



**Good morning!**

**Lab 10 is in SCI136**

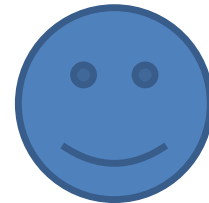
**For labs 2 – 10 the best 8 scores out of 9 will be used for the final grade calculation**

**Please, login into webassing, locate  
LectureMCQ\_L24 (PY105)**

**and answer question 1**

**(but ONLY Q1!).**

**Thank you!**



## For L245 Q2

For the question on the screen, select the number corresponding to the correct answer

1  
87.3% 69

2  
10.1% 8

3  
1.27% 1

4

5

6  
1.27% 1

**WRONG!**



The summary of the 97 % of the last topics

$$PV = nRT$$

$$U = \frac{i}{2} PV$$

$$U = \frac{i}{2} nRT$$

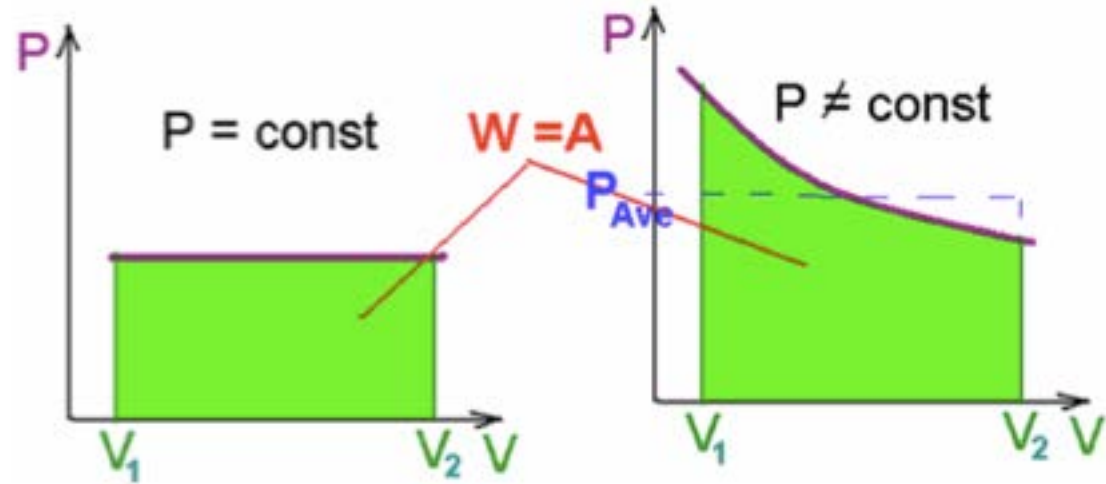
$$n = \frac{m}{M}$$

$i = 3$  • for point-like particles

$i = 5$  •—• for dumbbell-like particles (no oscillations)

$i = 6$  •—• for big particles made of 3 or more atoms (no oscillations)

$$Q = \Delta U + W_{\text{by system}}$$



$$W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$$

**Calculate the change in the internal energy of a Hydrogen gas that expands from an initial volume of 3 L and initial pressure of 300 kPa to a final volume of 7 L at constant pressure.**

$$PV = nRT$$

$$U = \frac{i}{2}PV$$

$$U = \frac{i}{2}nRT$$

$$n = \frac{m}{M}$$

**Webassign: L24 Q3**

**The work done by the gas during the process is ...**

**1. < 0      2. = 0      3. > 0**



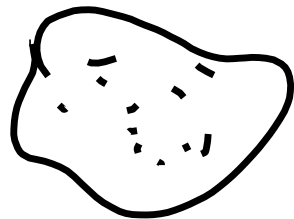
Calculate the change in the internal energy of a Hydrogen gas that expands from an initial volume of 3 L and initial pressure of 300 kPa to a final volume of 7 L at constant pressure.

