



**Good morning!**

**Lab 9 is in B9**

**If you are here, please pick up YOUR exam!!**

*to prove your presence!*

**Please, login into webassing, locate  
LectureMCQ\_L23 (PY105)  
and answer question 1  
(but ONLY Q1!).**



## current topics (do not read this slide)

Temperature, temperature scales, thermal contact, thermal conduction, thermal equilibrium, measuring temperature, heat, internal energy, meaning of temperature, meaning of heat, thermal expansion, coefficient of thermal expansion (CTE), linear, areal, and volumetric CTE, heat capacity, specific heat (capacity), thermally insulated system, heat balance equation (an equation for thermal equilibrium), phase transition, critical temperature, latent heat (capacity), method for solving thermal equilibrium problems, convection, thermal radiation, thermal conduction, thermal conductivity, the ideal gas, absolute temperature, a mole, the Avogadro's number, the universal gas constant, RMS values, the ideal gas law, iso – laws, graphs for gas processes (PV, VT, PT diagrams), the Boltzmann's constant, the meaning of the absolute temperature, the meaning of the pressure, degree of freedom, the equipartition theorem, monatomic, diatomic, polyatomic gas, calculating internal energy, the first law of thermodynamics, work done by gas, calculating specific heat ( $C_v$ ,  $C_p$ ), isothermal process, adiabatic process, thermodynamic cycle, work done over a cycle, heat engine, entropy, second law of thermodynamics, heat engine efficiency, the Carnot cycle, maximum (ideal) heat engine efficiency, a heat pump and a refrigerator (***the last topic of test 3***)

$$c_w = 4000 \text{ J/(kg } ^\circ\text{C)}; c_{\text{ice}} = 2000 \text{ J/(kg } ^\circ\text{C)}; \quad Q = \pm Lm$$

$$L_f = 3 \times 10^5 \text{ J/kg}$$

$$Q = cm(T_f - T_i)$$

**You need to make 20 ice cubes (5 g each) at  $-5^\circ\text{C}$ . You pour  $25^\circ\text{C}$  water into an ice tray and place it in a freezer. How much heat should water ....?**

**Webassign: L23 Q2**

**1. Absorb**

**2. Release**



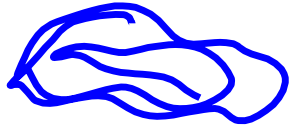
$$c_w = 4000 \text{ J/(kg } ^\circ\text{C)}; c_{\text{ice}} = 2000 \text{ J/(kg } ^\circ\text{C)}; L_f = 3 \times 10^5 \text{ J/kg}$$

You need to make 20 ice cubes (5 g each) at  $-5^\circ\text{C}$ . You pour  $25^\circ\text{C}$  water into an ice tray and place it in a freezer. How much heat should water ... ?

Webassign: L23 Q2

1. Absorb

2. Release



$$T_w = 25^\circ\text{C}$$

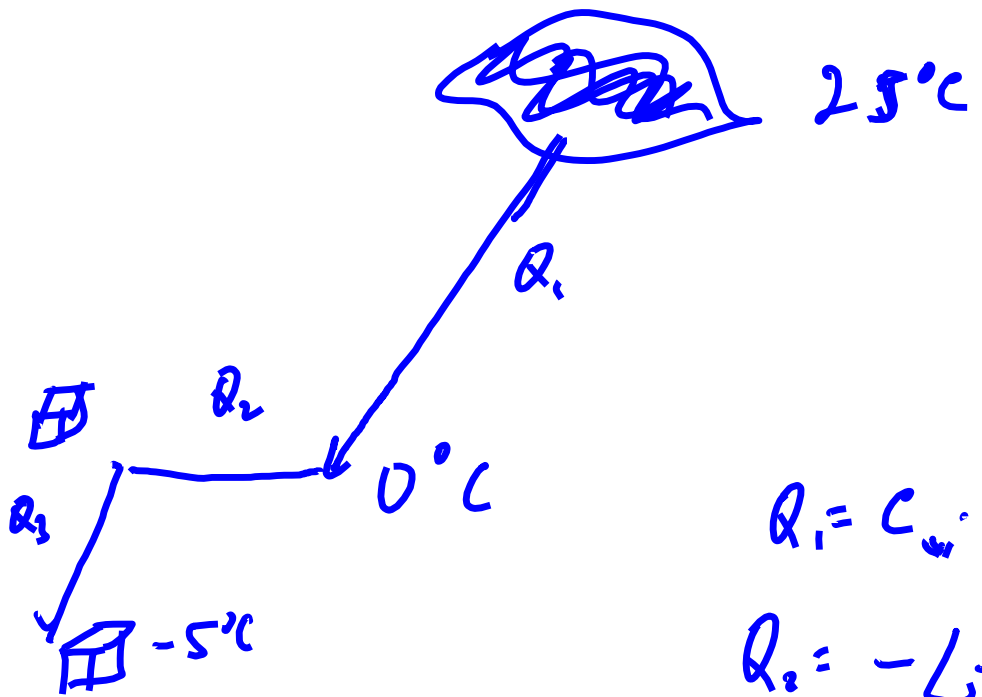


$$T_{\text{ice}} = -5^\circ\text{C}$$

$$Q = c \cdot m \cdot \Delta T$$

$$Q = 4000 \cdot 20 \cdot 0.005 \cdot (-5 - 25) \rightarrow \text{done}$$

~~WRONGS!~~



1. objects
2. processes  $\rightarrow \Delta T$   
 $\rightarrow T = \text{const}$
3.  $Q = \dots$

$$Q_1 = c_w \cdot m \cdot (0 - 25) = -4000 \cdot 20 \cdot 0.005 \cdot 25 \text{ J}$$

$$\underline{Q_2 = -L \cdot m = -300000 \cdot 20 \cdot 0.005 \text{ J}}$$

$$Q_3 = c_i \cdot m \cdot (-5 - 0) = -2000 \cdot 20 \cdot 0.005 \cdot 5 \text{ J}$$

$$Q = Q_1 + Q_2 + Q_3$$

$$Q = - \underline{4000} \cdot 20 \cdot \underline{0.005} \cdot 25 - 300 \underline{000} \cdot 20 \cdot \underline{0.005} -$$

$$- \underline{200} \cdot 20 \cdot \underline{0.005} \cdot 5 = -4,205.25 - 300 \cdot 20 \cdot 5 -$$

$$- 2 \cdot 2 \cdot 5 \cdot 5 = -100 \cdot 100 - 300 \cdot 100 - 4.25 =$$

$$= -10000 - 30000 - 100 = -40100 \text{ J}$$

**A solid object is placed into a liquid (poured into a container).**

**The liquid has its initial tempera-**

**ture of  $500^{\circ}\text{C}$ ; the solid is initially twice warmer.**

**The solid has the mass of a third of the mass of**

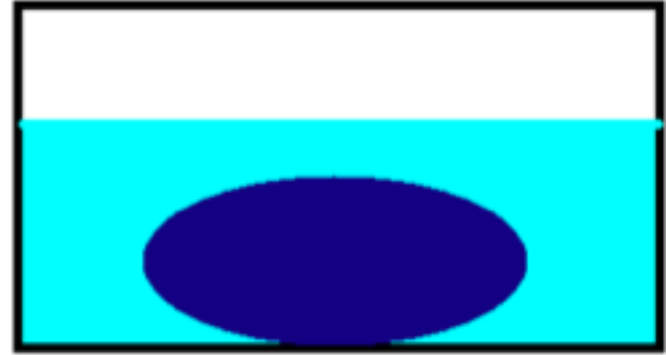
**the liquid, but its specific heat is twice of the**

