_{\text{cart}} = \frac{2 \sqrt{1+c}}{\sqrt{2gh}}$$

$$c = 0$$

$$t_{\text{cart}} < t_{\text{sph}}$$

A 5 kg ball rolls without slipping on a horizontal floor so that its center of mass has a speed of 2 m/s. How much work must be done on the ball to completely stop it (calculate the magnitude of the work)?



$$\omega = \frac{v}{R}$$

$$v = 2 \text{ m/s}$$

$$I = \frac{2}{5} m R^2$$

$$C = \frac{2}{5}$$

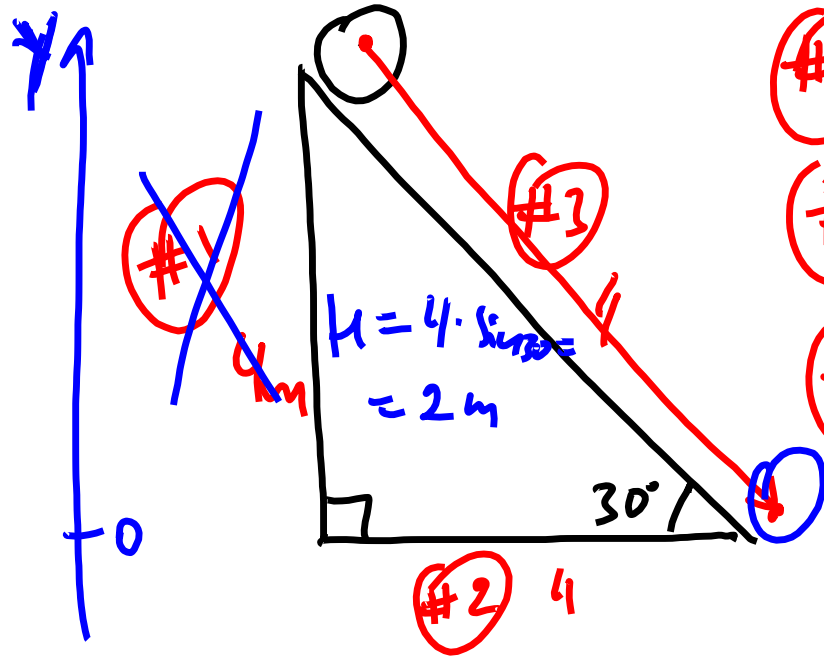
$$KE = \frac{1}{2} m v^2 + \frac{1}{2} I \omega^2 =$$

$$= \frac{1}{2} \cdot 5 \cdot 2^2 + \frac{1}{2} \cdot \frac{2}{5} \cdot 5 \cdot R^2 \cdot \omega^2 =$$

$$= 10 + \cancel{R^2} \cdot \left(\frac{2}{\cancel{R}} \right)^2 = 10 + 4 = \underline{\underline{14 \text{ J}}}$$

$$|W| = |\Delta K| = 14 \text{ J}$$

A solid cylinder with the mass of 2 kg rolls without slipping from rest down a ramp inclined at 30° . Find the speed of the cylinder (i.e. of its CofM) after traveling 4 m.



#1 There is no ramp
 #2 I don't like physics
 #3 I'm not here
 #4
 #5

$$40 = \frac{1}{2} \cdot 2 \cdot V_f^2 + \frac{1}{2} \cdot \frac{1}{2} \cdot 2 \cdot \left(\frac{V_f}{2} \right)^2$$

