

Lab 8 is in SCI 134

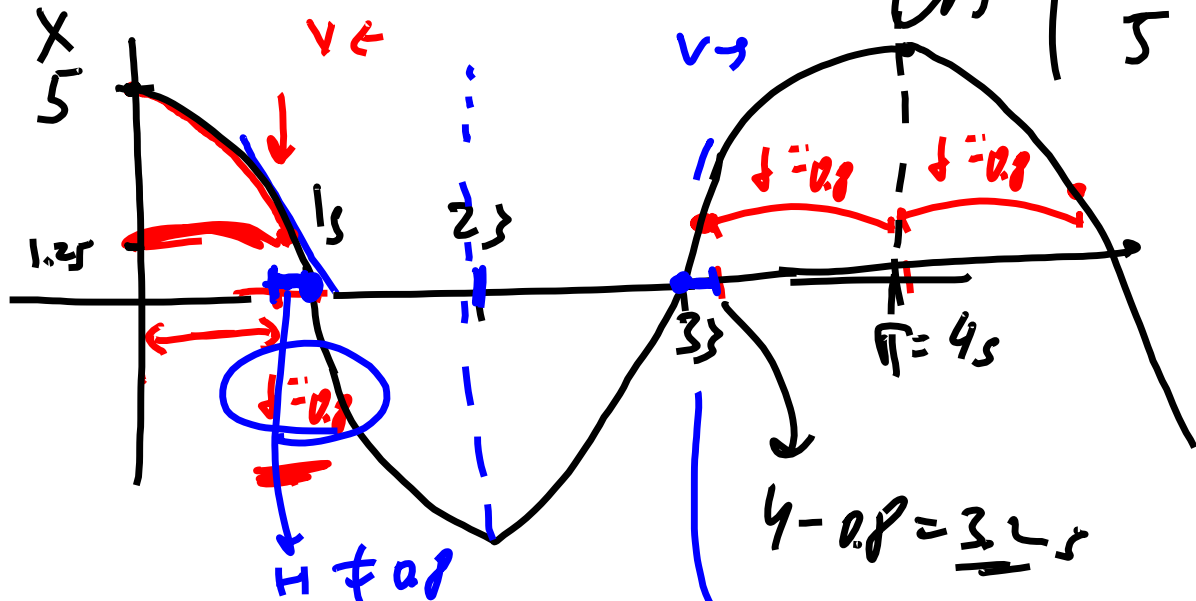
Please, login into webassing, locate
LectureMCQ_L20 (PY105)
and answer question 1
(but **ONLY Q1!**).



Good morning!

$$X = 5 \cos\left(\frac{\pi}{2} \cdot t\right)$$

$$\cos^{-1}\left(\frac{1.25}{5}\right) = \frac{\pi}{2} \cdot t \pm 2\pi$$

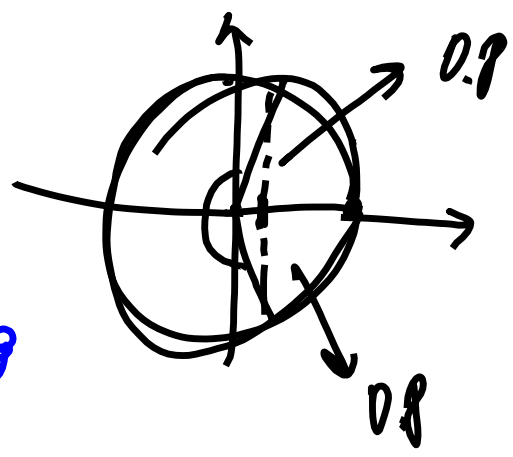


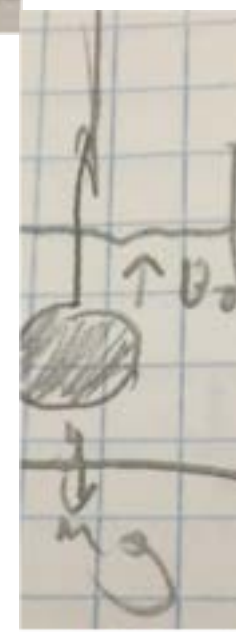
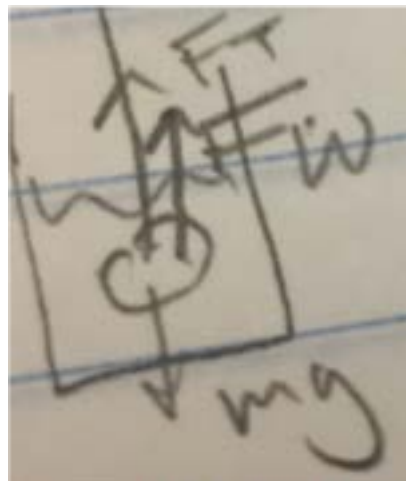
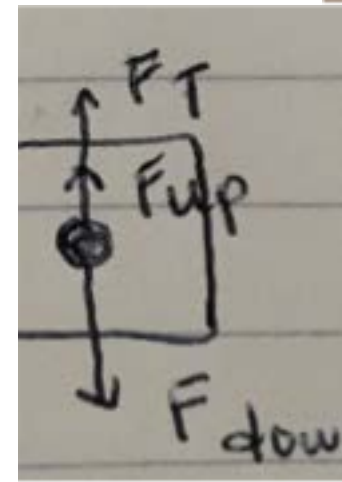
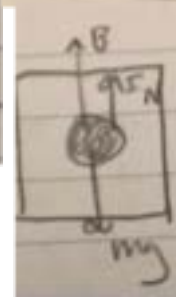
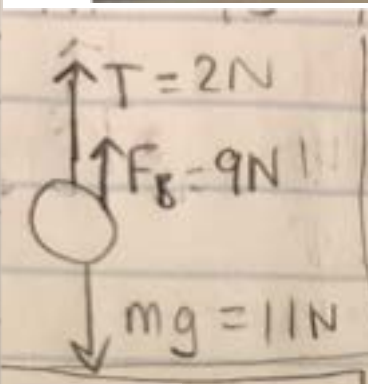
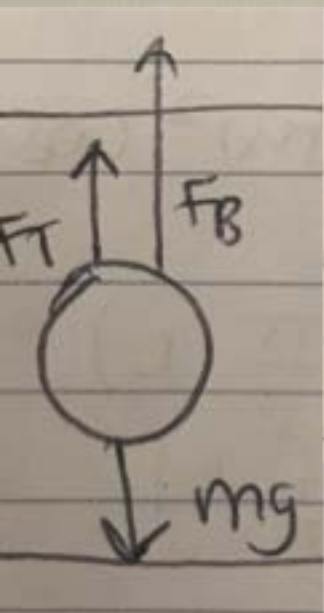
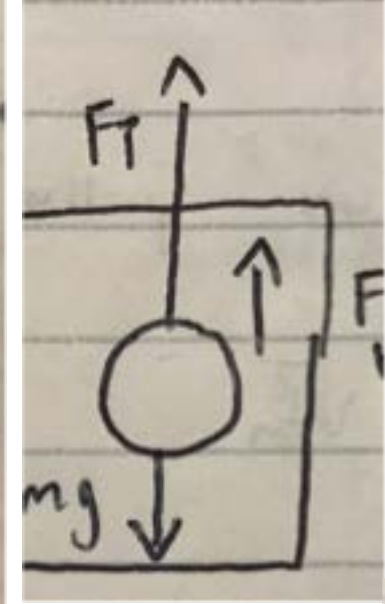
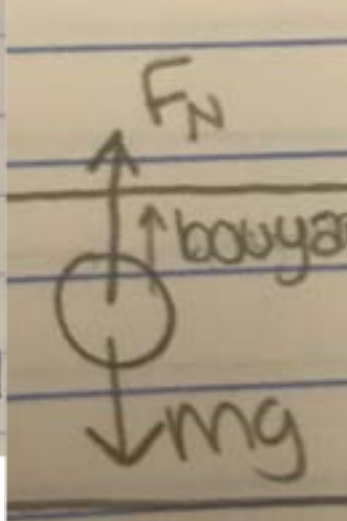
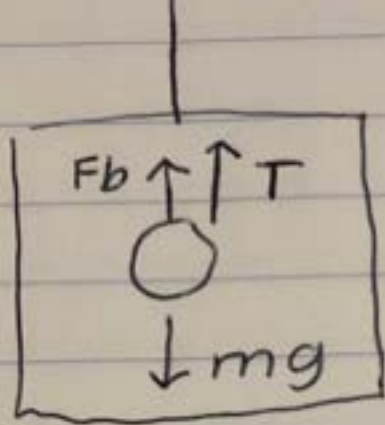
$$1 - 0.8 = 0.2$$

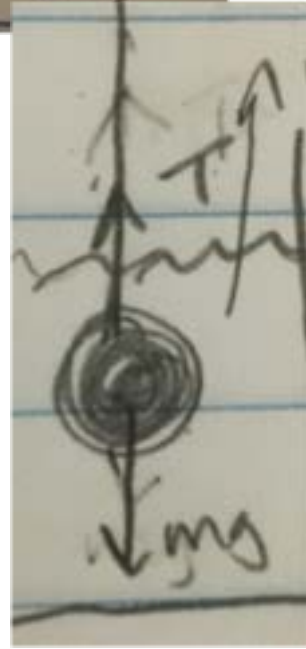
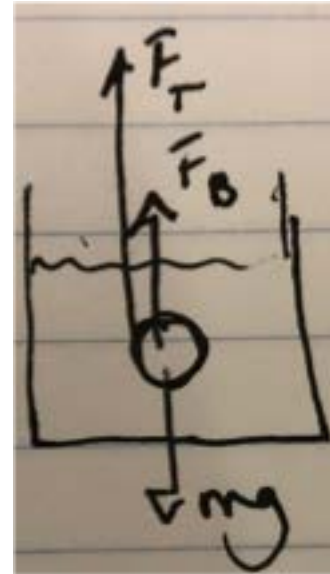
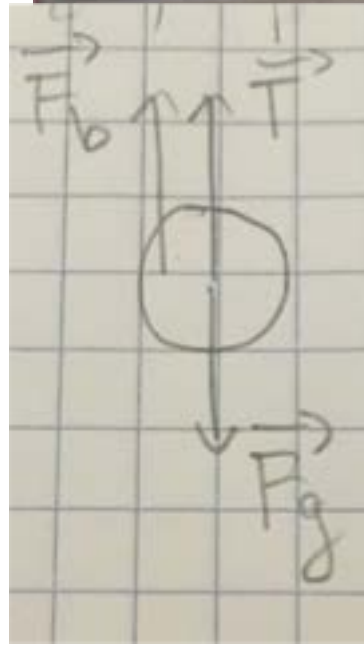
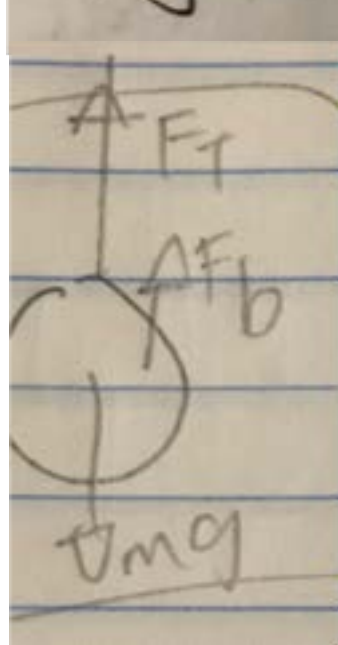
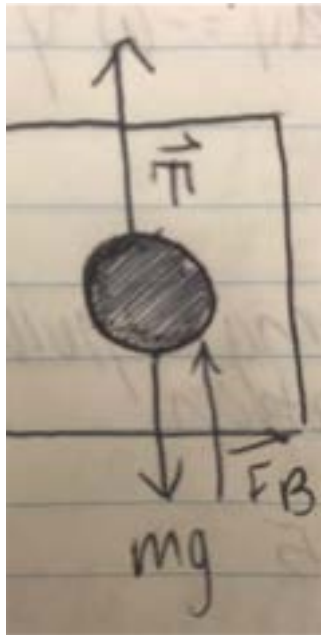
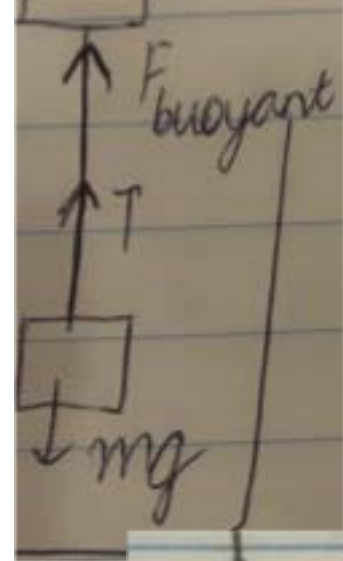
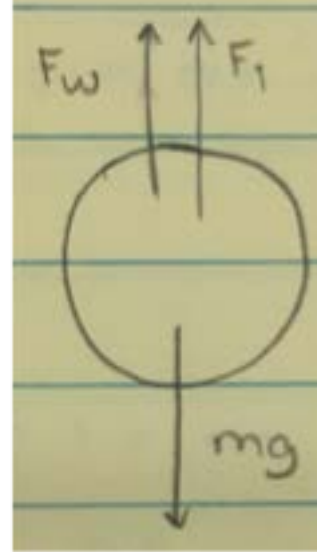
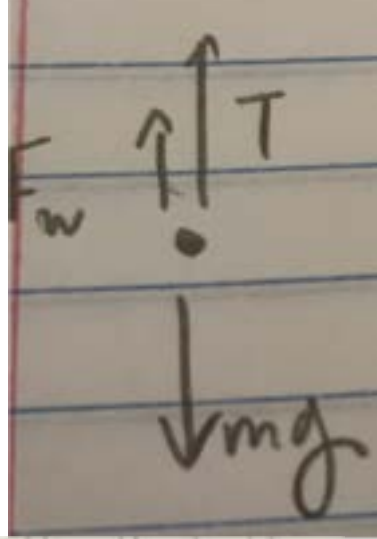
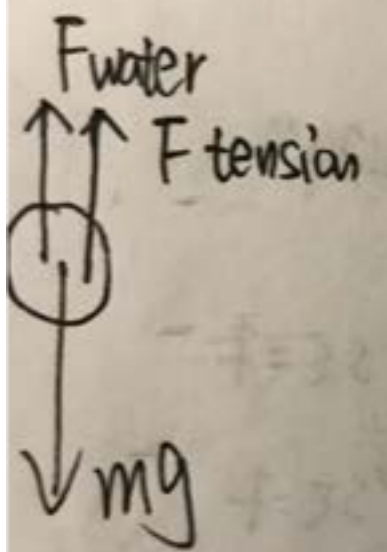
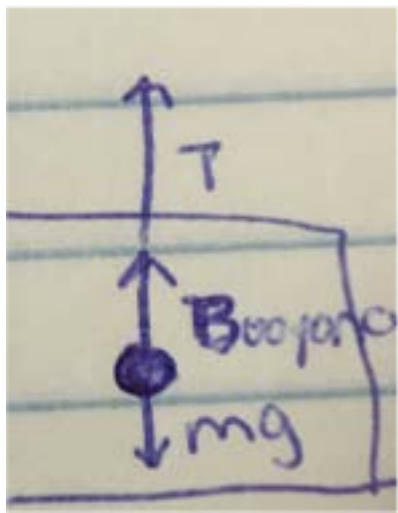
$$4 - 0.8 = 3.2s$$