**specific heat of the liquid. The container has**

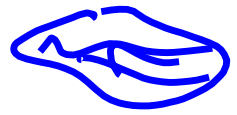
**the mass of the quarter of the solid and its**

**specific heat is equal to one half of the liquid's.**

**Find the final temperature of the system.**



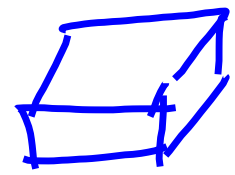
A solid object is placed into a liquid (poured into a container). The liquid has its initial temperature of  $500^{\circ}\text{C}$ ; the solid is initially twice warmer. The solid has the mass of a third of the mass of the liquid, but its specific heat is twice of the specific heat of the liquid. The container has the mass of the quarter of the solid and its specific heat is equal to one half of the liquid's. Find the final temperature of the system.



$$t_{iL} = 500^{\circ}\text{C}$$

$$m_L$$

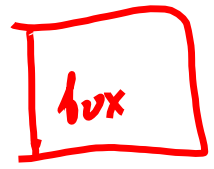
$$c_L$$



$$t_{iS} = 1000^{\circ}\text{C}$$

$$m_S = \frac{1}{3} m_L$$

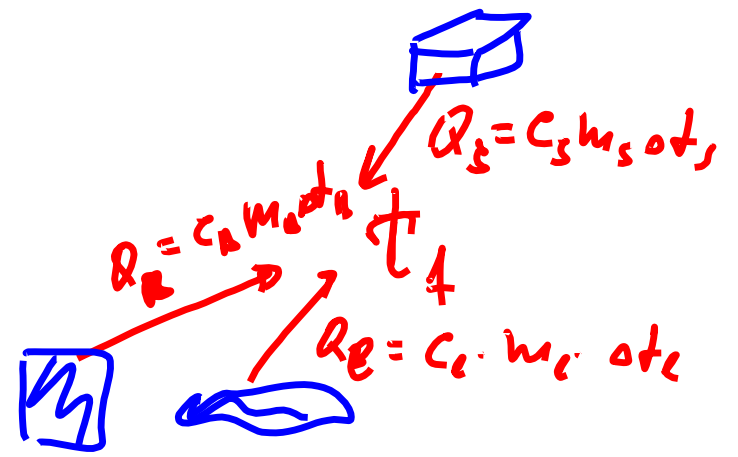
$$c_S = 2 \cdot c_L$$



$$m_B = \frac{1}{4} m_S$$

$$c_B = \frac{1}{2} c_L$$

$$t_{iB} = 500^{\circ}\text{C}$$



$$Q_1 + Q_2 + Q_3 = 0$$



$$Q_s + Q_e + Q_B = 0$$

$$C_s m_s \Delta t_s + C_e m_e \Delta t_e + C_B m_B \Delta t_B = 0$$

$$p = 2 \cdot \cancel{C_e} \cdot \cancel{\frac{1}{3}} \cdot \cancel{m_e} \cdot (t_f - 1000) + \cancel{C_e} \cdot \cancel{m_e} \cdot (t_f - 500) + \frac{1}{2} \cancel{C_e} \cdot \frac{1}{4} \cdot \frac{1}{3} \cdot \cancel{m_e} \cdot (t_f - 500)$$

$$p = \frac{2}{3} \cdot (t_f - 1000) + t_f - 500 + \frac{1}{24} \cdot (t_f - 500)$$

↳ solve for  $t_f$

$$0 = \frac{2}{3} t_f - \frac{2}{3} \cdot 1000 + t_f - 500 + \frac{1}{24} \cdot t_f - \frac{1}{24} \cdot 500 \quad | \times 24$$

$$0 = 2 \cdot 8 \cdot t_f - 2 \cdot 8 \cdot 1000 + 24 \cdot t_f - 24 \cdot 500 + t_f - 500$$

$$16000 + 12000 + 500 = (16 + 24 + 1) t_f$$

$$28500 = 41 \cdot t_f$$

$$t_f = \frac{28500}{41} = 695^\circ\text{C}$$

## Last topics (do not read this slide)

The ideal gas, absolute temperature, a mole, the Avogadro's number, the universal gas constant, RMS values, the ideal gas law, iso – laws, graphs for gas processes (PV, VT, PT diagrams), the Boltzmann's constant, the meaning of the absolute temperature, the meaning of the pressure, degree of freedom, the equipartition theorem, monatomic, diatomic, polyatomic gas, calculating internal energy, the first law of thermodynamics, work done by gas, calculating specific heat ( $C_v$ ,  $C_p$ ), isothermal process, adiabatic process, thermodynamic cycle, work done over a cycle, heat engine, entropy, second law of thermodynamics, heat engine efficiency, the Carnot cycle, maximum (ideal) heat engine efficiency, a heat pump and a refrigerator (***the last topic of test 3***)

## Structure of Matter

As we know now, all objects around us (solid or fluid) are made of a huge amount of tiny and very light particles (atoms and molecules).

For example, an oxygen atom has the weight of  
 $m_0 = 2.66 * 10^{-26}$  kg

 The mass of an atom or a molecule

If we take  $m = 1$  gram of oxygen, the total number  $N$  of atoms in it is

$$N = m/m_0 = 3.76 * 10^{22}$$

## Avogadro's Number

An amount of a matter having  $6.02 \times 10^{23}$  particles is named a **MOLE**

A mole is very similar to a dozen, in the sense that it stands for a certain number of things.

A dozen means 12, while a mole means  $6.02 \times 10^{23}$ .

This number is also known as *Avogadro's number*,  $N_A$ .

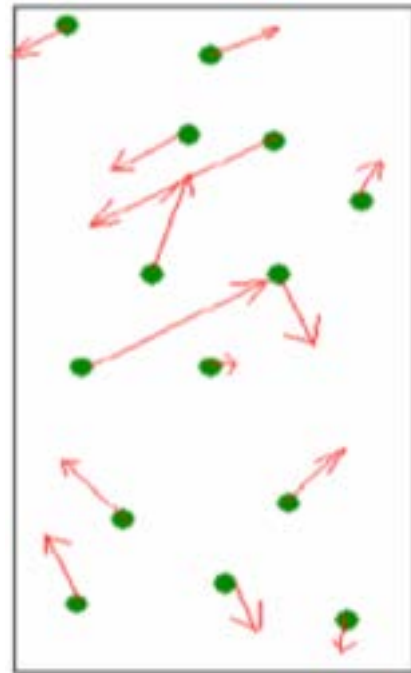
$$N_A = 6.02 \times 10^{23}$$

**1 mole =  $N_A$  particles**

Every material has the same number of particles in 1 mole, but the mass of 1 mole is different to different materials.