$$PV = nRT$$

$$U = \frac{i}{2} nRT$$

$$U = \frac{i}{2} PV$$

$$n = \frac{m}{M}$$



$i = ?$

$H_2 \Rightarrow i = 5$

$W_{\text{by\_gas}}$  1.  $< 0$       2.  $= 0$       3.  $> 0$

$$U_i = \frac{i}{2} P V_i$$

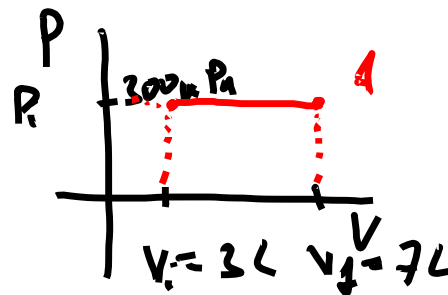
$$U_f = \frac{i}{2} P V_f$$

$$\Delta U = U_f - U_i = \frac{5}{2} P \cdot V_f - \frac{5}{2} P \cdot V_i =$$

$$= \frac{5}{2} P \cdot (V_f - V_i) = \frac{5}{2} P \Delta V =$$

$$= \frac{5}{2} \cdot 300 \text{ kPa} \cdot 4 \text{ L} = \frac{5}{2} \cdot 300 \cdot 10^3 \text{ Pa} \cdot 4 \cdot 10^{-3} \text{ m}^3 = 3000 \text{ J}$$

$V_f > V_i \Rightarrow \Delta V > 0$



$P = \text{const}$

$$W = P \cdot \Delta V$$

Calculate the change in the internal energy of a Hydrogen gas that expands from an initial volume of 3 L and initial pressure of 300 kPa to a final volume of 7 L at constant pressure.

Webassign: L24 Q3

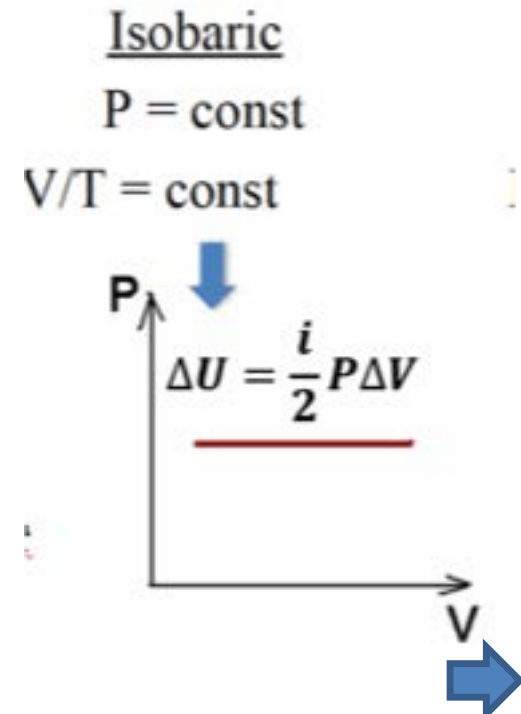
$$U = \frac{i}{2}PV$$

The work done **by** the gas during the process is ...

1.  $< 0$       2.  $= 0$       3.  $> 0$

$$\Delta U = \frac{i}{2}P\Delta V$$

**V and T must change!**



Calculate the amount of heat a Hydrogen gas absorbs/releases when it expands from an initial volume of 3 L and initial pressure of 300 kPa to a final volume of 7 L at constant pressure.

$$PV = nRT$$

$$n = \frac{m}{M}$$

$$n = \frac{m}{M}$$

$$U = \frac{i}{2} nRT \quad U = \frac{i}{2} PV$$

$$Q = cm\Delta t \quad ; \quad Q = \Delta U + W = 3000 + W$$

$$W = \int_{P=\text{const}} P \Delta V = 300 \text{ kPa} \cdot 4 \text{ L} = 1200 \text{ J}$$

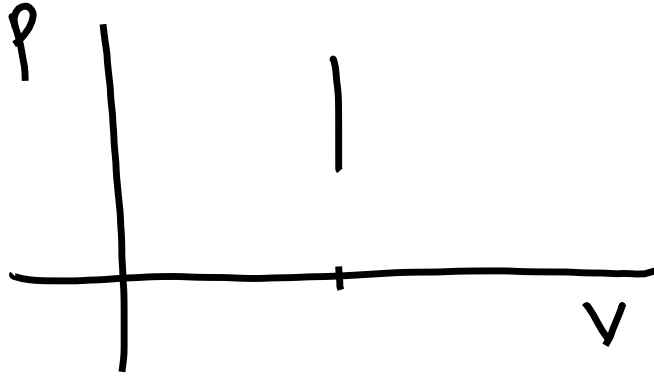
$$3000 = \frac{\sum P \cdot \Delta V}{2} = \frac{\sum W}{2} \Rightarrow W = \frac{2}{5} \cdot \Delta U = \frac{2}{5} \cdot 3000$$

$$\text{if } P = \text{const} \quad \Delta U = \frac{i}{2} \cdot W$$

$$Q = 3000 + 1200 = 4200 \text{ J} > 0$$

$W$

$$V = \omega h f$$



- $> 0$  1.
- $= 0$  2.
- $< 0$  3.