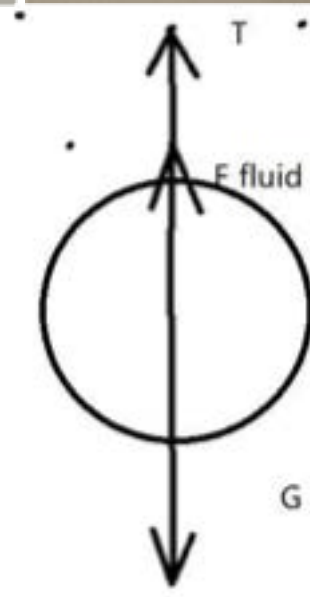
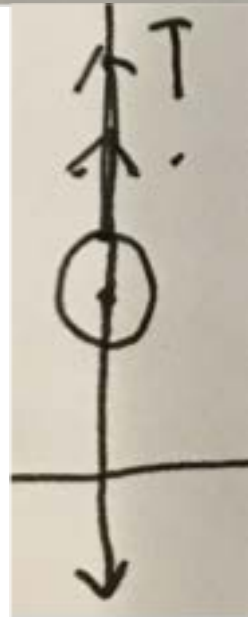
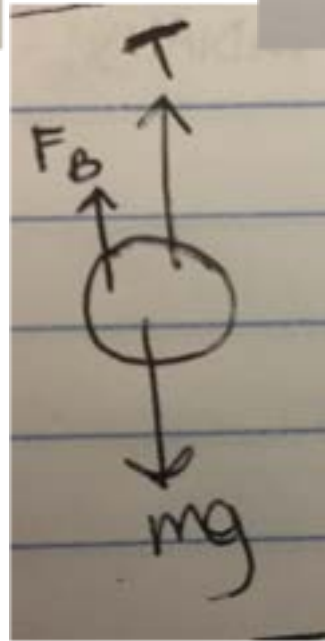
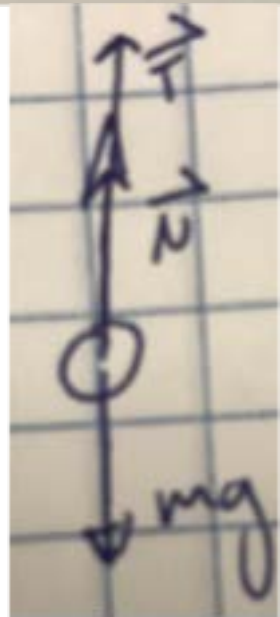
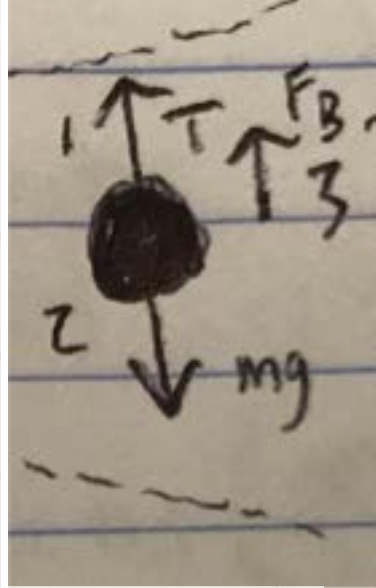
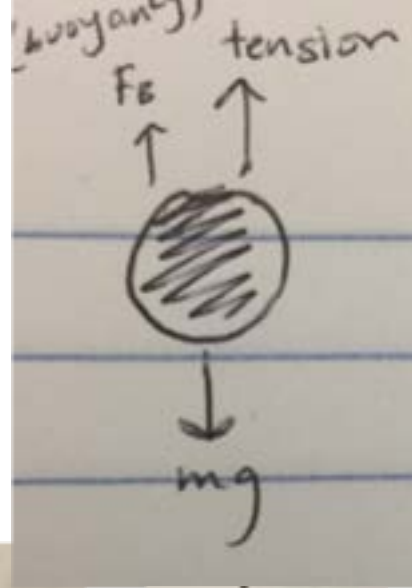
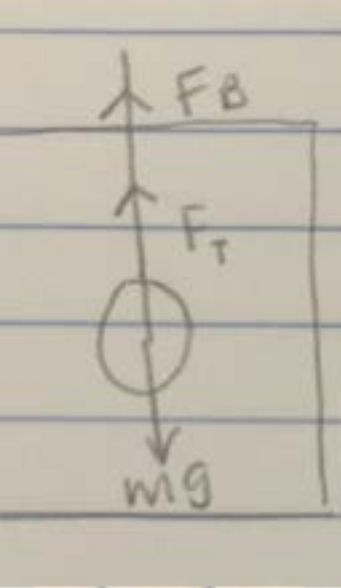
$$t^* = 3 + 4 = 7 + 0.8$$

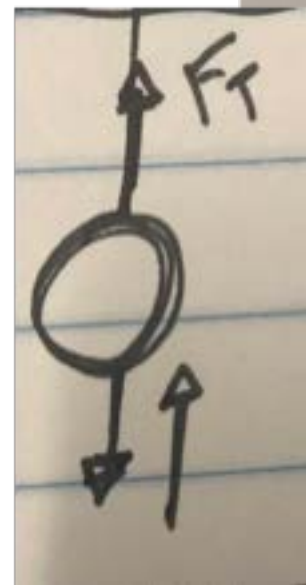
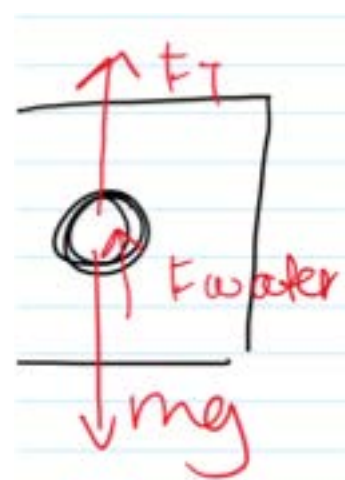
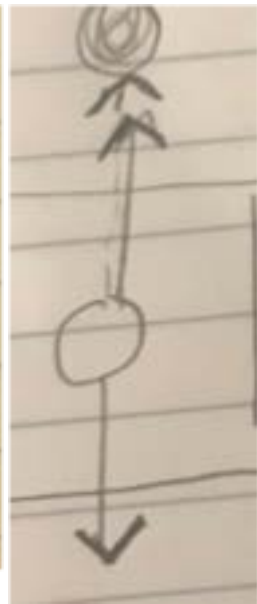
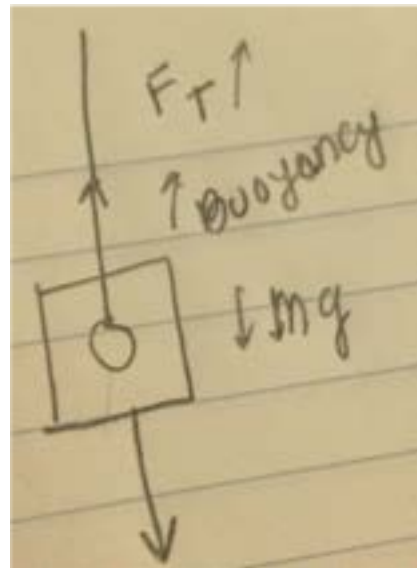
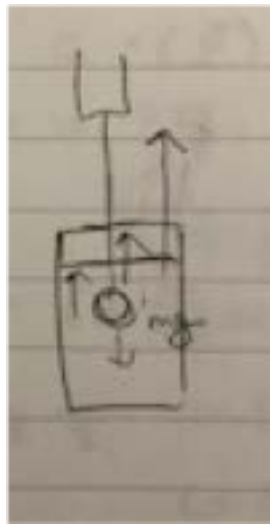
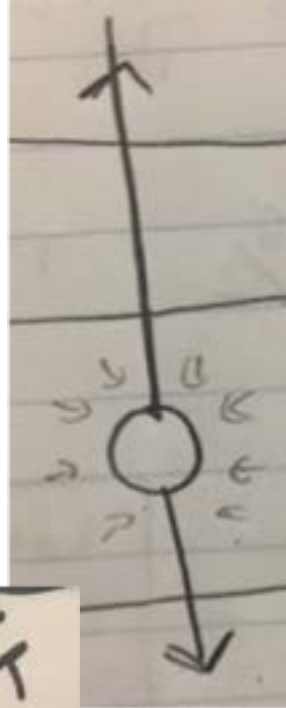
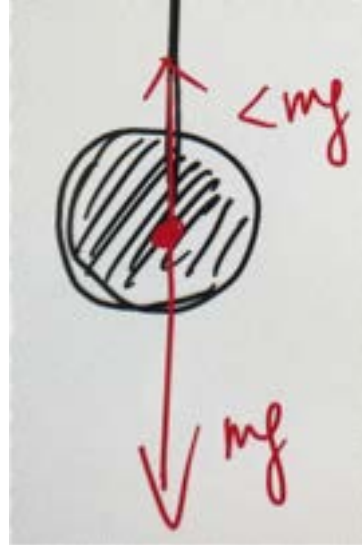
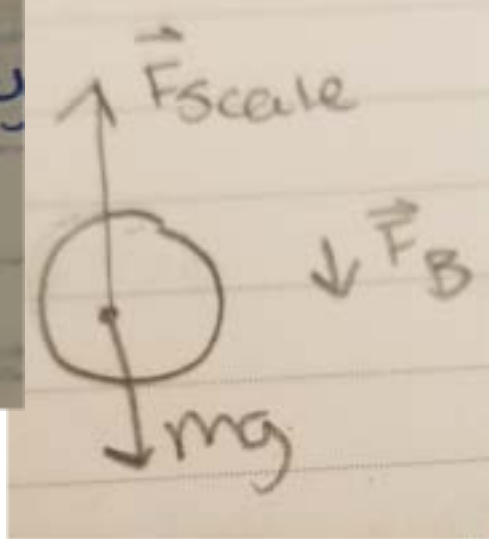
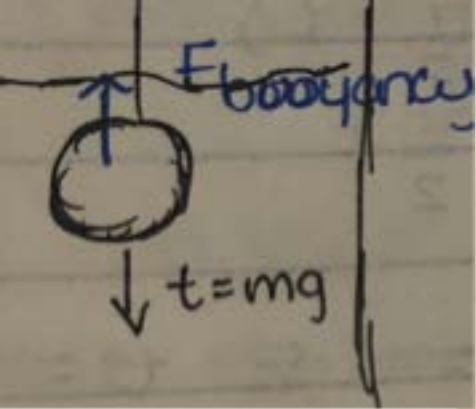
$$3 + 0.2 = 3.2$$

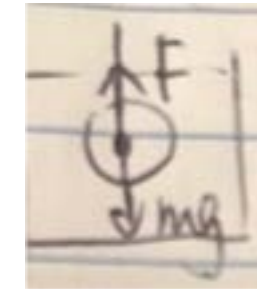
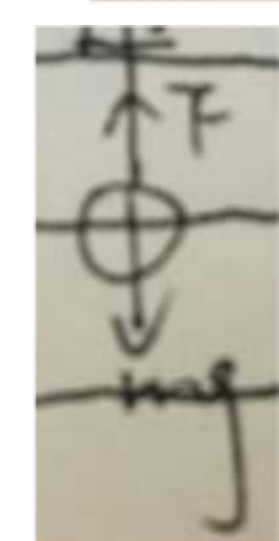
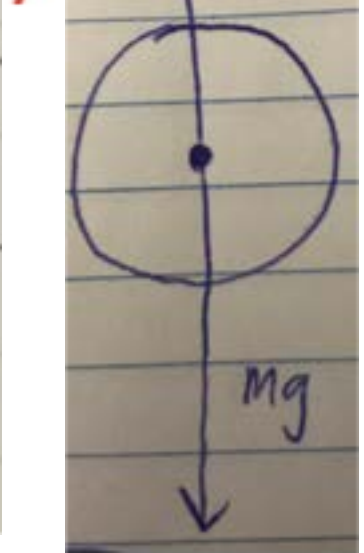
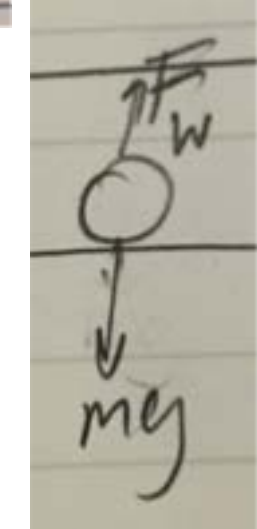
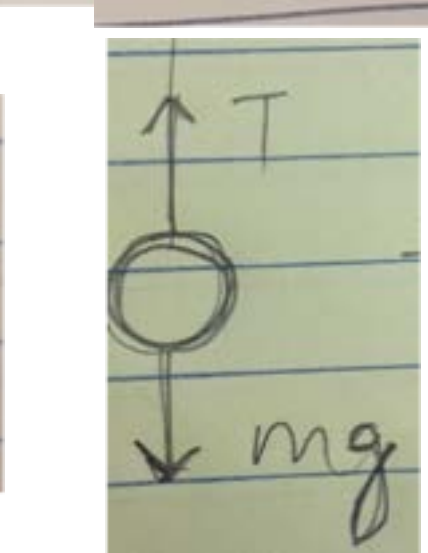
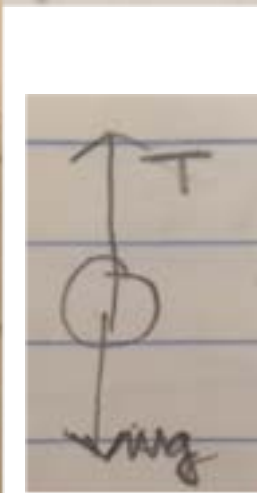
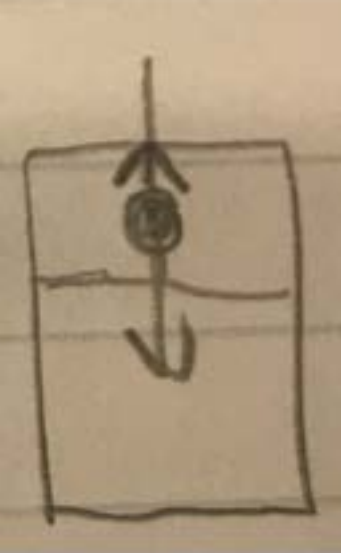
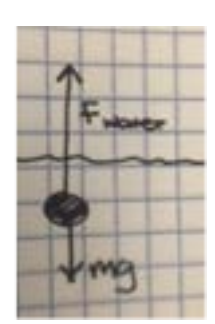
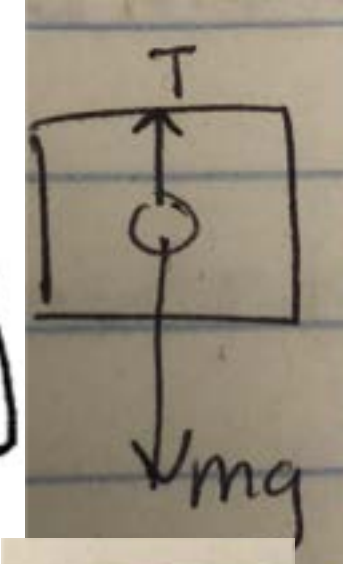
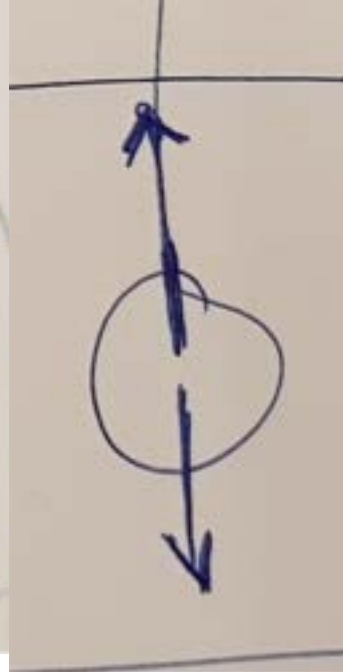
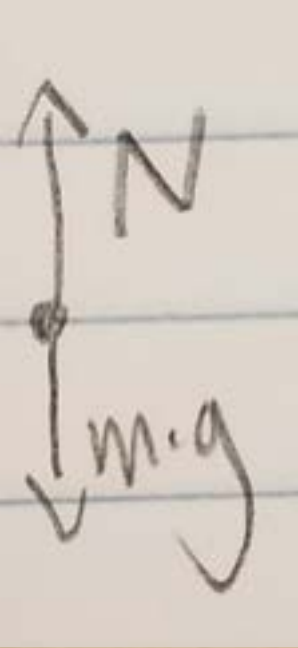