*A molar mass  $\mu = m_0 N_A$  is the mass of 1 mole of the substance.*

(note: Use  $\mu$  or  $M$ )



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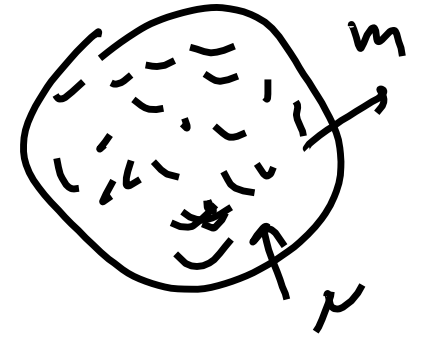
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$$M = \mu = m_0 N_A$$

$m_0$  = the mass of an atom or a molecule

**# of moles**

$$n = \frac{N}{N_A} = ??$$



$$n = \frac{N \cdot m_0}{N_A \cdot m_0} = \frac{M}{M}$$

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# of moles

Mass of the gas

$$n = \frac{N}{N_A} = \frac{m_0 N}{m_0 N_A} = \frac{m}{M} = \frac{m}{\mu}$$

Molar mass

(note: Use  $\mu$  or  $M$ )

Webassign: L23 Q3

gram/mol

Molar mass of  $H_2 =$

1. 1 kg/mol
2. 2 kg/mol
3. 3 kg/mol
- ...
9. None of the above

For elements with no stable isotopes, the mass number of the isotope with the longest half-life is in parentheses.

Periodic Table Image & Worksheet Copyright © 2007 Michael Davis, Thomson Learning, Inc. All Rights Reserved. Updated Apr 13, 2014

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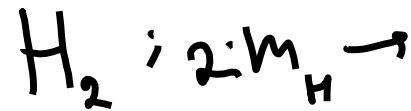
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$$M_{H_2} = 2 \frac{g}{mol} = 0.002 \frac{kg}{mol}$$

# of moles

Mass of the gas

$$n = \frac{N}{N_A} = \frac{m_0 N}{m_0 N_A} = \frac{m}{M} = \frac{m}{\mu}$$

Molar mass

(note: Use  $\mu$  or  $M$ )

gram/mol

Webassign: L23 Q3

Molar mass of  $H_2 =$

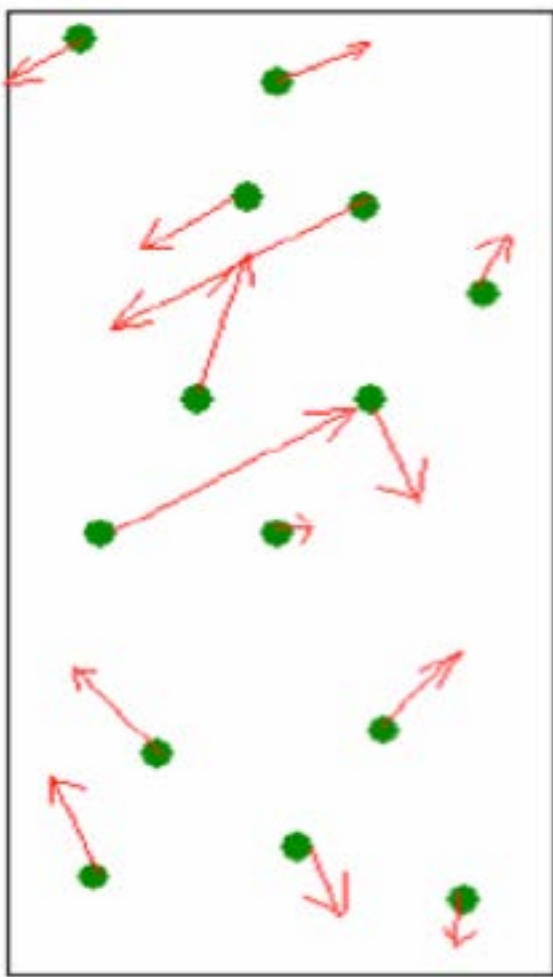
1. 1 kg/mol
2. 2 kg/mol
3. 3 kg/mol
- ...
9. None of the above



## The Ideal Gas Law

An ideal gas satisfies these conditions:

1. It consists of **a large** number of identical particles (atoms, molecules).
2. The volume occupied by the particles themselves is negligible compared to the volume of the container they're in (**particles are dots or made of dots**).
3. The particles move in **random** motion.
4. The particles obey Newton's laws of motion; they experience forces only during collisions; any collisions are completely elastic, and instantaneous (take a negligible amount of time).



$T > 0$

What is the average velocity of the ideal gas particles (for  $T > 0$ )?

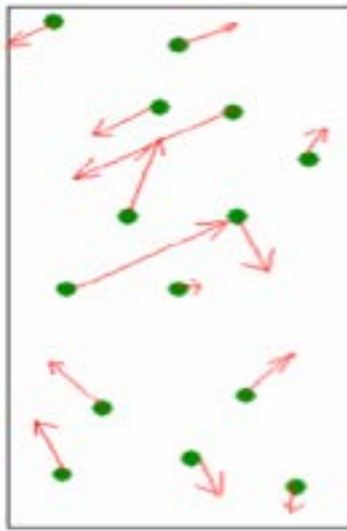
$$\frac{1}{N} \sum \vec{v} = ?$$

Webassign: L23 Q4

- 1) It depends on the temperature of the gas.
- 2) Zero.
- 3) It points to the right.
- 4) It is immeasurable.

What is the average velocity of the ideal gas particles (for  $T > 0$ )?

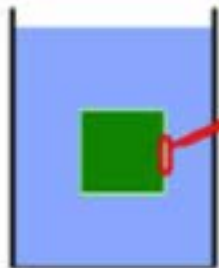
$$\frac{1}{N} \sum \vec{v} = ?$$



Webassign: L23 Q4

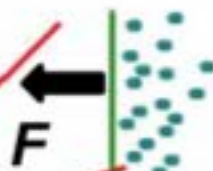
- 1) It depends on the temperature of the gas.
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- 4) It is immeasurable.

The nature of pressure.