$$W = P_{\text{Ave}} \cdot \vec{V} = P_{\text{Ave}} \cdot \phi = \phi$$

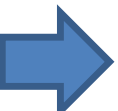


**A container of a monatomic ideal gas contains just the right number of moles so that  $nR = 20 \text{ J/K}$ . The gas is in state 1 such that:  $P_1 = 20 \text{ kPa}$  and  $V_1 = 100 \text{ L}$**

**(a) What is the temperature  $T_1$  of the gas?**

$$PV = nRT \quad n = \frac{m}{M} \quad Q = \Delta U + W_{\text{by system}}$$

$$U = \frac{i}{2} nRT \quad U = \frac{i}{2} PV \quad W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$$



A container of a monatomic ideal gas contains just the right number of moles so that  $nR = 20 \text{ J/K}$ . The gas is in state 1 such that:  $P_1 = 20 \text{ kPa}$  and  $V_1 = 100 \text{ L}$

(a) What is the temperature  $T_1$  of the gas?

$$PV = nRT$$

[Webassign: L24 Q4](#)

$$n = \frac{m}{M}$$

$$T_1 =$$

$$U = \frac{i}{2} nRT$$

1. 100 K

2. 200 K

$$U = \frac{i}{2} PV$$

3. 300 K

4. ...

$$Q = \Delta U + W_{\text{by system}}$$

$$W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$$



A container of a monatomic ideal gas contains just the right number of moles so that  $nR = 20 \text{ J/K}$ . The gas is in state 1 such that:  $P_1 = 20 \text{ kPa}$  and  $V_1 = 100 \text{ L}$

(a) What is the temperature  $T_1$  of the gas?

$$PV = nRT$$

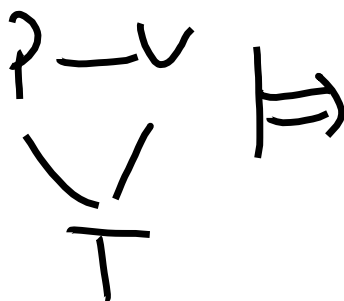
$$n = \frac{m}{M}$$

$$U = \frac{i}{2} nRT$$

$$U = \frac{i}{2} PV$$

$$Q = \Delta U + W_{\text{by system}}$$

$$W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$$


$$PV = nRT$$
$$20 \text{ kPa} \cdot 100 \text{ L} = 20 T_1$$
$$\frac{20 \cdot 100}{20} = T_1$$
$$T_1 = 100 \text{ K}$$

**A container of monatomic ideal gas contains just the right number of moles so that  $nR = 20 \text{ J/K}$ . The gas is in state 1 such that:  $P_1 = 20 \text{ kPa}$  and  $V_1 = 100 \text{ L}$   
(a) What is the temperature  $T_1$  of the gas?**

**Use the ideal gas law:  $PV = nRT$ , so:  
 $T_1 = P_1V_1/nR = 2000/20 = 100 \text{ K}$**

**A container of a monatomic ideal gas contains just the right number of moles so that  $nR = 20 \text{ J/K}$ . The gas is in state 1 such that:  $P_1 = 20 \text{ kPa}$  and  $V_1 = 100 \text{ L}$ .**

**(b) If  $Q = 2500 \text{ J}$  of heat is added to the gas, and the gas expands at constant pressure, the gas will reach a new equilibrium state 2. What is the final temperature  $T_2$ ?**



A monatomic gas has just the right number of moles;  $nR = 20 \text{ J/K}$ .  
The initial state :  $P_1 = 20 \text{ kPa}$  and  $V_1 = 100 \text{ L}$ . (b) If  $Q = 2500 \text{ J}$  of heat is added to the gas, and the gas expands at constant pressure, what is the final temperature  $T_2$ ?

[Webassign: L24 Q5](#)

1.  $PV = nRT$

2.  $n = \frac{m}{M}$

3.  $U = \frac{i}{2}nRT$

4.  $U = \frac{i}{2}PV$

5.  $Q = \Delta U + W_{\text{by system}}$

6.  $W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$

To relate  $T_2$  and  $Q$  we will  
**NOT** need to use equation...

1.    2.    3.    4.    5.    ...



A monatomic gas has just the right number of moles;  $nR = 20 \text{ J/K}$ .  
 The initial state :  $P_1 = 20 \text{ kPa}$  and  $V_1 = 100 \text{ L}$ . (b) If  $Q = 2500 \text{ J}$  of heat  
 is added to the gas, and the gas expands at constant pressure, what  
 is the final temperature  $T_2$ ? [Webassign: L24 Q5](#)

1.  $PV = nRT$  To relate  $T_2$  and  $Q$  we will NOT need to use equation...