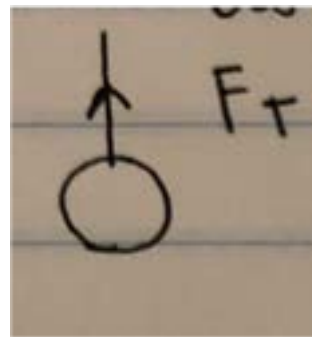
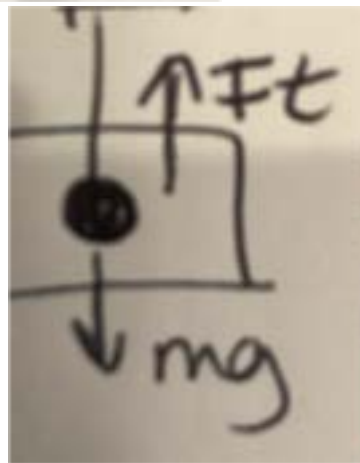
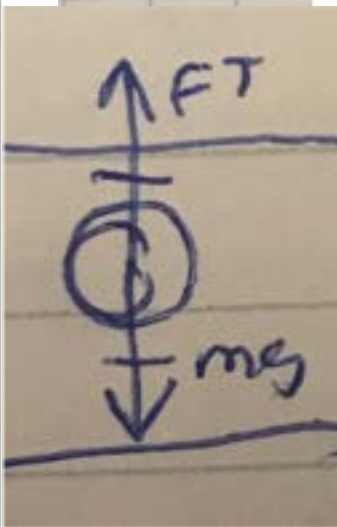
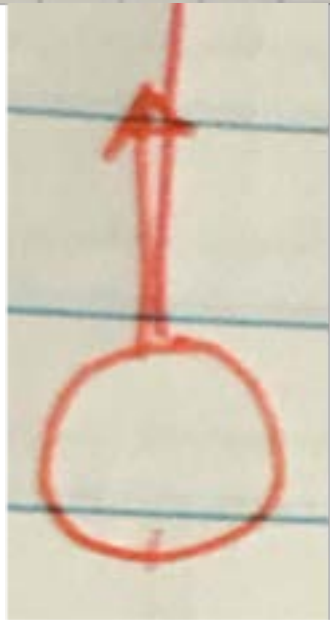
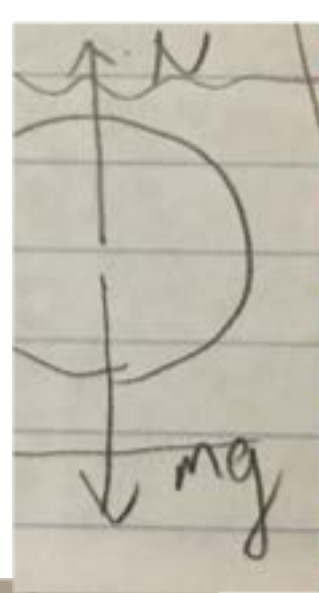
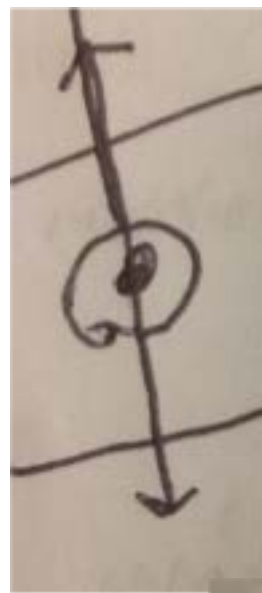
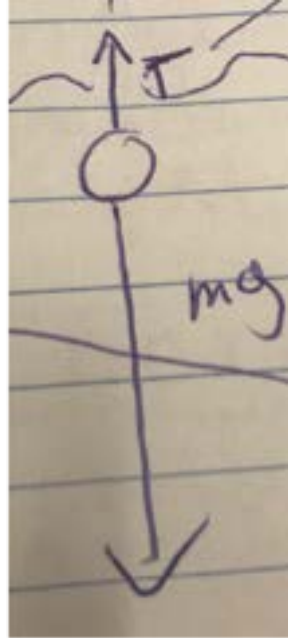
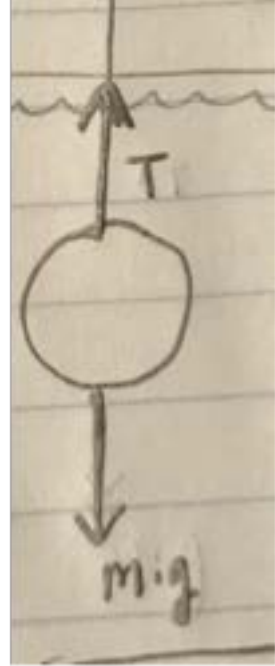
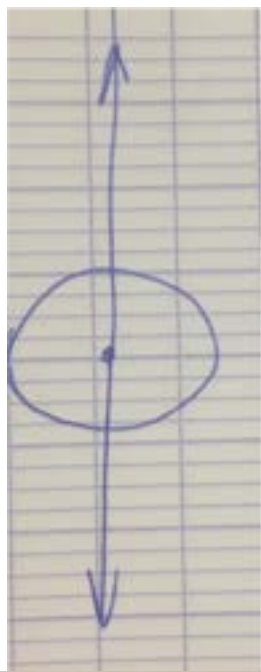
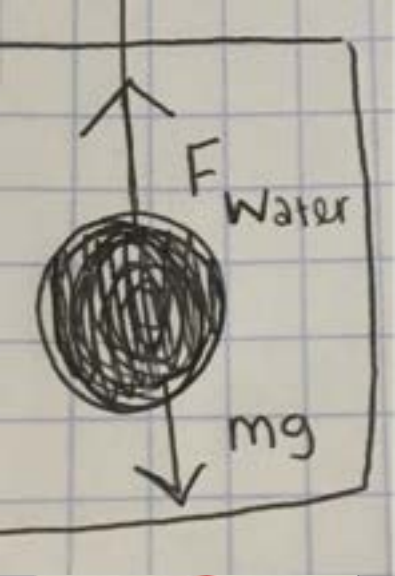


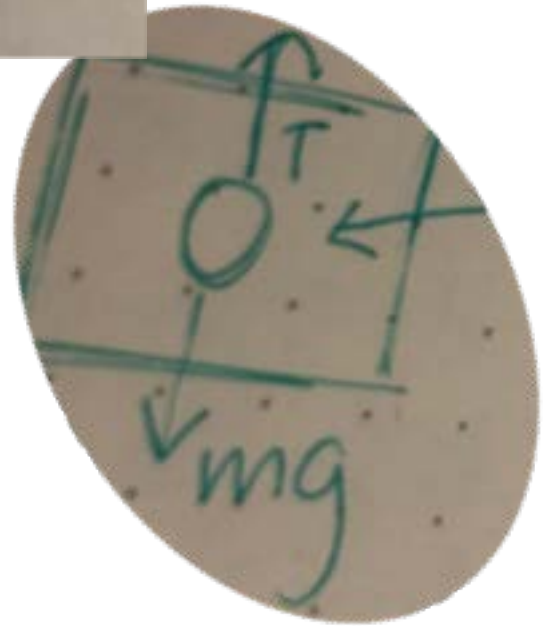
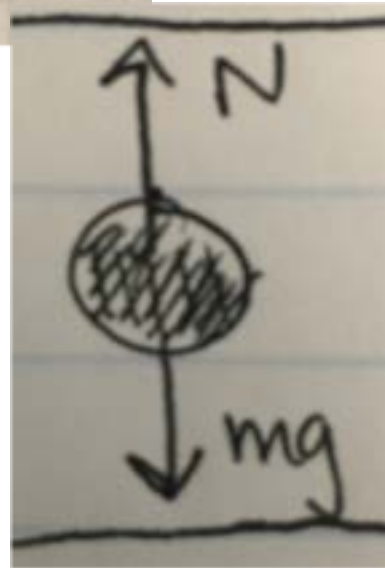
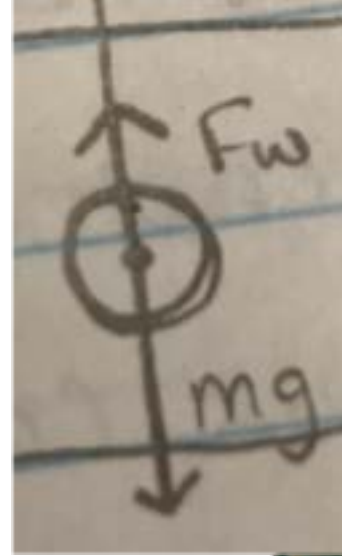
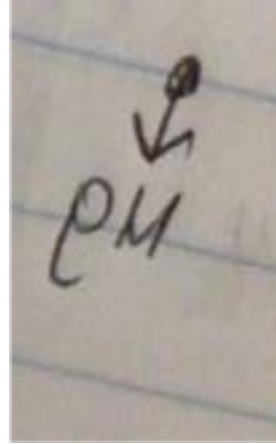
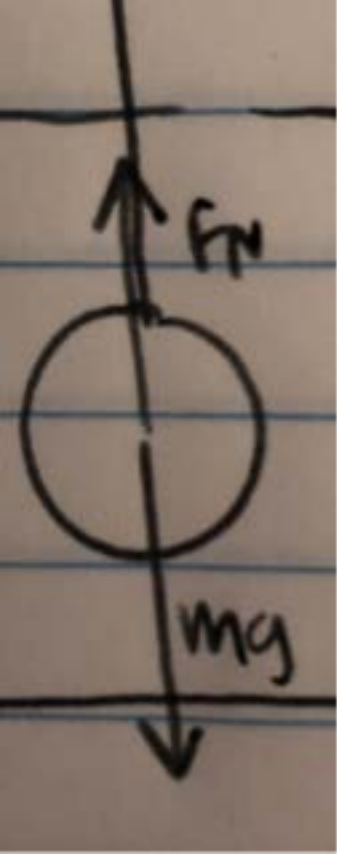