Molecules are hitting a wall!

$$\vec{F} \Delta t = m \vec{v}_2 - m \vec{v}_1$$



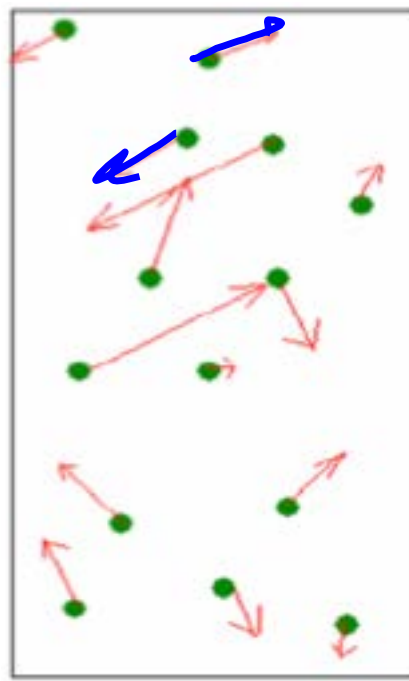
To describe the force acting from the fluid on the object the physical quantity PRESSURE is used.

Pressure



Webassign: L23 Q4

What is the average velocity of the ideal gas particles (for  $T > 0$ )?



- 1) It depends on the temperature of the gas.
- 2) Zero.
- 3) It points to the right.
- 4) It is immeasurable.

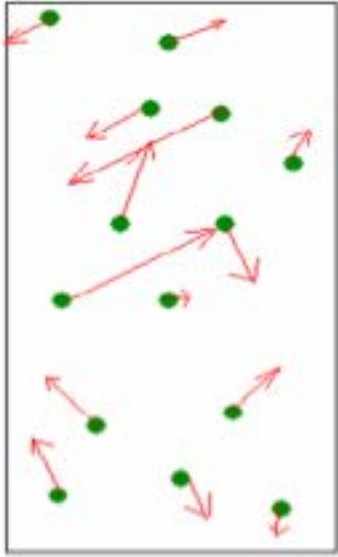
$$\frac{1}{N} \sum \vec{v} = ?$$

**The average translational Kinetic Energy ( $T > 0$ )**

$$KE_{tr\_ave} = \frac{\frac{mv_1^2}{2} + \frac{mv_2^2}{2} + \frac{mv_3^2}{2} + \dots + \frac{mv_N^2}{2}}{N} > 0$$

**Always positive!**

What is the average velocity of the ideal gas particles?



$$\underline{T > 0}$$

2) Zero.

For the huge number of particles  $\frac{1}{N} \sum \vec{v} = 0$

The average velocity is zero, because, on average, the velocity of particles going in one direction is cancelled by the velocity of particles going in the opposite direction.

**Vector addition - when all vectors point in all possible directions!**

# Ideal Gas Equations

The definition of absolute Temperature

Kinetic Theory of Ideal Gas

$E_{\text{tr K-AVE}}$  is Av Tr KE of  $N$  particles

$$\vec{F}\Delta t = m\vec{v}_2 - m\vec{v}_1$$

$$E_{\text{tr K-AVE}} = \frac{3}{2}kT$$

$$T = t + 273.15$$

$$PV = \frac{2N}{3}E_{\text{tr K-AVE}}$$

$k$  – Boltzmann constant

$$k = 1.38 \cdot 10^{-23} \text{ J/K}$$

*the ideal gas law*

$$PV = NkT$$

**The Ideal Gas Law**

$$PV = nRT$$

$$R = 8.31 \text{ J/(mol K)}$$

For curious people

$$PV = NkT$$

It is convenient to rewrite the law:

$$n = \frac{N}{N_A}$$

$N = n * N_A$ ,  $n$  is the number of moles:  $PV = nN_AkT$

Let's define  $N_Ak = R$ , the universal gas constant:

$$R = 8.31 \text{ J}/(\text{mol K})$$

$$PV = nRT$$

The Ideal Gas Law

The number of moles

## The Ideal Gas Law

$$\frac{PV}{RT} = \frac{nRT}{RT}$$

$$\frac{PV}{nT} = ???$$

$$\frac{PV}{RT} = n; \quad \frac{PV}{nT} = \underline{\underline{R = \text{const}}}$$

Webassign: L23 Q5

$$\frac{PV}{T} = \dots$$

1. Always constant
2. Sometimes constant
3. Always change
4. None of the above



## The Ideal Gas Law

$$PV = nRT$$

$$n = \nu = \frac{N}{N_A} = \frac{m}{M}$$

Webassign: L23 Q5

$$\frac{PV}{T} = \dots$$

1. Always constant
2. Sometimes constant
3. Always change
4. None of the above



$$\frac{PV}{nT} = R = 8.31 \text{ J/(mol K)}$$

Always constant

$$R = 8.31 \text{ J/(mol K)}$$

$$\frac{PV}{nT} = n \cdot R$$

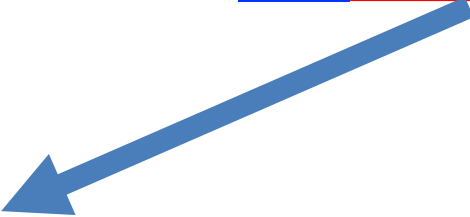
amount of gas

↓  
May change

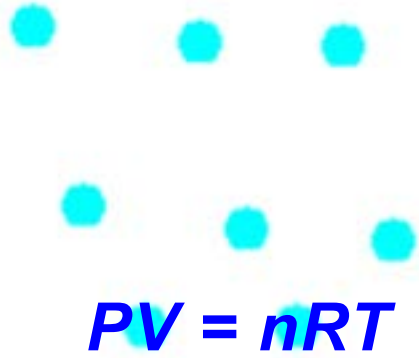
$$PV = nRT$$

$$\frac{PV}{T} = nR$$

2. Sometimes constant



When the amount of gas does *NOT* change  $\Rightarrow n = \text{const} \Rightarrow PV/T = \text{const}$

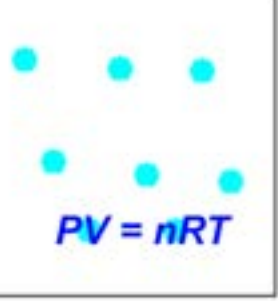


**An ideal gas is in a container at the temperature of  $127^{\circ}\text{C}$ .**

**Find the new temperature if the volume of the container was tripled, the pressure was**

**decreased to the half of the initial, and a quarter of the gas was lost to the environment.**





An ideal gas is in a container at the temperature of  $127^{\circ}\text{C}$ . Find the new temperature if the volume of the container was tripled, the pressure was

decreased to the half of the initial, and a quarter of the gas was lost to the environment.