$V_f = \dots$

$$KE_i = 0$$

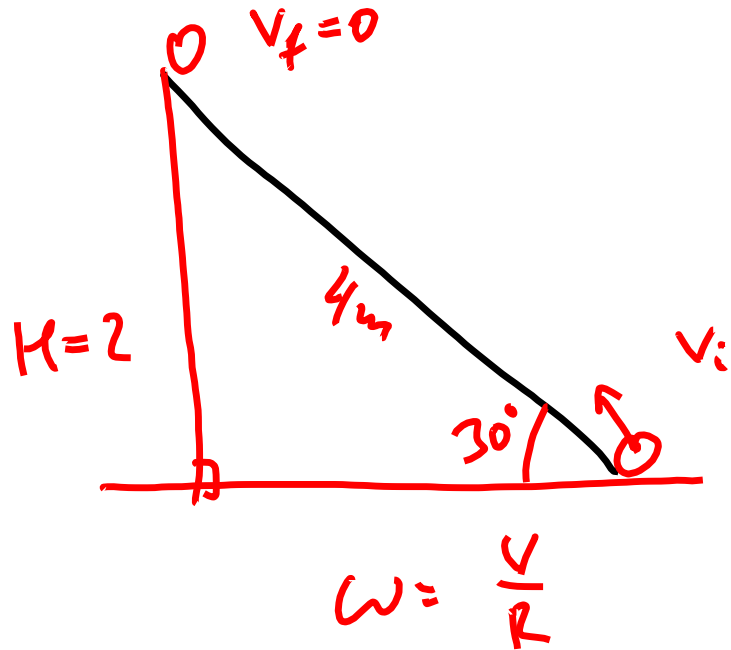
$$PE_i = mgh = 2 \cdot 10 \cdot 2 = 40 \text{ J}$$

$$ME_i = 40 \text{ J}$$

$$PE_f = 0$$

$$KE_f = \frac{1}{2} m V_f^2 + \frac{1}{2} I \omega^2$$

A solid cylinder with the mass of 2 kg rolls without slipping up a ramp inclined at 30° . Find the minimum speed for the cylinder (i.e. of its CofM) needed to travel 4 m.



$$ME_i = PE_i + KE_i = \phi + \frac{1}{2} m v_i^2 + \frac{1}{2} I \omega_i^2$$

$$ME_f = mgh + \phi$$

$$ME_i = ME_f$$

$$\frac{1}{2} \cdot 2 \cdot v_i^2 + \frac{1}{2} \cdot \frac{1}{2} \cdot 2 \cdot \cancel{R^2} \cdot \left(\frac{v_i}{\cancel{R}} \right)^2 = 2 \cdot 10 \cdot 2$$

NO Friction!



NO Rotation!

$$K E = \frac{1}{2} m v^2 + \frac{1}{2} I \omega^2$$

$$\omega \neq \frac{v}{R}$$

$$\omega = 0$$

Physical terms/parameters/quantities

used to describe motion:

position, trajectory, path, origin, reference frame, coordinate, position vector, radius-vector, displacement, magnitude of the displacement, distance traveled, time of motion, elapsed time, average velocity, average speed, instantaneous velocity, instantaneous speed,

=> need to know each definition literally!

Some helpful questions for solving physics problems (page # 12)

1. What objects are involved? What processes are happening to them? (use your imagination - make a picture showing the objects and the processes they are involved into)
 2. What properties of the objects and the processes might be important?
 3. What physical quantities should be used for describing those properties, what connections might be important?
 5. What laws or definitions should be used to describe important connections mathematically?
 6. How can I solve my equations mathematically?
 8. Does it make a sense?
 9. Could I solve a similar problem again? How much time would it take?
- Who could help me (if I need it)?

http://teachology.xyz/general_algorithm.htm

General Problem solving strategy for problems on N2L

1. Read, imagine what is happening
2. Draw a picture, select your system (an object or objects)
3. For each system draw FBD, show all important forces, directions, vectors, quantities (known and unknown)
4. Add the reference frame (x- y- axes, the origin)
5. Write N2L for each system/object (for both components, attention to +/-).
6. Write kinematical equations (Eq., MCV, MCA).
7. Do the math

General strategy for using TBE.

1. Picture
2. Convert picture into a diagram: FBD
3. Convert FBD into torque-diagram by SETTING the axis of rotation
4. Write the actual value (a.c.a a component) for torque of each force relative to the same axis
5. Set TBE and solve it
6. If needed, select another axis or use FBE

Circular and Rotational motion, Rolling:

Linear and angular variables, Centripetal acceleration, Moment of inertia, N2LforRM, RKE, Angular momentum, Work of torque

Friction, Energy and Work, momentum, collisions: Kinetic and static friction, work of a constant force, kinetic and potential energy, WKET, LCME, LCLM.