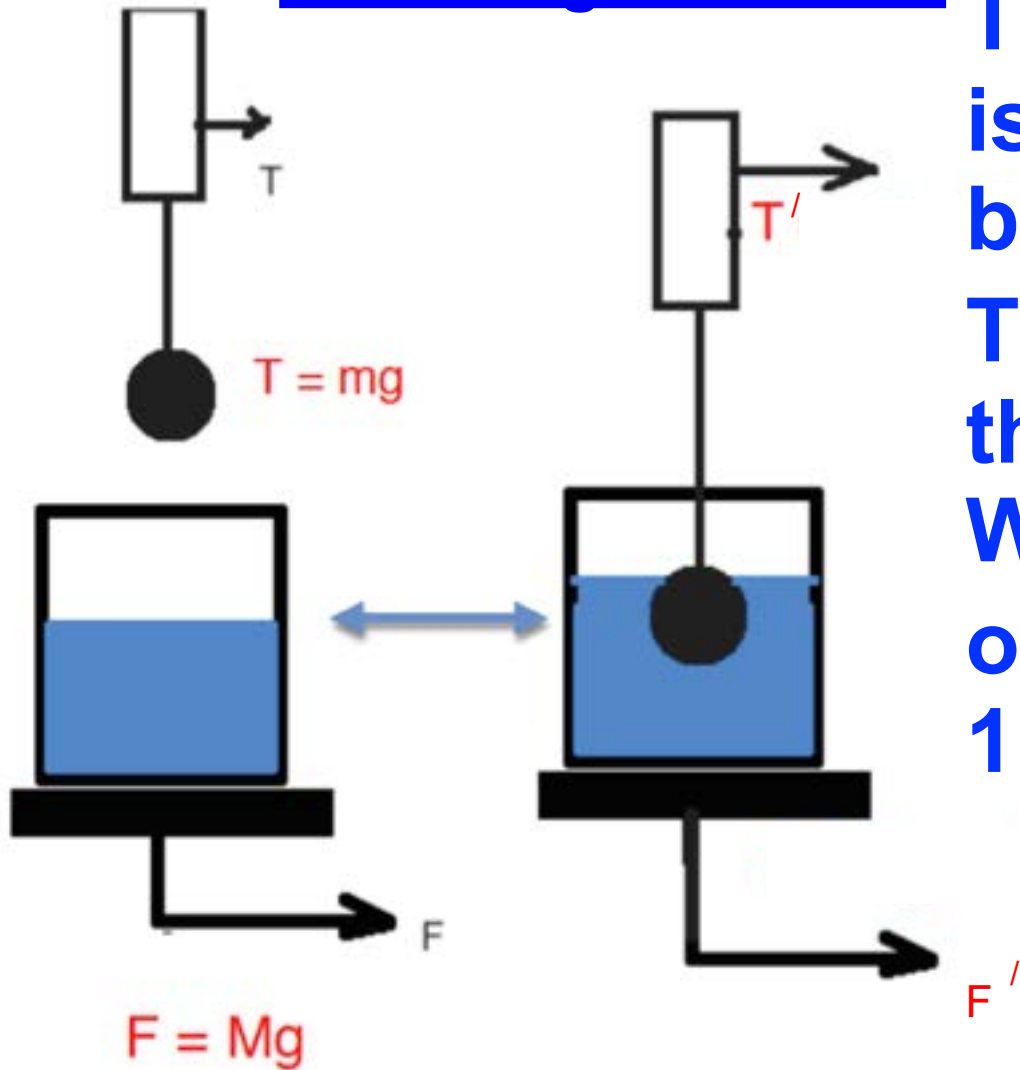








Webassign: L20 Q2

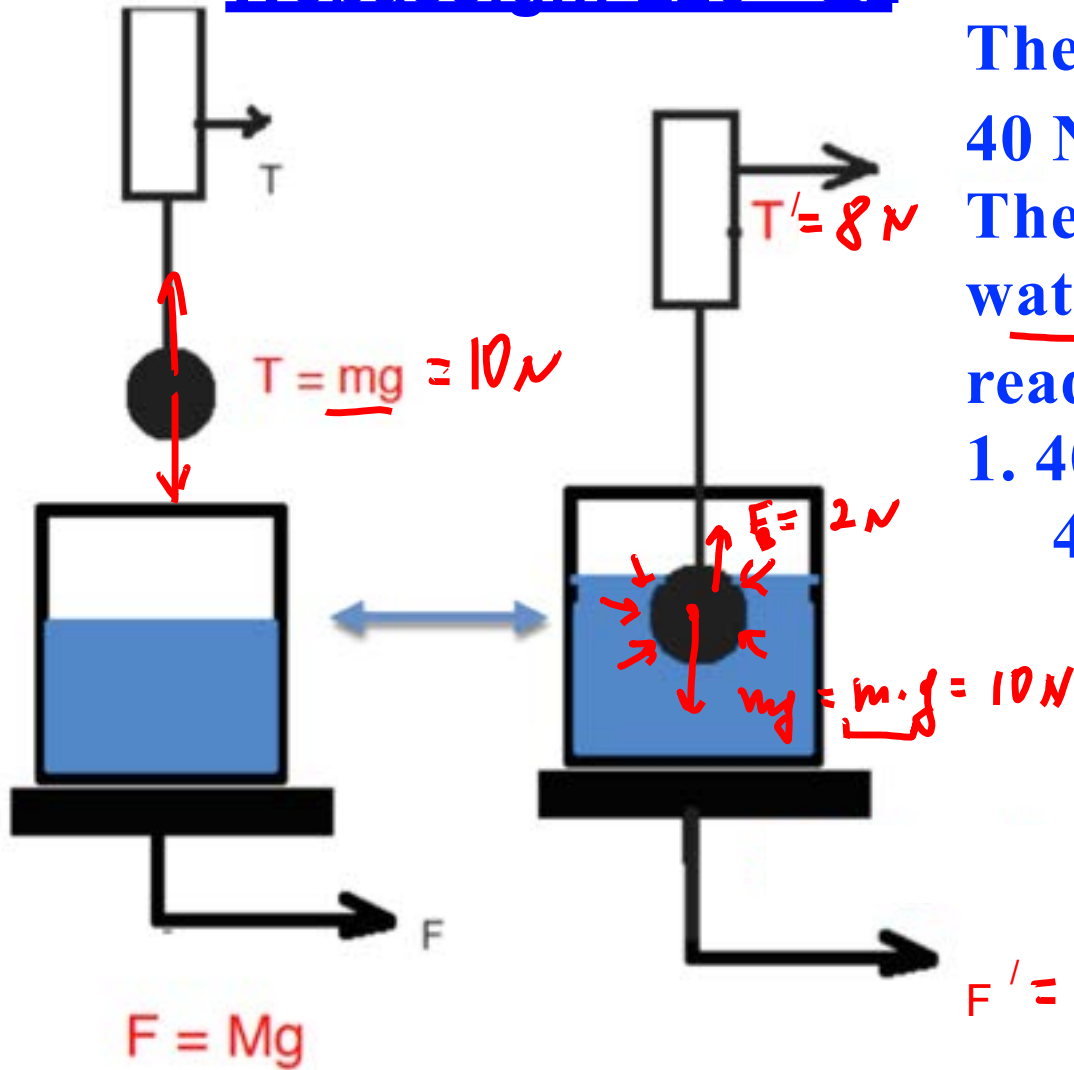


The weight of a ball in air is 10 N. The weight of a beaker with water is 40 N. The apparent weight of the ball in water is 8 N. What is the new reading of the scale?.

- 1. 40 N
- 2. 41 N
- 3. 42 N
- 4. 43 N
- 5. 44 N ...



Webassign: L20 Q2

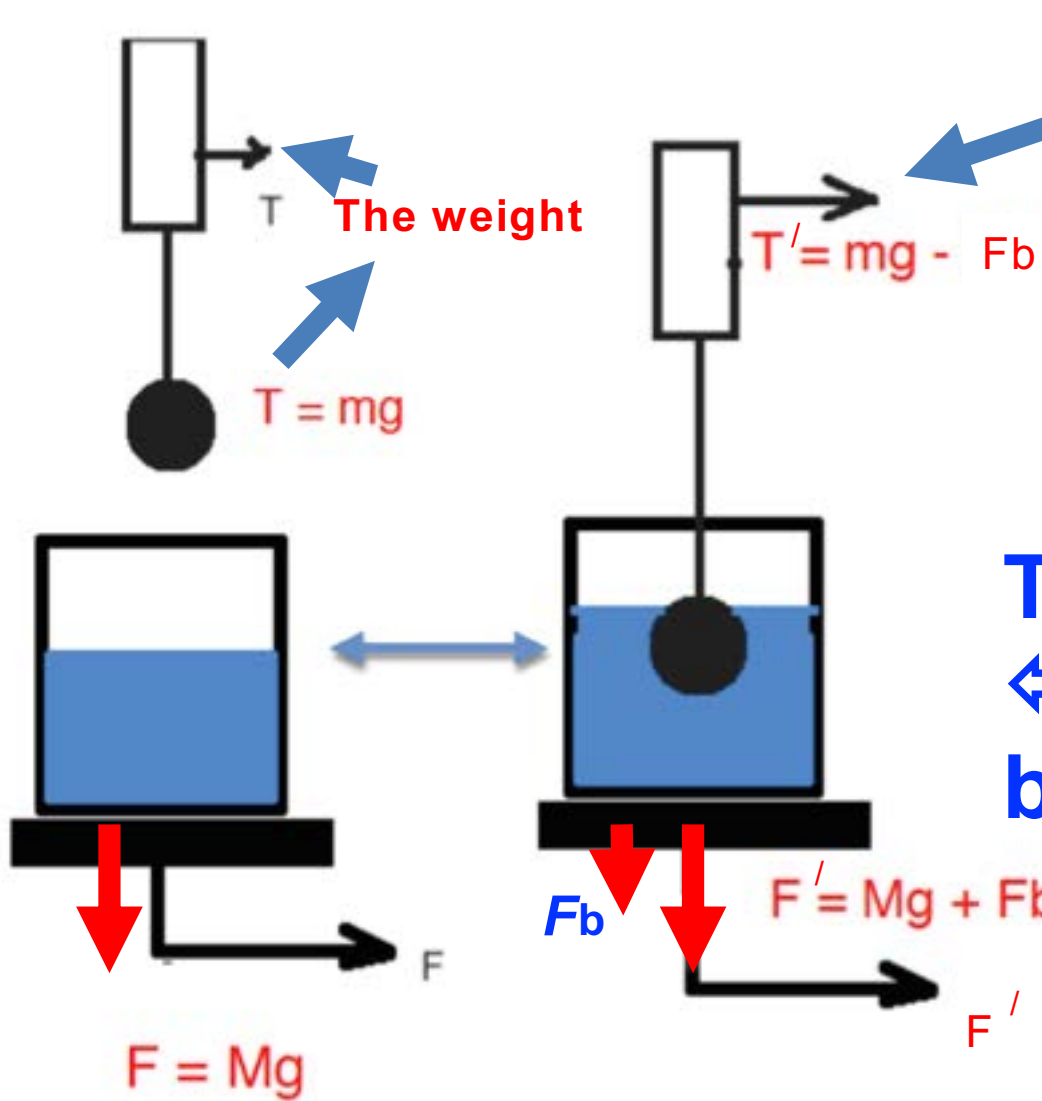


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The weight of a beaker with water is 40 N.

The apparent weight of the ball in water is 8 N. What is the new reading of the scale?

- 1. 40 N
- 2. 41 N
- 3. 42 N
- 4. 43 N
- 5. 44 N ...

$F' = 40 + 2 = 42\text{ N}$



The weight

$$T = mg$$

$$T' = mg - F_b$$

The apparent weight

$$F_b + T' = mg$$

\Rightarrow

$$F_b = mg - T' = T - T'$$

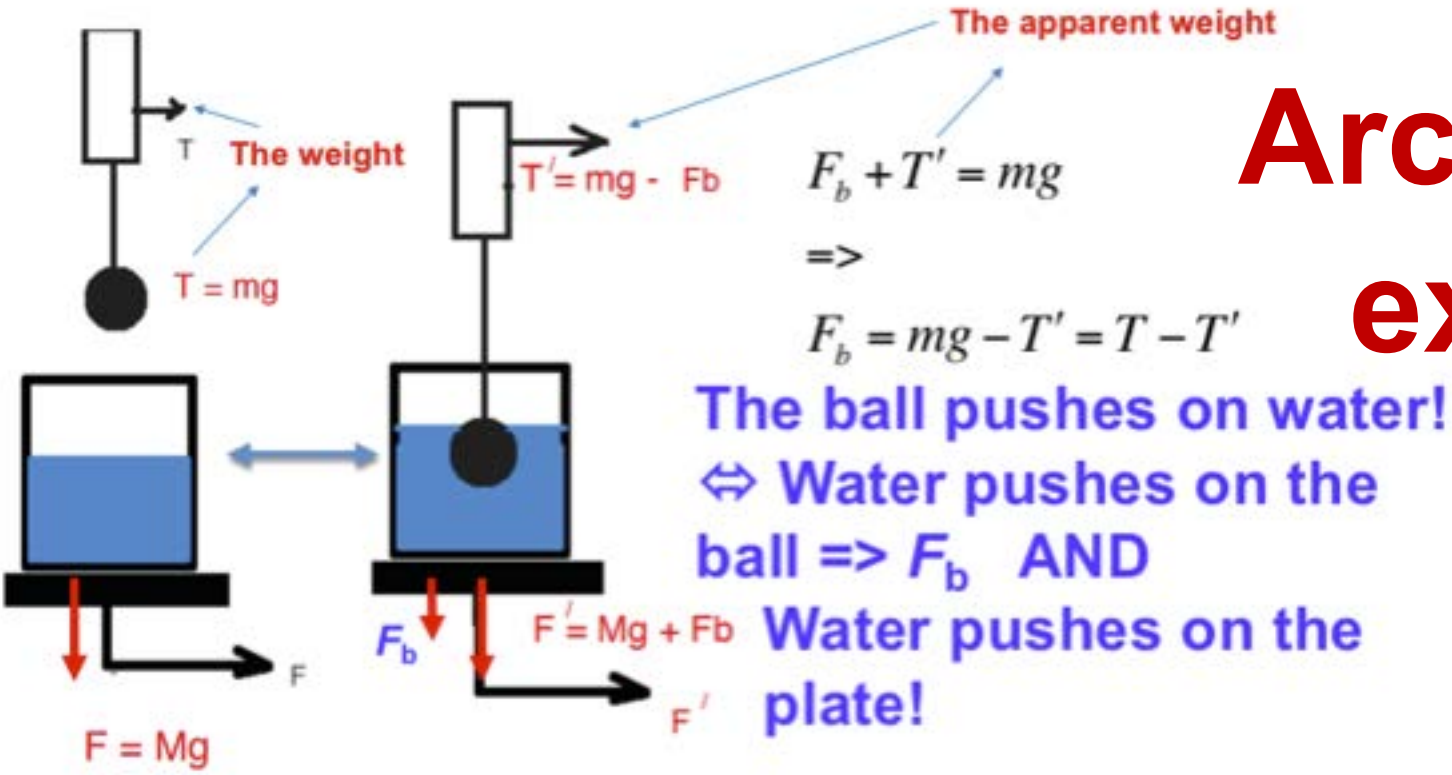
The ball pushes on water!

\Leftrightarrow Water pushes on the ball $\Rightarrow F_b$ AND

Water pushes on the plate!

Water pushes on the plate!

Archimedes experiment (~250 BC)



<https://en.wikipedia.org/wiki/Archimedes>

Buoyant force!