$t_i = 127^{\circ}\text{C}$   
 $t_f = ?$

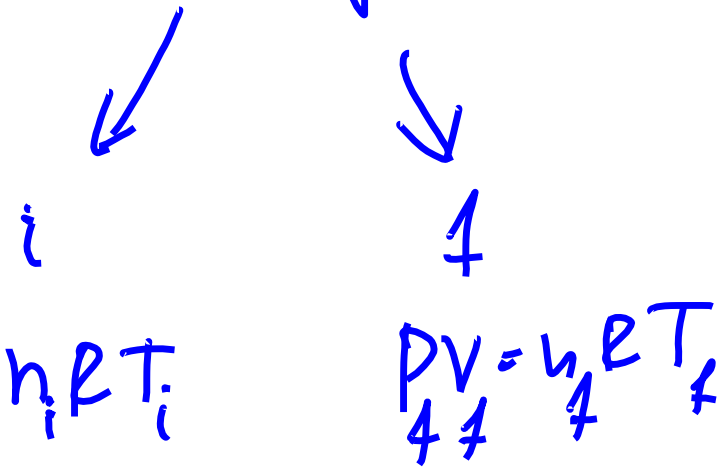
$$\frac{P_i V_i}{P_f V_f} = \frac{n_i R T_i}{n_f R T_f} \Rightarrow$$

$V_f = 3 \cdot V_i$   
 $P_f = \frac{1}{2} P_i$   
 $\frac{\frac{1}{2} P_i \cdot 3 \cdot V_i}{P_i V_i} = \frac{n_i R T_i}{\frac{3}{4} n_i R T_f}$

~~$n_f = \frac{1}{4} n_i$~~

$n_f = n_i - \frac{1}{4} n_i = \frac{3}{4} n_i$   
 $\frac{\frac{1}{2}}{3} = \frac{\frac{3}{4} T_i}{T_f}$   
 $T_f = 2 \cdot T_i$

Change!



$$T_4 = 2 \cdot T_i = 2 \cdot 127 = 254$$

↓  
K

↓  
K;

W/R only

$$T_i = 127 + 273 = 400\text{K}$$

$$T_4 = 2 \cdot 400 = 800\text{K}$$

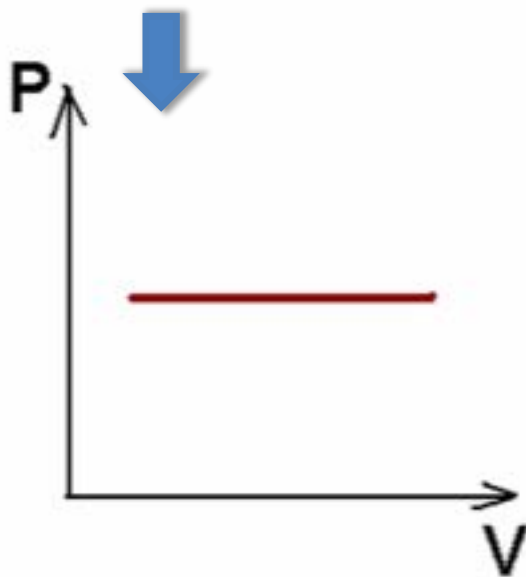
$$t_4 = 800 - 273 = 527^\circ\text{C}$$

## Three standard processes ( $n = \text{const}$ ):

Isobaric

$$P = \text{const}$$

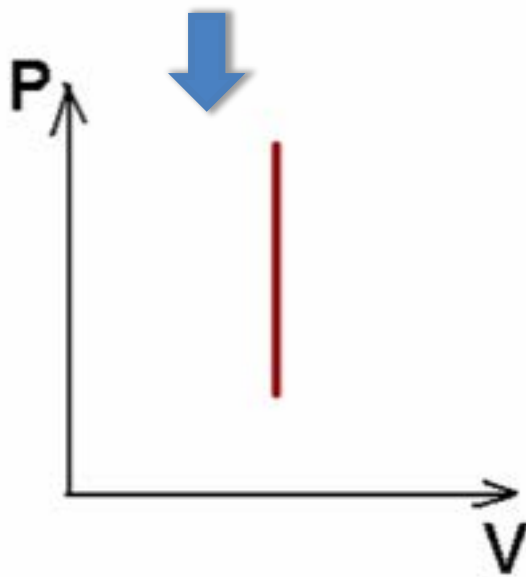
$$V/T = \text{const}$$



Isochoric

$$V = \text{const}$$

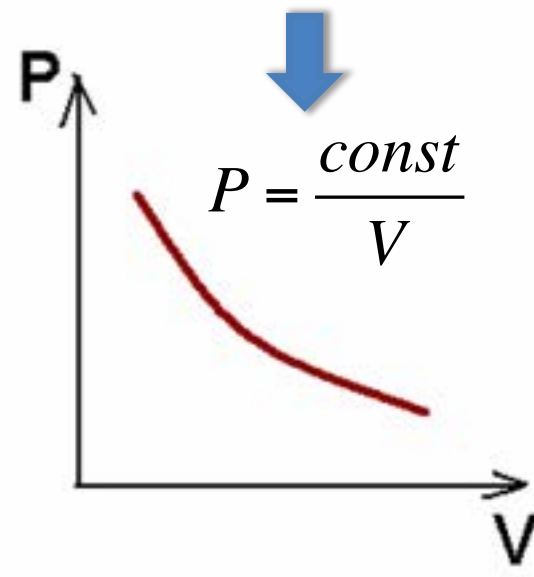
$$P/T = \text{const}$$



Isothermal

$$T = \text{const}$$

$$PV = \text{const}$$



$$n = m/M$$

$$n = \text{const}$$

$$\frac{PV}{Tn} = R = 8.31 \text{ J/(K mole)}$$

(Try to plot graphs for the same processes using PT and VT axes)

## Monatomic ideal gas •

For an atom:  $KE = Tr\_KE$



Each particle is a *dot*. •

Only translational kinetic energy does exist, hence the internal energy is equal to just total average kinetic energy of all the particles, therefore:

$$KE_{tr\_ave} = \frac{3}{2}kT$$

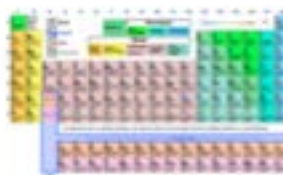
Monatomic ideal gas:  $E_{int} = E_{K-AVE}N = \frac{3}{2}NkT = 3 * \frac{1}{2}NkT$

**An internal energy of the gas:  $U = E_{int} = E_{KE\_ave} * N$**

*Each direction (x, y, and z – 3 directions!) contributes  $\frac{1}{2}NkT$  to the energy.*

Monatomic ideal gas •

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Monatomic ideal gas:  $E_{int} = E_{KE\_AVE} N = \frac{3}{2} NkT = 3 * \frac{1}{2} NkT$



An internal energy of the gas:  $U = E_{int} = E_{KE\_ave} * N$

Each direction (x, y, and z – 3 directions!) contributes  $\frac{1}{2} NkT$  to the energy.

$$P V = \boxed{NkT} \Rightarrow P V = \boxed{nRT}$$

$$U = N \cdot E_{TrKE} = N \cdot \frac{3}{2} k T =$$

$$= \frac{3}{2} \underline{k N T} = \underline{\frac{3}{2} n R T}$$

$$\underline{U} = \underline{\frac{3}{2} n R T} = \underline{\frac{3}{2} P V}$$



$E_{tr \text{ K-AVE}}$  is Av Tr KE of CofM of gas particles.

$$E_{tr \text{ K-AVE}} = \frac{3}{2}kT$$

This is a definition of the absolute temperature

$k$  – Boltzmann constant;

$$k = 1.38 \cdot 10^{-23} \text{ J/K}$$

For an atom:  $KE = Tr\_KE$

Energy of a GAS made of  $N$  atoms.


$$U = N \cdot E_{K-AVE} = N \frac{3}{2}kT = nN_A \frac{3}{2}kT = \frac{3}{2}nN_A kT = \frac{3}{2}nRT$$

$$U = \frac{3}{2}nRT$$



Internal energy  
for a monatomic gas


## For a molecule: $KE = Tr\_KE + Rot\_KE$

For a *diatomic* (two atoms make one molecule) molecule there are *three translation directions*, and *rotational kinetic energy also contributes*, but *only* for rotations about two of the three perpendicular axes. The *five* contributions to the energy (five degrees of freedom) give: 

( we ignore possible oscillations)

$$\text{Diatomic ideal gas: } E_{\text{int}} = \frac{5}{2}NkT = U = \frac{5}{2}nRT$$


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*Polyatomic gas:*   $U = E_{\text{int}} = \frac{6}{2}NkT = \frac{6}{2}nRT$

$i$  (the number of degrees of freedom) depends on the type of the particles:

$i = 3$  • for point-like particles

$i = 5$  —• for dumbbell-like particles (no oscillations)

$i = 6$   for big particles made of 3 or more atoms (no oscillations)

Ideal gas: 
$$U = E_{\text{int}} = \frac{i}{2} \frac{N}{N_A} N_A kT = \frac{i}{2} nRT = \frac{i}{2} PV$$

**In General:** →

Ideal gas: 
$$U = \frac{i}{2} nRT$$

# Convenient connections

$$U = \frac{i}{2} nRT$$



$$PV = n \cdot R \cdot T$$

$$U = \frac{i}{2} \cdot PV$$

# Convenient connections

$$U = \frac{i}{2} nRT$$

Internal energy

$$U = \frac{i}{2} PV$$

$$PV = nRT$$

$$\Delta U = \frac{i}{2} R \Delta(nT) = \frac{i}{2} \Delta(PV)$$

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$$\Delta U = \frac{i}{2} \Delta(VP)$$

or

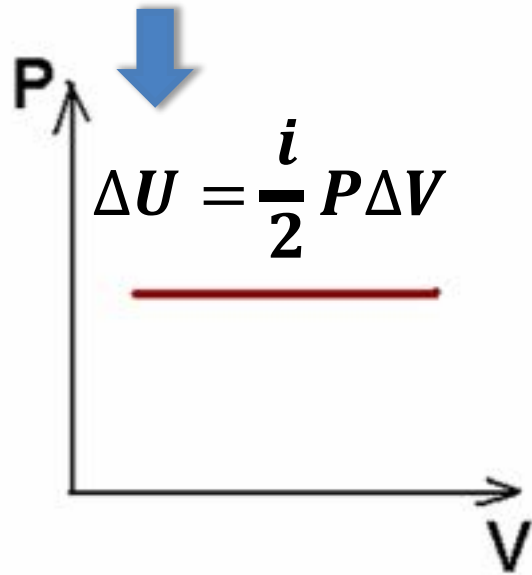
$$\Delta U = \frac{i}{2} nR\Delta T$$

Three standard processes ( $n = \text{const}$ ):

Isobaric

$$P = \text{const}$$

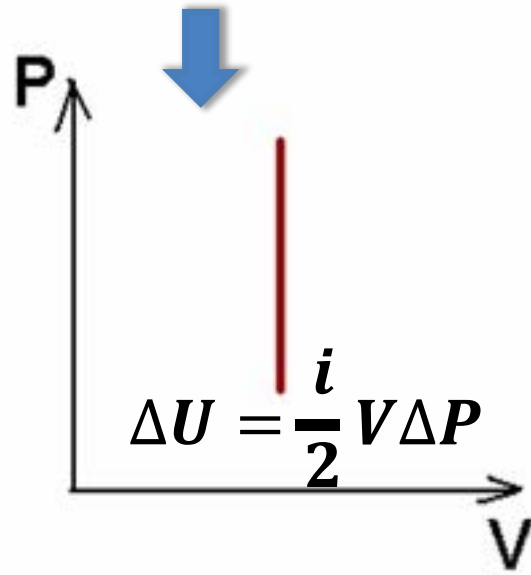
$$V/T = \text{const}$$



Isochoric

$$V = \text{const}$$

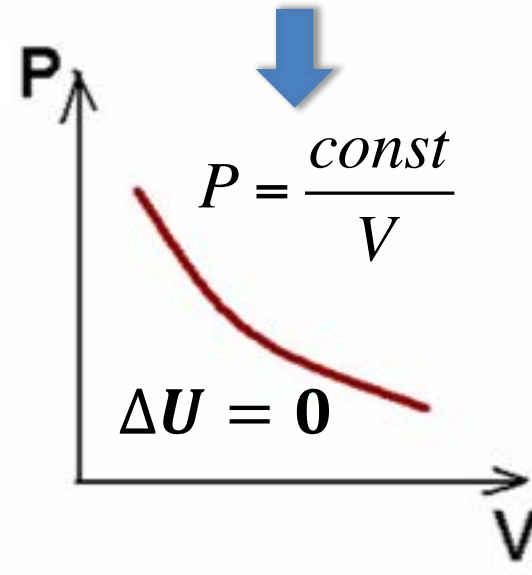
$$P/T = \text{const}$$



Isothermal

$$T = \text{const}$$

$$PV = \text{const}$$



always


$$n = m/M$$

$$n = \text{const}$$

$$\frac{PV}{Tn} = R = 8.31 \text{ J/(K mole)}$$

(Try to plot graphs for the same processes using PT and VT axes)

## Previewer Tools

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Show: All, None  Assignment Score  Key  Solution  Help/Hints  Mark  Answer Format Tips

Current Score: 0/9 Due: Thu Jun 30 2016 11:00 PM EDT

Question	1	2	3	4	5	6	7	Total
Points	0/2	0/1	0/1	0/2	0/1	0/1	0/1	0/9

## Description


Gases, work and energy, 1LT, 2LT, engines

1.  0/2 points

OSColPhys1 13.P.036.WA. [26

Two insulated cylinders  $A$  and  $B$  with volumes  $V_A = 1.4 \text{ m}^3$  and  $V_B = 5.2 \text{ m}^3$  contain chlorine gas at different pressures and temperatures. The cylinders are insulated (no heat is lost to or gained from the outside) and connected by a valve. Initially the valve is closed and the gas in the two cylinders has the following values:

$$P_A = 4.0 \times 10^5 \text{ N/m}^2, \quad T_A = 190 \text{ K}, \quad P_B = 2.5 \times 10^5 \text{ N/m}^2, \quad T_B = 500 \text{ K}.$$

6.  0/1 points

OSColPhys1 15.P.019.WA. [261175

Calculate the net work output of a heat engine following path ABCDA in the figure below, where  $V_1 = 6.6 \times 10^{-3} \text{ m}^3$  and  $V_2 = 26.4 \times 10^{-3} \text{ m}^3$ .