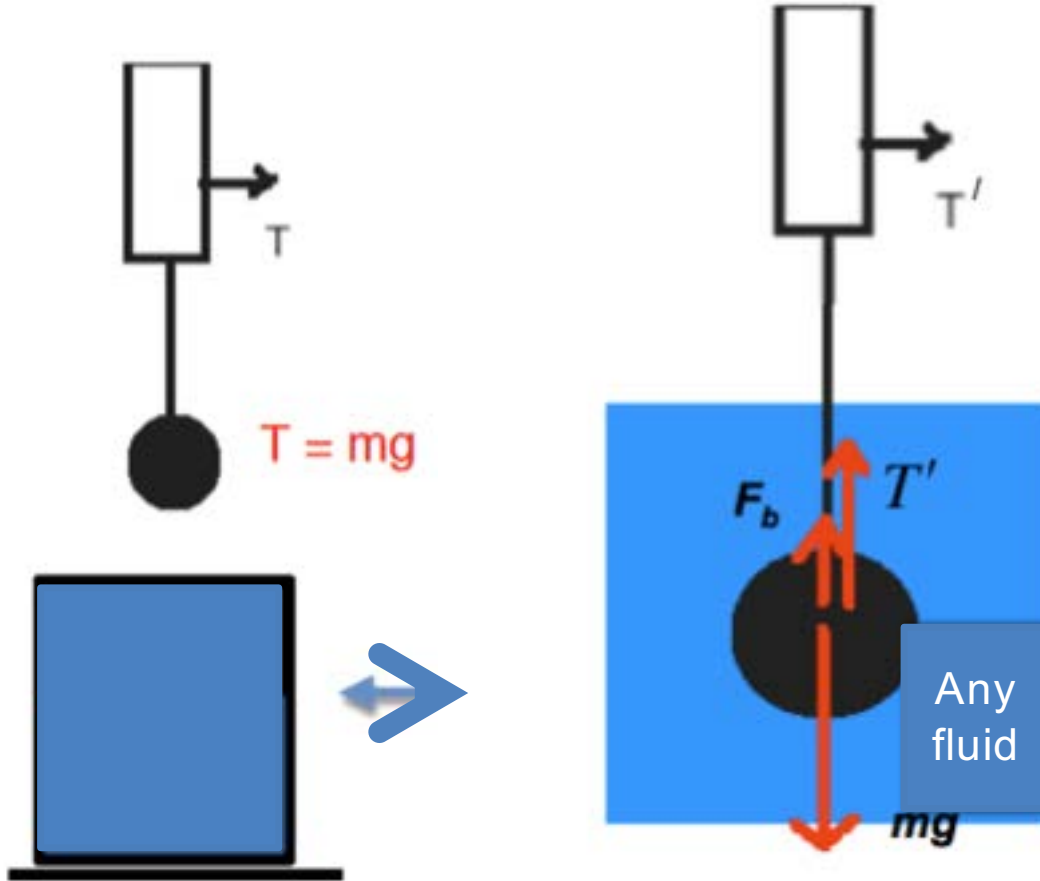
$$F_B = T - T'$$

And **ALWAYS**

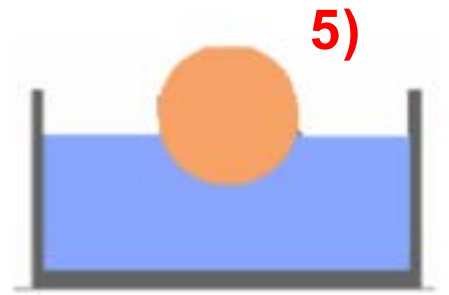
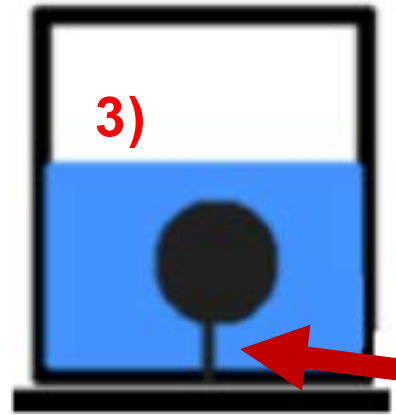
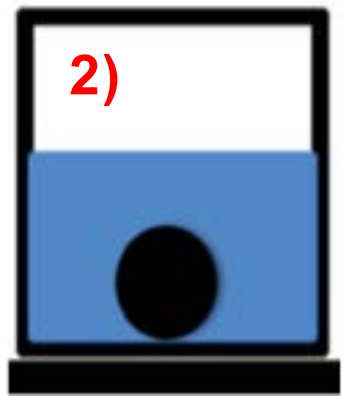
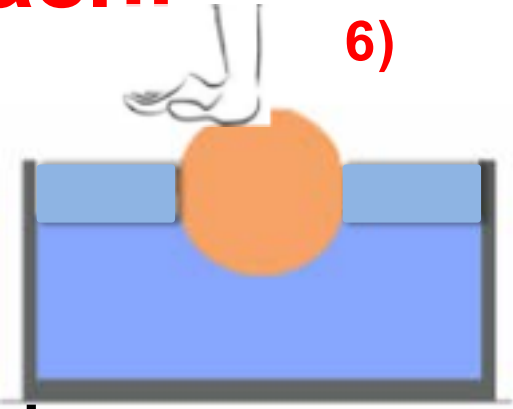
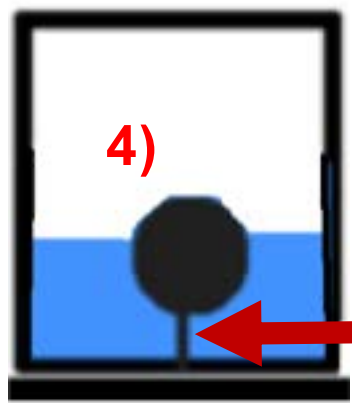
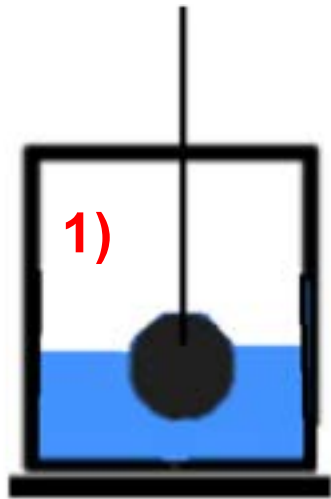
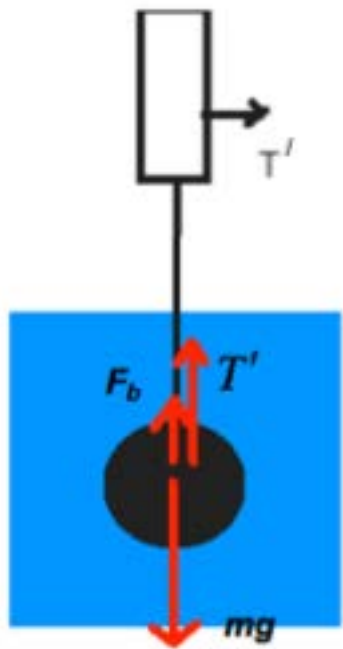
$$F_B = m_{\text{fluid_displaced}} * g$$

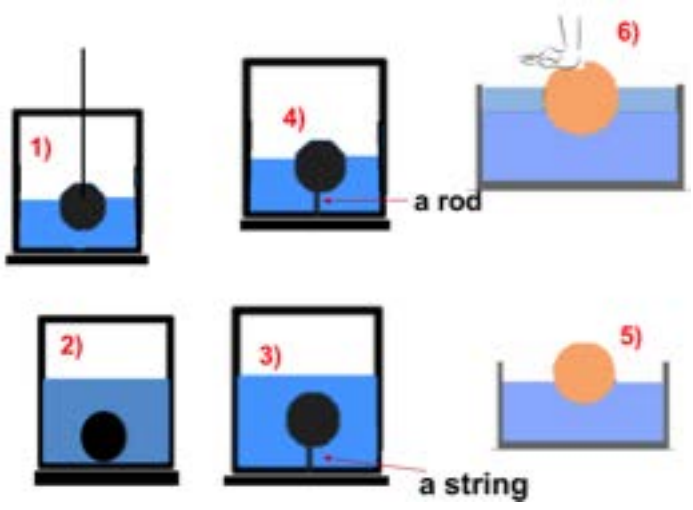
Not just water!

$F_B =$ the weight of the fluid *displaced* by an object! by Archimedes

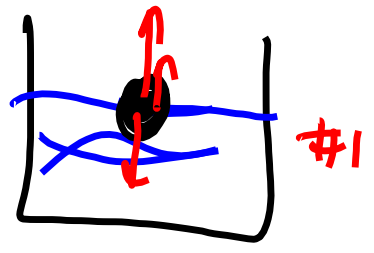
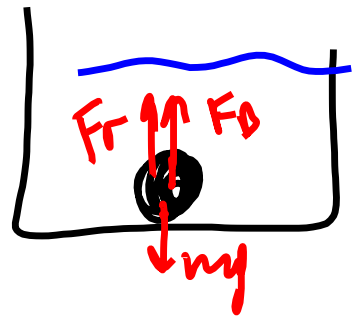


Typical situations: draw FBD for each!

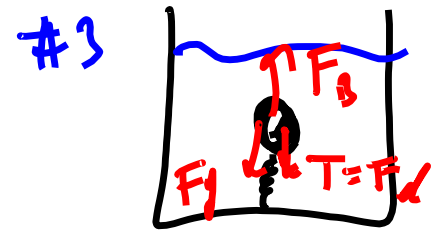




#2



#1

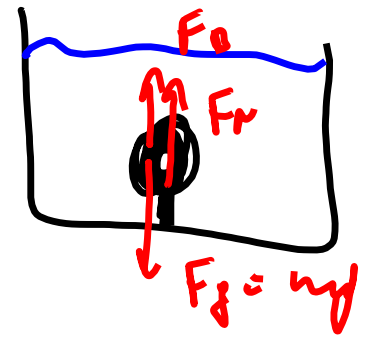


#3



#6 a

#4



#5



#6 b ⇒ #5



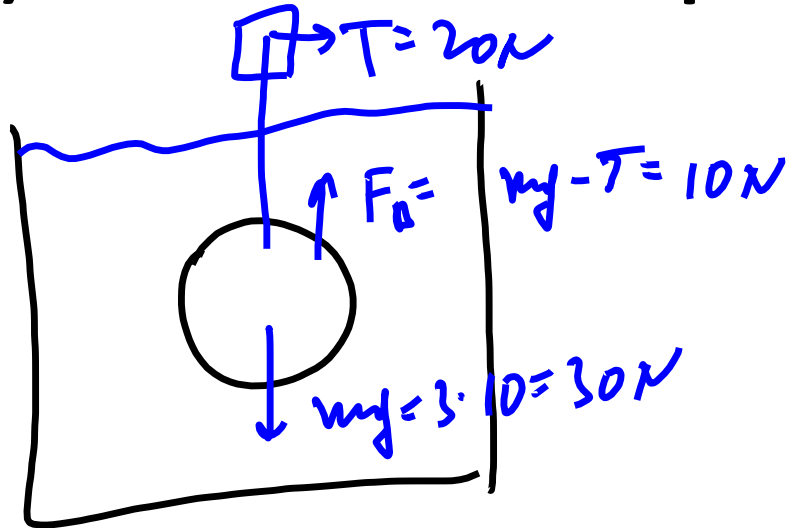
**A general strategy for solving problems on
buoyant force.**



**Is essentially the same as a general strategy
for solving problems on ANY force!**

- 1. Draw a picture, convert it into FBD.**
- 2. Set FBE (N2L for Equilibrium)**
- 3. If necessary, add additional relationships
(think what variables are connected: F_B , m , g , ρ ,
 V , etc. – depending on forces and geometry)**
- 4. Solve**

When a 3 kg ball with diameter of 10 cm is completely immersed in some fluid its apparent weight is 20 N. Find the magnitude of the buoyant force acting on the ball. How much fluid (in kg and m^3) does the ball displace?

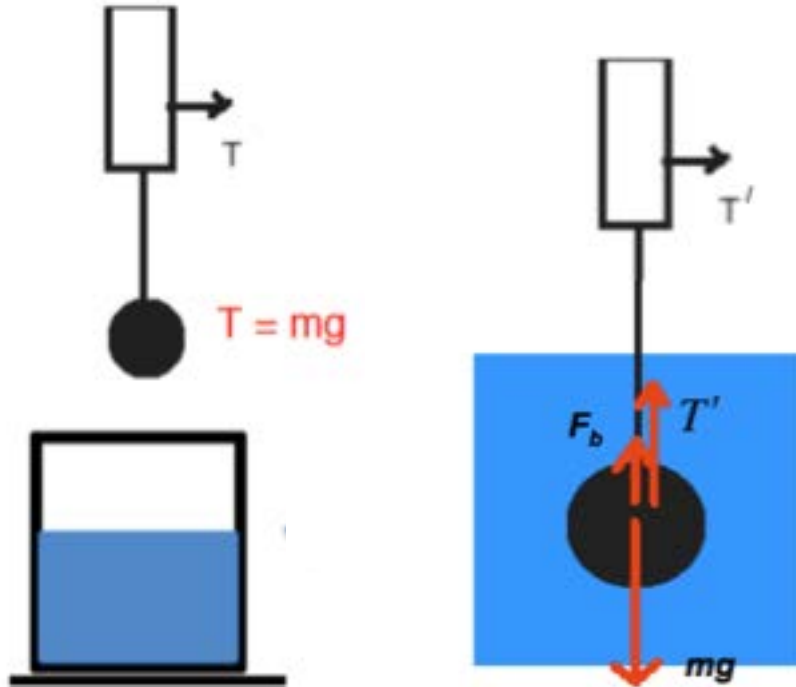


$$F_b = \frac{W}{\text{Fl. d. by } a} = m_f \cdot g$$

$$10N = m_f \cdot g \Rightarrow m_f = 1\text{kg}$$

$$V_{\text{fl. d. by } a} = V_{\text{obj. in fl.}} = \frac{4}{3}\pi r^3 = \frac{4}{3}\pi (0.05)^3$$

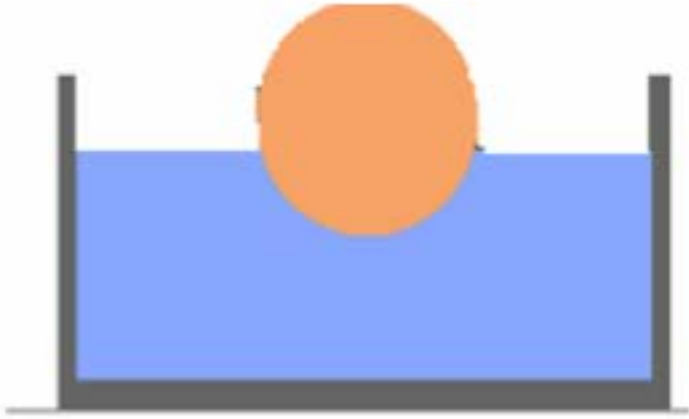
When a 3 kg ball with diameter of 10 cm is completely immersed in some fluid its apparent weight is 20 N. Find the magnitude of the buoyant force acting on the ball. How much fluid (in kg and m³) does the ball displace?



$$F_B = T - T' = 3 \cdot 10 - 20 = 10 \text{ N}$$

$$m_{\text{fluid_displaced}} = F_B / g = 1 \text{ kg}$$

$$V = \frac{4}{3} \pi \left(\frac{0.1}{2} \right)^3 = 0.0005 \text{ m}^3$$



A basketball floats in a bathtub of water.

The ball has a mass of 0.5 kg and a diameter of 22 cm (0.22 m).

[Webassign: L20 Q3](#)

What is the buoyant force?

How many forces are acting on the ball?

1 2 3 ...

How much water (in kg) does the ball displace?





A basketball floats in a bathtub of water.

The ball has a mass of 0.5 kg and a diameter of 22 cm (0.22 m).

$$F_B = m_{\text{fluid_displaced}} \cdot g$$

What is the buoyant force?

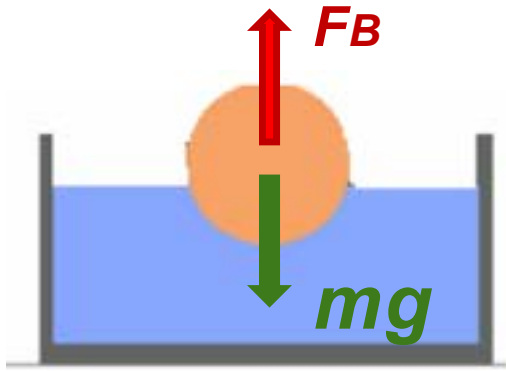
How much fluid (in kg) does the ball displace?

$$F_b = mg = 0.5 \cdot 10 = 5 \text{ N} \Rightarrow 5 = m_{\text{fl}} \cdot g \Rightarrow m_{\text{fl}} = \frac{5}{10} = 0.5 \text{ kg}$$

Webassign: L20 Q3

How many forces are acting on the ball?

1 2 3 ...



A basketball floats in a bathtub of water.
The ball has a mass of 0.5 kg and
a diameter of 22 cm (0.22 m).

$$g = 9.8 \text{ m/s}^2$$

(a) What is the buoyant force?

The ball is in equilibrium, hence

$$F_b = W = mg = 4.9 \text{ N}$$

$$F_B = m_{\text{fluid_displaced}} * g \quad \Rightarrow \quad m_{\text{fluid_displaced}} = F_B/g = 490 \text{ g}$$

Buoyant force! (Again)

Any fluid!

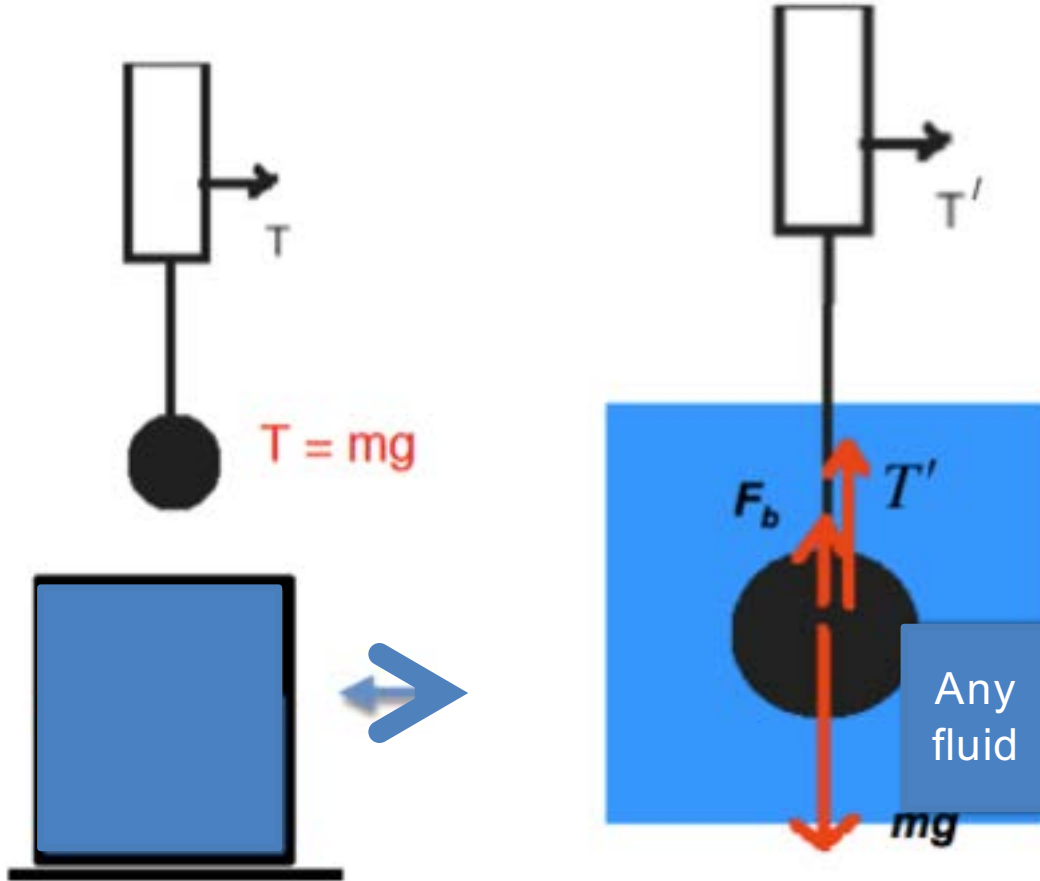
$$F_B = T - T'$$

And ALWAYS

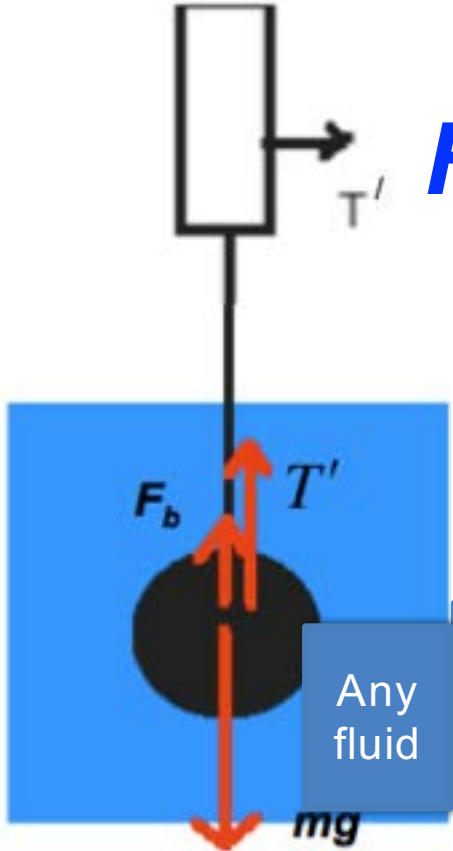
$$F_B = m_{\text{fluid_displaced}} * g$$

Not just water!

F_B = the weight of the fluid displaced by an object!



Any fluid!



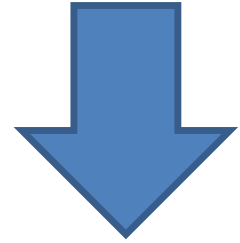
$$F_B = m_{\text{fluid_displaced}} * g$$

Not just water!

F_B = the weight
of the fluid
displaced by an
object!

Experiments!

The same ball;
DIFFERENT fluids



DIFFERENT F_B



???

To describe how much matter (or how many elementary particles) there are on average in the medium the physical quantity Density is used.

Density (ro) $\rho = \frac{m}{V}$ (kg/m³) $\rightarrow m = \rho V$

Some Densities

Material (or object)	Density (kg/m ³)
Air (20 ⁰ C and 1 atmosphere)	1.21
Water (4 ⁰ C and 1 atmosphere)	1000
Iron	7900
Mercury (the metal)	13600
Earth (the planet, on average)	5500

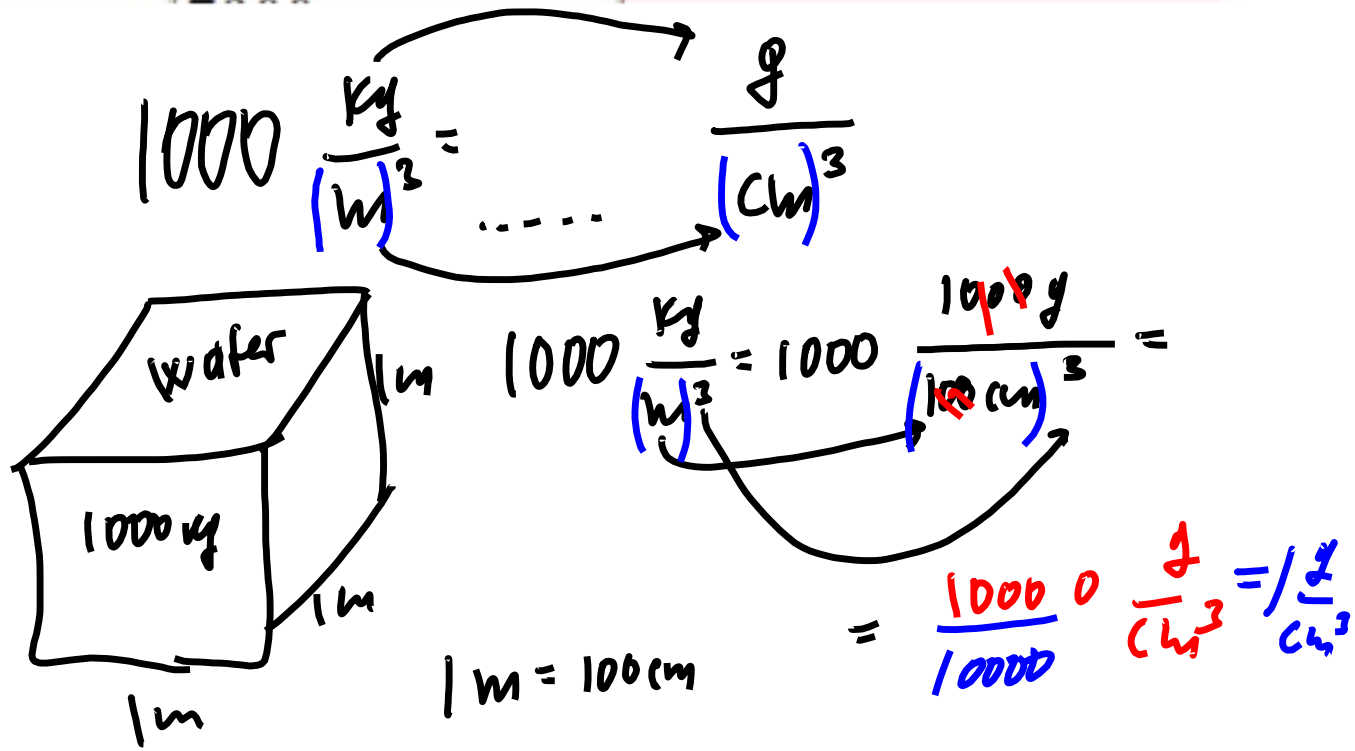
= ?? g /cm³



Webassign: L20 Q4

Water (4°C and 1 atmosphere)	1000 kg/m ³	= ?? g/cm ³
------------------------------	------------------------	------------------------

- 1. 1000 g/cm³
- 2. 100 g/cm³
- 3. 10 g/cm³
- 4. 1 g/cm³
- 5. 2000 g/cm³
- 6. 200 g/cm³
- 7. 20 g/cm³
- 8. 2 g/cm³
- 9. None of the above



To describe how much matter (or how many elementary particles) there are on average in the medium the physical quantity Density is used.

Density (ro) $\rho = \frac{m}{V}$ (kg/m³) $\rightarrow m = \rho V$

Some Densities

Material (or object)	Density (kg/m ³)
Air (20 ⁰ C and 1 atmosphere)	1.21
Water (4 ⁰ C and 1 atmosphere)	1000
Iron	7900
Mercury (the metal)	13600
Earth (the planet, on average)	5500

= 1 g /cm³

To describe how much matter (or how many elementary particles) there are on average in the medium the physical quantity Density is used.

$$\text{Density (ro)} \quad \rho = \frac{m}{V} \text{ (kg/m}^3\text{)} \quad \rightarrow \quad m = \rho V$$

Some Densities

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Air (20 ⁰ C and 1 atmosphere)	1.21
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Mercury (the metal)	13600
Earth (the planet, on average)	5500

$$= 1 \text{ g /cm}^3$$

What is the mass of a 2 L bottle of soda (assume $\rho_{\text{soda}} = \rho_{\text{water}}$)?

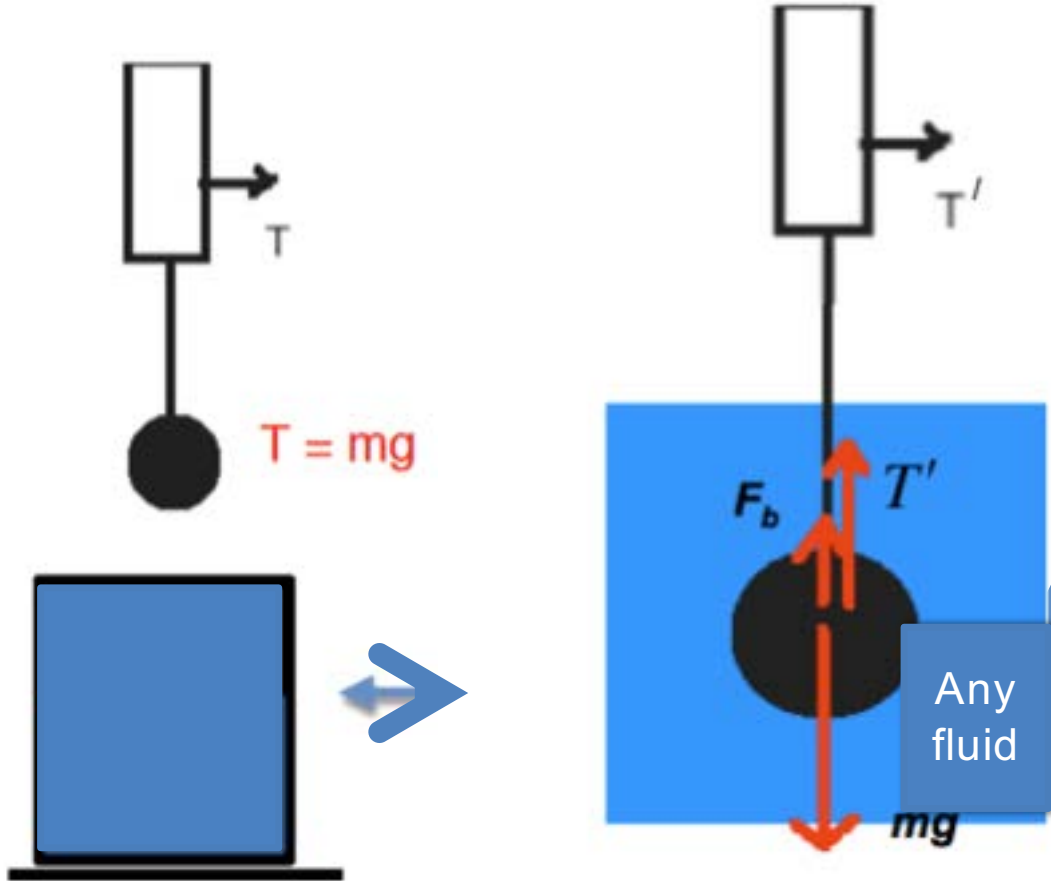
$$1 \text{ L} = 1000 \text{ cm}^3$$

$$2 \text{ L} = 2000 \text{ cm}^3 \rightarrow m_{\text{soda}} = 2000 \text{ cm}^3 \cdot 1 \frac{\text{g}}{\text{cm}^3} = 2000 \text{ g} = \underline{\underline{2 \text{ kg}}}$$

Buoyant force!

$$m = \rho V$$

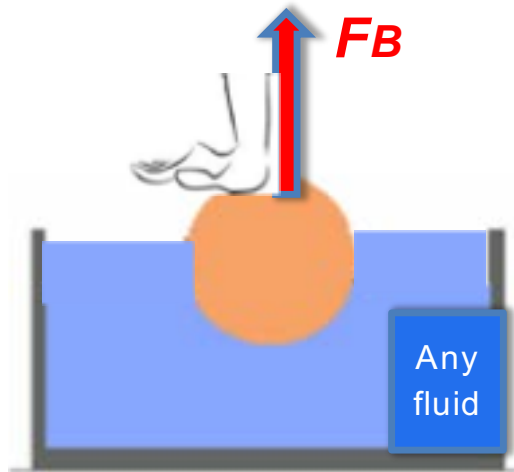
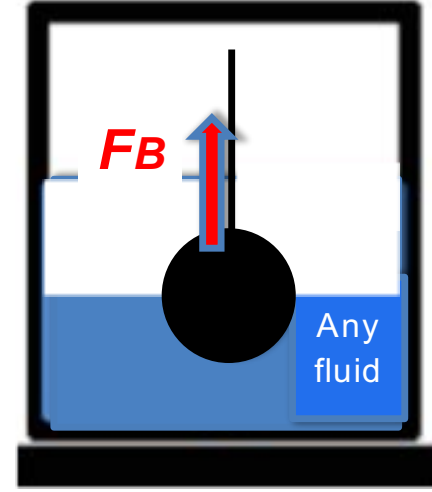
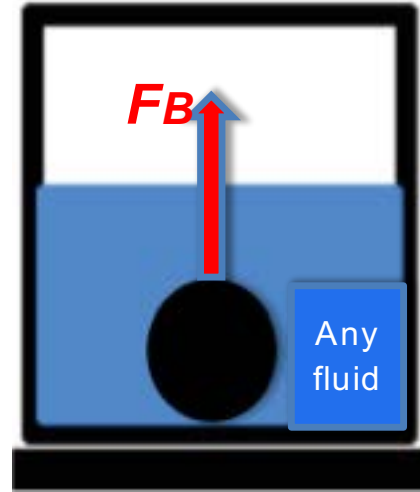
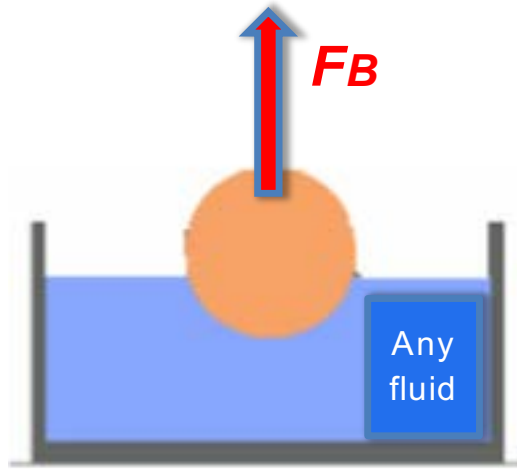
$$F_b = m_{\text{fluid displaced}} * g =$$
$$= \rho_{\text{fluid}} V_{\text{displaced}} * g$$



Not just water!

Buoyant force is one of many acting!

Other Forces Are Not Shown (your job!)