Calculate the internal energy and the pressure of 1 kg of a Hydrogen gas at the room temperature held in a 1 L jar.

$$T \sim 20^\circ\text{C} \Rightarrow T = 273 + 20 = 293\text{K}$$

$$PV = nRT$$

$$U = \frac{i}{2} nRT$$

$$U = \frac{i}{2} PV$$

$$n = \frac{m}{M}$$

$$n = \frac{m}{M} = \frac{1\text{kg}}{2 \cdot \frac{\text{g}}{\text{mol}}}$$

$$V = 1\text{L} = 10^{-3}\text{m}^3$$

$$PV = nRT$$

$$P = \frac{500 \cdot 8 \cdot 293}{10^{-3}} = 1.17 \cdot 10^9 \text{Pa}$$

$$= \frac{1000\text{g}}{2\text{g}} \text{mol} = 500\text{mol}$$

$$U = \frac{5}{2} \cdot nRT = \frac{5}{2} \cdot 500 \cdot 8 \cdot 293 = 2.9 \cdot 10^6 \text{J}$$



Calculate the change in the internal energy of a Hydrogen gas that expands from an initial volume of 3 L and initial pressure of 300 kPa to a final volume of 7 L at constant temperature.

[Webassign:L23 Q6](#)

1.  $\Delta U > 0$

2.  $\Delta U = 0$

3.  $\Delta U < 0$

$$U = \frac{i}{2} nRT \quad PV = nRT$$

$$U = \frac{i}{2} PV$$

$$n = \frac{m}{M}$$

Calculate the change in the internal energy of a Hydrogen gas that expands from an initial volume of 3 L and initial pressure of 300 kPa to a final volume of 7 L at constant temperature.

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~~1.  $\Delta U > 0$~~

2.  $\Delta U = 0$

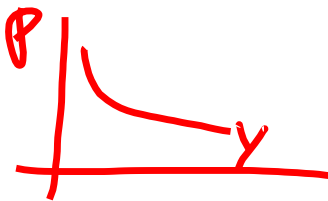
~~3.  $\Delta U < 0$~~

$U = \frac{i}{2} nRT$      $PV = nRT$

$U = \frac{i}{2} P \cdot V$

$n = \frac{m}{M}$

$P = \text{const}$



$U = \frac{i}{2} n R \cdot P$   
 $\downarrow$  const     $\downarrow$  const

$\Rightarrow U = \text{const}$   
 $\Delta U = 0$

$$U = \frac{i}{2} nRT$$

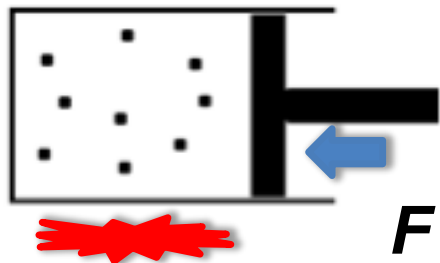
**Two ways to change  $U$**

$$U = \frac{i}{2} PV$$

**Thermal contact**

**Do work**

$$\Delta U = Q + W_{\text{on system}}$$

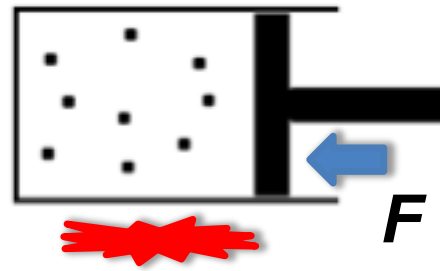


$$\Delta U = Q + W_{\text{on system}}$$

$$W_{\text{on system}} = -W_{\text{by system}}$$

**N3L!**

$$\Delta U = Q - W_{\text{by system}}$$



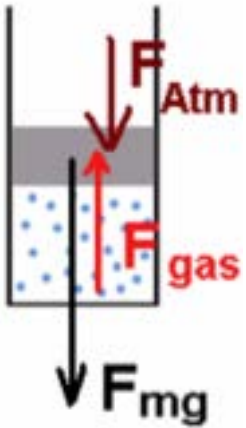
$$U = \frac{i}{2} nRT$$

# The First Law of Thermodynamics

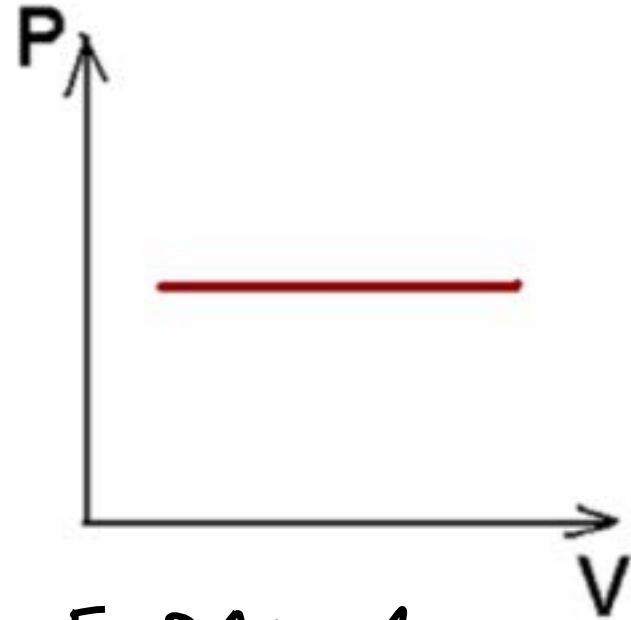
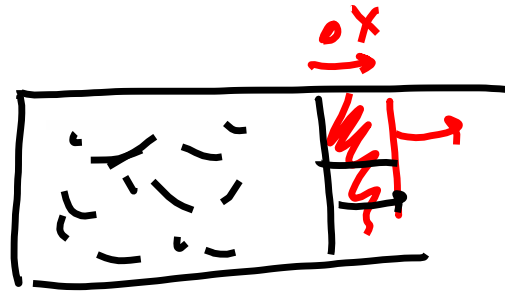
$$Q = \Delta U + W_{\text{by system}}$$

For example: The heat *absorbed* by the system can be *spent*  $\Rightarrow \Delta U$  or  $W_{\text{by system}}$ .

# WORK done by a gas.



Isobaric  
 $P = \text{const}$



$$P = \text{const} \Rightarrow F = P \cdot A = \text{const}$$

$$|W| = F \cdot \Delta s \cdot \cancel{\cos 0} = P \cdot \underbrace{(A \cdot \Delta s)}$$

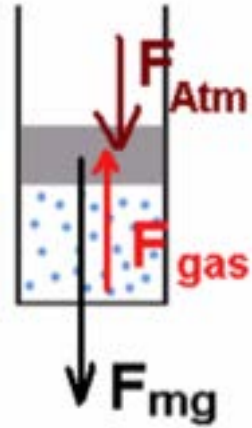
$$|W| = P \cdot \Delta V$$

$\downarrow$   
const

# WORK done by a gas.

Isobaric

$$F = \text{const} \quad \Leftrightarrow P = \text{const}$$

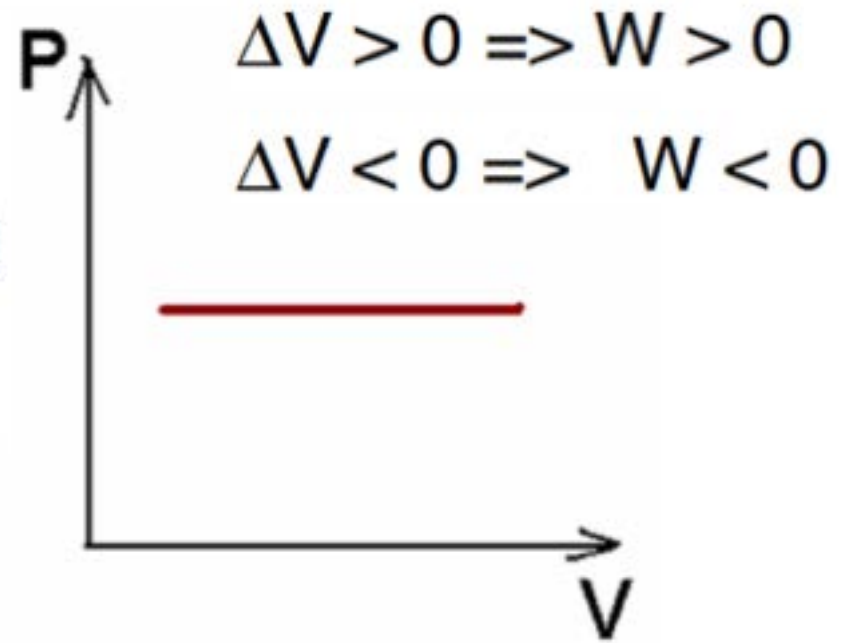


$$W = F * \Delta x \quad V/T = \text{const}$$

$$F = P * A, \text{ so:}$$

$$\underline{W} = P * A * \Delta x = P * \Delta(Ax) = \underline{P * \Delta V}$$

$$PV = nRT$$



At constant pressure the work done by the system is the pressure multiplied by the change in volume.

If there is a change in volume and the pressure changes the work done by the system is the area under the P-V graph.

$$PV = nRT$$

This is why P-V diagrams are so useful in thermodynamics.

$$\Delta V > 0 \Rightarrow W > 0 \quad | \quad \Delta V < 0 \Rightarrow W < 0$$

$$P = \text{const} \Rightarrow F = PA = \text{const}$$

$$W = P \cdot \Delta V = P \cdot (V_2 - V_1)$$

$$P \neq \text{const}$$

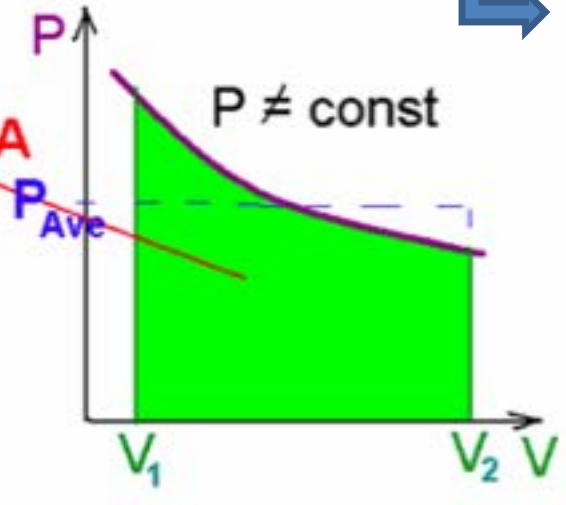
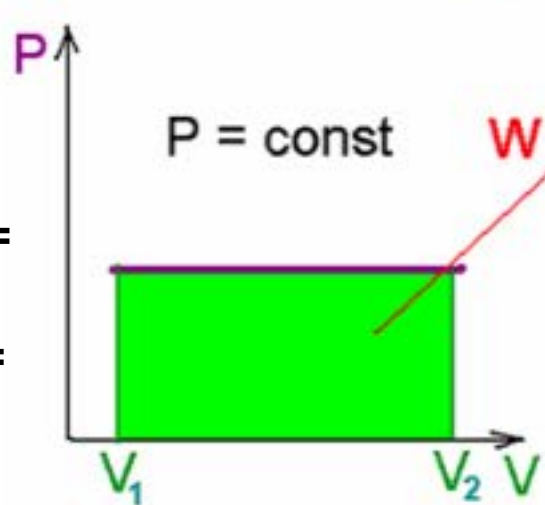
$$W = P_{\text{Ave}} \cdot \Delta V = \text{Area (P-V graph)}$$



$$W_{P=\text{const}} =$$

$$= P \Delta V =$$

$$= nR \Delta T$$



$$V_i = V_f$$

$$W = 0!$$

+ or -

The summary of the 97 % of the last topics

$$PV = nRT$$

$$U = \frac{i}{2} PV$$

$$U = \frac{i}{2} nRT$$

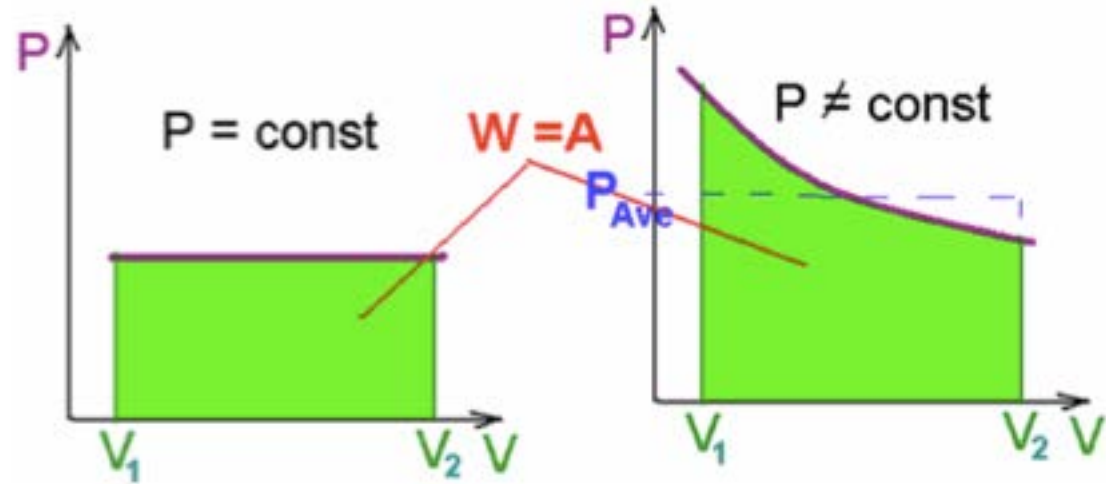
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$$Q = \Delta U + W_{\text{by system}}$$



$$W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$$