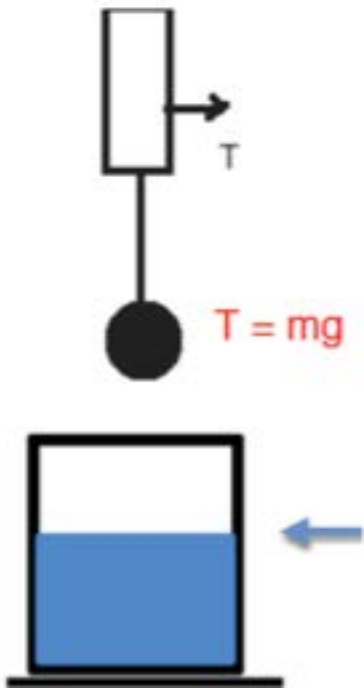
$$F_b = \rho_{fluid} V_{displaced} * g =$$
$$= \rho_{fluid} V_{of_the_object_in_the_fluid} * g$$

Webassign: L20 Q5

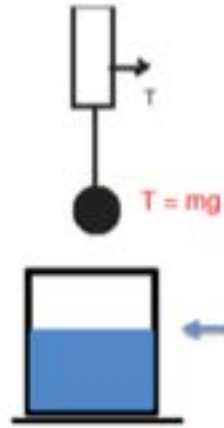
When a 3 kg ball is immersed in water its apparent weight W_A is 20 N. When the same 3 kg ball is immersed in mercury its apparent weight W_A is ...

1. 20 N
2. > 20 N
3. < 20 N
4. no way to say

Material (or object)	Density (kg/m^3)
Air (20 ⁰ C and 1 atmosphere)	1.21
Water (4 ⁰ C and 1 atmosphere)	1000
Iron	7900
Mercury (the metal)	13600
Earth (the planet, on average)	5500



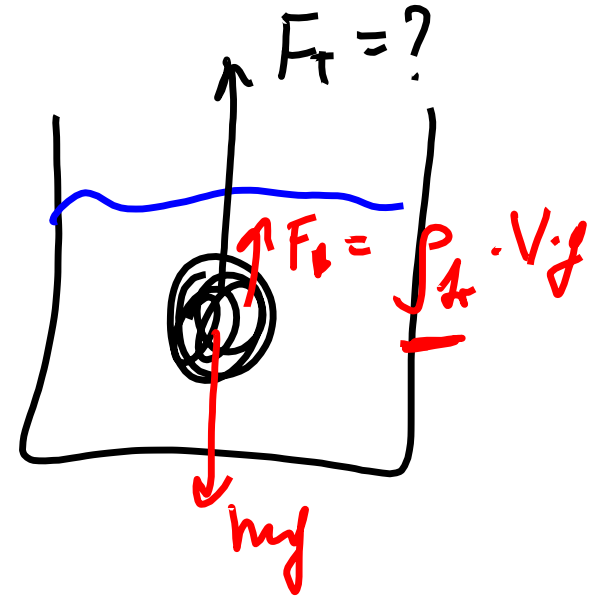
Webassign: L20 Q5



When a 3 kg ball is immersed in water its apparent weight W_A is 20 N. When the same 3 kg ball is immersed in mercury its apparent weight W_A is ...

1. 20 N
2. ~~> 20 N~~
3. < 20 N
4. no way to say

Material (or object)	Density (kg/m ³)
Air (20°C and 1 atmosphere)	1.21
Water (4°C and 1 atmosphere)	1000 ✓
Iron	7900
Mercury (the metal)	13600 ✓
Earth (the planet, on average)	5500



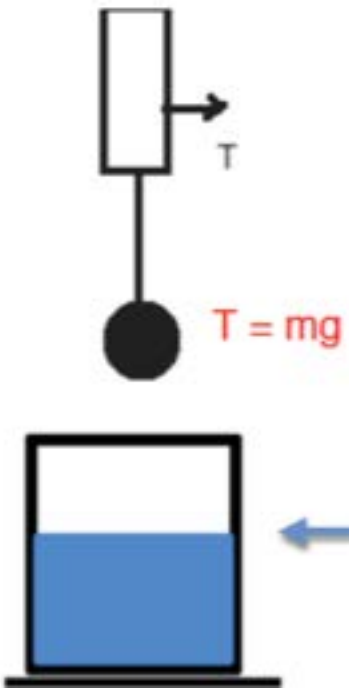
$$\rho \uparrow ; F_B \uparrow ; F_T = mg - F_B$$

Webassign: L20 Q5

When a 3 kg ball is immersed in water its apparent weight W_A is 20 N. When the same 3 kg ball is immersed in mercury its apparent weight W_A is ...

1. 20 N
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Density of the object v.

Density of the fluid

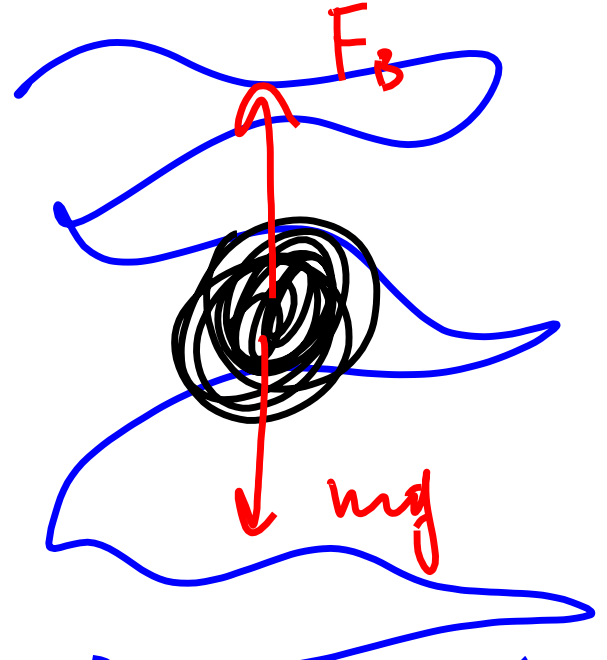
An object is immersed in a fluid and released.

Sinking ρ_o ρ_F

Floating
(in equilibrium) ρ_o ρ_F

Rising ρ_o ρ_F

F_B v. mg



~~$\rho_o \cdot V_{ob} \cdot g$~~ v. ~~$\rho \cdot V_{ob} \cdot g$~~

$\rho_o > \rho$

Density of the object ρ_o

Density of the fluid ρ_f

An object is immersed in a fluid and released.

Sinking $\rho_o > \rho_f$

Floating
(in equilibrium) $\rho_o = \rho_f$

Rising $\rho_o < \rho_f$

Correct set of symbols is ...

1. =, =, =

2. >, >, >

3. <, <, <

4. >, =, <

5. <, =, >

6. None of the above

A plastic cylinder is floating in *water*.

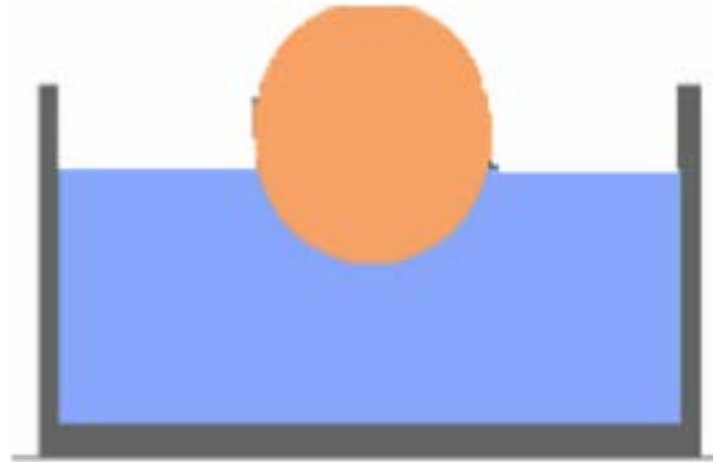
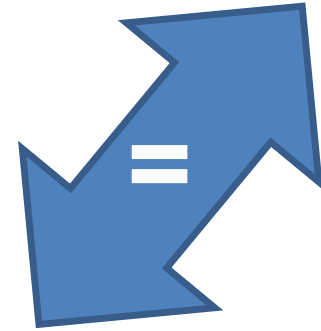


Measure the dimensions and find the mass of an object hidden in the cylinder, and also the *average* density of the cylinder.

Have we done in the past *anything* on FLOATING?

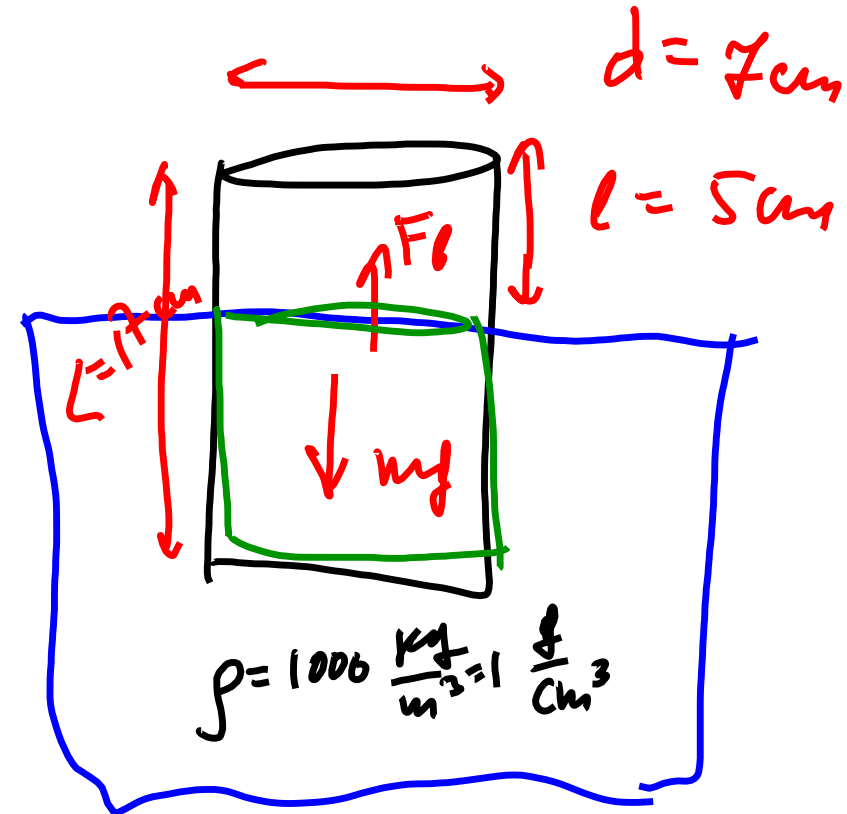


A plastic cylinder is floating in *water*. Measure the dimensions and find the mass of an object hidden in the cylinder, and also the *average* density of the cylinder.



A plastic cylinder is floating in water.

Measure the dimensions and find the mass of an object hidden in the cylinder, and also the *average* density of the cylinder.



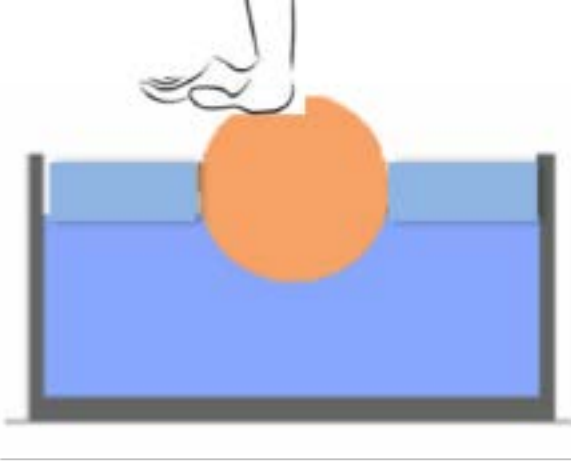
$$F_b = \rho_w \cdot V_{\text{displ}} \cdot g$$

$$mg = F_b = \rho_w \cdot V_{\text{obimm}} \cdot g$$

$$m = \rho_w \cdot V_{\text{obimm}} = 1 \frac{\text{g}}{\text{cm}^3} \cdot A \cdot H =$$

$$= 1 \cdot \pi \cdot r^2 \cdot (L - l) = \pi \cdot \left(\frac{7}{2}\right)^2 \cdot (17 - 5) =$$

$$= 461 \text{ g} \approx \underline{\underline{0.5 \text{ kg}}}$$



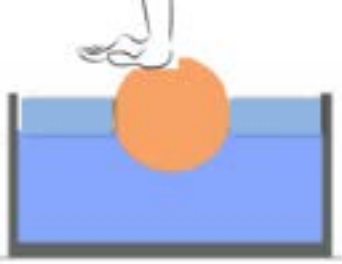
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The ball has a mass of 0.5 kg and a diameter of 22 cm (0.22 m).

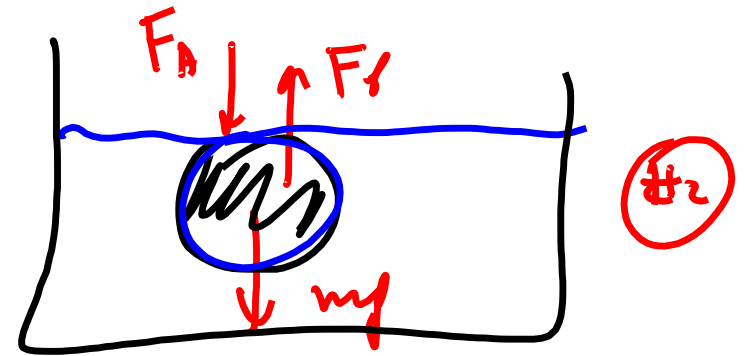
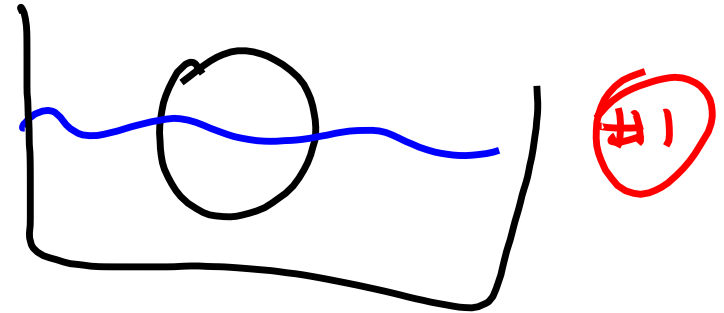
What *additional* force do we need to apply to the ball to completely submerge it into water? If instead of a force we would need to add a weight, what would be the mass of that weight?



A basketball floats in a bathtub of water.



The ball has a mass of 0.5 kg and a diameter of 22 cm (0.22 m).



What additional force do we need to apply to it to completely submerge it into water? If instead of a force we would need to add a weight, what would be the mass of that weight?

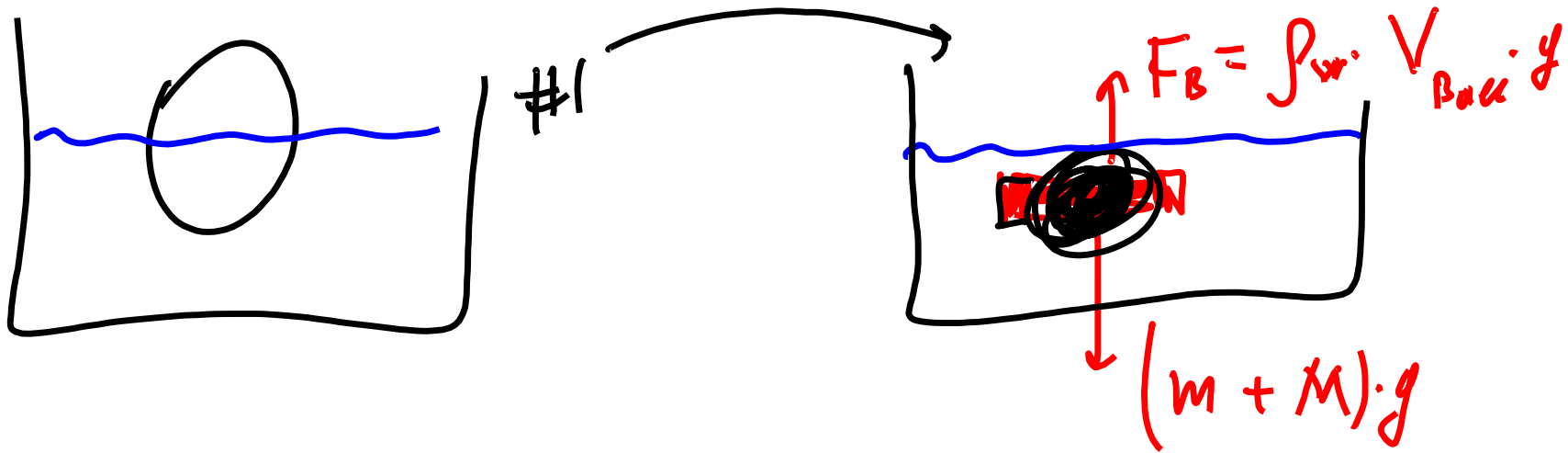
$$F_A + mg = F_R$$

$$F_A = F_R - mg = \rho_w \cdot V_{\text{tot}} \cdot g - m \cdot g =$$

$$= 1000 \cdot \frac{4}{3} \pi \cdot 0.11^3 \cdot 10 - 0.5 \cdot 10 = 50.75 \text{ N}$$

$$N; m_{\text{add}} \Rightarrow W = F_A$$
$$F_A = m_{\text{add}} \cdot g \Rightarrow m_{\text{add}} = \frac{F_A}{g}$$

$$m = 50.75/10 = 5 \text{ kg}$$



$$(m + M) g = \rho_{\text{water}} \cdot V_{\text{ball}} \cdot g$$

$$M = 1000 \cdot \frac{4}{3} \pi \cdot 0.11^3 - 0.5 = 5 \text{ kg}$$

A boat floats in a lake. When the anchor is taken from the boat and placed on the floor of the lake the level of the water in the lake ...

- 1. does not change**
- 2. Rises**
- 3. Lowers**



What will happen if *this element* will be removed?

1. It sinks
2. It floats
(in equilibrium)
3. It rises to the surface
4. We don't know



What will happen if *this element* will be removed?

1. It sinks
2. It floats
(in equilibrium)
3. It rises to the surface
4. **We don't know (may be a rod, may be a string)**



For the ball: $d = 10 \text{ cm}$ $\rho_{ball} = 0.8 \frac{\text{g}}{\text{cm}^3}$

Find the apparent weight of the ball in water.

**If the ball was held by a spring with $k = 10 \text{ N/m}$,
What would be the elongation (the stretch) of the string?**





$$d = 10 \text{ cm} \quad \rho_{ball} = 0.8 \frac{\text{g}}{\text{cm}^3} ; \quad \left| \frac{\text{g}}{\text{cm}^3} = 1000 \frac{\text{kg}}{\text{m}^3} \right.$$

Find the apparent weight of the ball in water.

$$\rho_w = 0.8 \frac{\text{g}}{\text{cm}^3} = 0.8 \cdot 1000 \frac{\text{kg}}{\text{m}^3} = 800 \frac{\text{kg}}{\text{m}^3}$$

If the ball was held by a spring with $k = 10 \text{ N/m}$,
What would be the elongation (the stretch) of the string?

$$mg + F_T = F_B$$

$$F_T = F_B - mg = \rho_w \cdot V \cdot g - \rho_B \cdot V \cdot g = (\rho_w - \rho_B) \cdot V \cdot g =$$

$$= \underline{(1 - 0.8) \cdot \frac{4}{3} \pi \cdot \left(\frac{10}{2}\right)^3 \cdot 10} \frac{\text{kg} \cdot \text{m}}{\text{s}^2}$$

$$F_T = |F_{el}| = k \cdot |\Delta x| ;$$

$$F_T = k \cdot \Delta x ; \quad \Delta x = \frac{|F_T|}{k} = \dots$$

$$mg + F_T = F_B$$

$$F_T = F_B - mg = \rho_w \cdot V \cdot g - \rho_B \cdot V \cdot g = (\rho_w - \rho_B) \cdot V \cdot g =$$

$$F_T = |F_{el}| = k \cdot |\Delta x|;$$

$$F_T = k \cdot \Delta x; \quad \Delta x = \frac{|F_T|}{k} = \dots$$

$$F_T = (1 - .8) \cdot (4/3) \cdot \text{Pi} \cdot (5)^3 \cdot 10 = 1047 \text{ g} \cdot \text{m/s}^2 = 1.05 \text{ N}$$

Or, using SI system

$$F_T = (1000 - 800) \cdot (4/3) \cdot \text{Pi} \cdot (0.05)^3 \cdot 10 = 1.05 \text{ N}$$

**A general strategy for solving problems on
buoyant force.**



**Is essentially the same as a general strategy
for solving problems on ANY force!**

- 1. Draw a picture, convert it into FBD.**
- 2. Set FBE (N2L for Equilibrium)**
- 3. If necessary, add additional relationships
(think what variables are connected: F_B , m , g , ρ ,
 V , etc. – depending on forces and geometry)**
- 4. Solve**

Done with buoyant force!

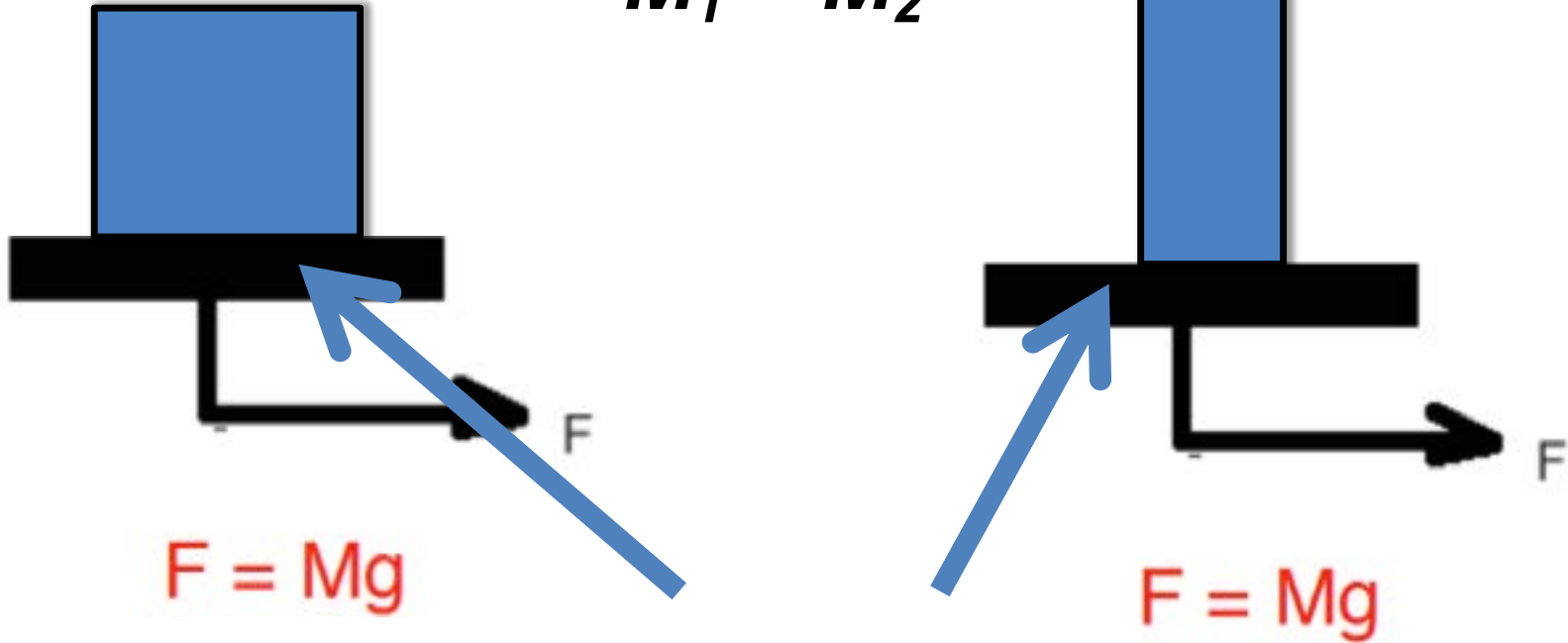
A general strategy for solving problems on buoyant force.



- 1. Draw a picture, convert it into FBD.**
- 2. Set FBE (N2L for Equilibrium)**
- 3. If necessary, add additional relationships (think what variables are connected: F_B , m , g , ρ , V , etc. – depending on forces and geometry)**
- 4. Solve**

A wide beaker vs. a tall beaker

$$M_1 = M_2$$



“Force distribution”

Dose it matter?

“force distribution” = Pressure



Snowshoes make difference!

Pressure

$$P = \frac{F}{A} = \frac{F_{1m^2}}{1m^2}$$

The SI unit is Pa

= “FROCE DISTRIOBUTION OVER AREA”

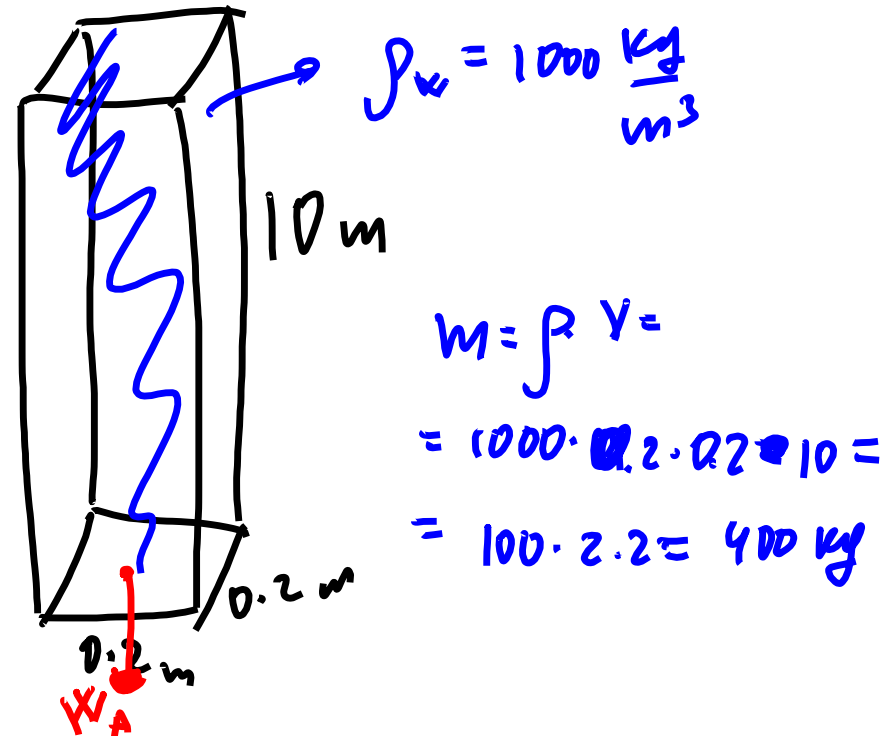
The SI unit Pa = N/m²

A 10 m tall rectangular plastic column with the base of 20 cm by 20 cm is filled with water. Calculate the weight of the water in the column.

Weight of water $W = \dots$

1. 1000 N
2. 2000 N
3. 3000 N

etc.



A 10 m tall rectangular column with the base of 20 cm by 20 cm is filled with water. How much pressure does the water exert on the bottom of the column?

$$W = 400 * 10 =$$

1. 1000 N
2. 2000 N
3. 3000 N
4. 4000 N

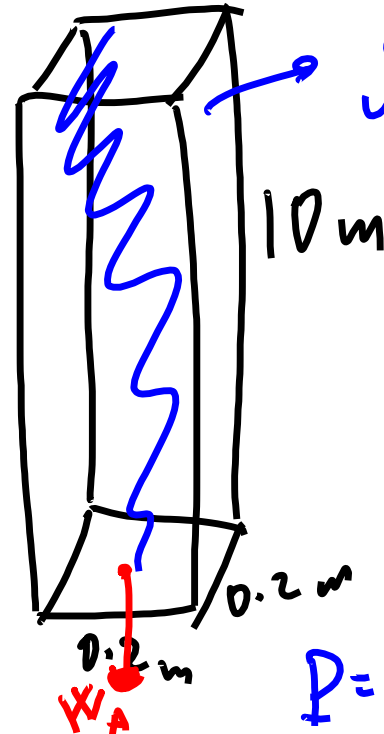
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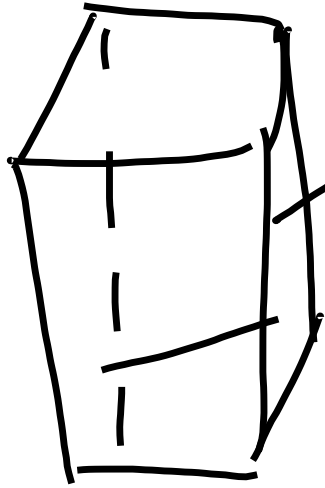
$$P = \frac{400 \cdot 10}{.2 \cdot .2} = 100000 \text{ Pa}$$



$$\rho_w = 1000 \frac{\text{kg}}{\text{m}^3}$$

$$\begin{aligned} m &= \rho \cdot V = \\ &= 1000 \cdot .2 \cdot .2 \cdot 10 = \\ &= 100 \cdot 2 \cdot 2 = 400 \text{ kg} \end{aligned}$$

$$P = \frac{400 \cdot 10}{.2 \cdot .2} = 100000 \text{ Pa}$$



$$V = A \cdot H$$

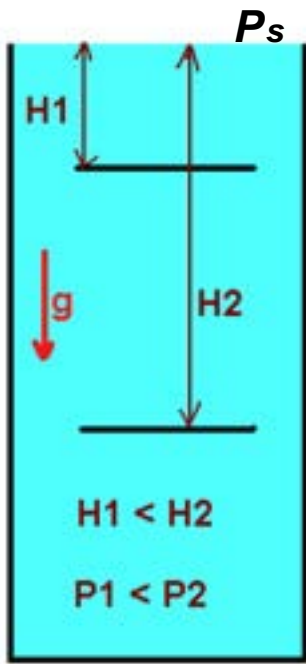
$$m = \rho V = \rho A \cdot H$$

$$W = m \cdot g = \rho A \cdot H \cdot g$$

$$P = \frac{W}{A} = \frac{\rho A \cdot H \cdot g}{A} = \underline{\underline{\rho \cdot H \cdot g}}$$

Pressure in a medium

Static fluid!



The lower the level is (deeper in fluid), the more is the pressure provided by the fluid.

“The pressure at the bottom...”

The reason is the force of gravity acting on the liquid.

The top plate has less fluid above it then the bottom plate!

$$m = \rho V$$

$$V = Ah$$

The amount of the fluid acting on the bottom plate.

The amount of the fluid acting on the top plate.

$$P = \frac{F_{mg}}{A}$$

$$P = \frac{mg}{A} = \frac{\rho Vg}{A}$$

$$P = \frac{\rho Ahg}{A} = \rho gh$$



Which one?

or

$$P_{total} = P_{surface} + P_{gauge}$$

Gauge pressure