2.  $n = \frac{m}{M}$  1. 2. 3. 4. 5. ...

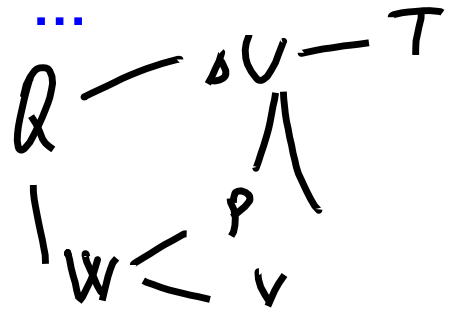
3.  $U = \frac{i}{2} nRT$

4.  $U = \frac{i}{2} PV$

5.  $Q = \Delta U + W_{\text{by system}}$

6.  $W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$

$Q = P \Delta V$   
 $Q = c \cdot m \cdot \Delta T$



$$2500 = Q = \Delta U + W = \frac{3}{2} nR \cdot \Delta T + P \cdot \Delta V = \frac{3}{2} nR \cdot \Delta T + nR \Delta T = \Delta T \cdot 20 \cdot \left(\frac{3}{2} + 1\right)$$

$$\Delta T = \frac{2500}{20 \cdot \frac{5}{2}} = 50 \text{ K}$$

$$T_2 = T_1 + \Delta T \Rightarrow T_2 = 150 \text{ K}$$



A container of monatomic ideal gas contains just the right number of moles so that  $nR = 20 \text{ J/K}$ . The gas is in state 1 such that:  $P_1 = 20 \text{ kPa}$  and  $V_1 = 100 \text{ L}$ .

(b) If  $Q = 2500 \text{ J}$  of heat is added to the gas, and the gas expands at constant pressure, the gas will reach a new equilibrium state 2. What is the final temperature  $T_2$ ? We've already seen that, at constant pressure for a monatomic ideal

gas:  $PV = nRT$   $P = \text{const} \Rightarrow W = P\Delta V = nR\Delta T$

$$Q = \Delta U + W = (3/2)nR\Delta T + nR\Delta T = (5/2)nR\Delta T$$

Therefore  $\Delta T = (2/5)Q/nR = 1000/20 = 50 \text{ K}$ .

$$T_2 = T_1 + \Delta T = 150 \text{ K}$$



**(c) How much work was done by the gas during the expansion?**

$$W = P \cdot \Delta V = \underbrace{nR \cdot \Delta T}_{20 \cdot 50} = 1000 \text{ J}$$

$$\Delta U = Q - W = 2500 - 1000 = 1500 \text{ J}$$

**(d) What is the final volume  $V_2$ ?**

$$P_2 V_2 = nR \cdot T_2 \Rightarrow V_2 = \frac{20 \cdot 150}{20 \cdot P_2} = 150 \text{ L}$$

(c) How much work was done by the gas during the expansion?

$$W = P\Delta V = nR\Delta T = 20 * 50 = 1000 \text{ J}$$



(This equation is true only for a constant pressure process)

(d) What is the final volume  $V_2$ ?

One approach is to bring in the ideal gas law again:

$$V_2 = nRT_2/P_2 = 20(150)/(20 \times 10^3) = 150 \times 10^{-3} \text{ m}^3$$

**62,325 J of heat energy is transferred to a system consisting of 30 moles of an ideal gas. If the volume of this gas stays constant at 40 L, calculate the change in the internal energy of the gas.**

**Webassign: L24 Q7**

**The work of the gas is**

- 1.  $> 0$**
- 2.  $= 0$**
- 3.  $< 0$**

**Webassign: L24 Q6**

**$\Delta U$  is**

- 1.  $> 62,325 \text{ J}$**
- 2.  $= 62,325 \text{ J}$**
- 3.  $< 62,325 \text{ J}$**



**62,325 J of heat energy is transferred to a system consisting of 30 moles of an ideal gas. If the volume of this gas stays constant at 40 L, calculate the change in the internal energy of the gas.**

**Webassign: L24 Q7**

**The work of the gas is**

- 1.  $> 0$**
- 2.  $= 0$**
- 3.  $< 0$**

$$\begin{array}{l} V = \text{const} \\ W = 0 \end{array} \quad |$$

**Webassign: L24 Q6**

**$\Delta U$  is**

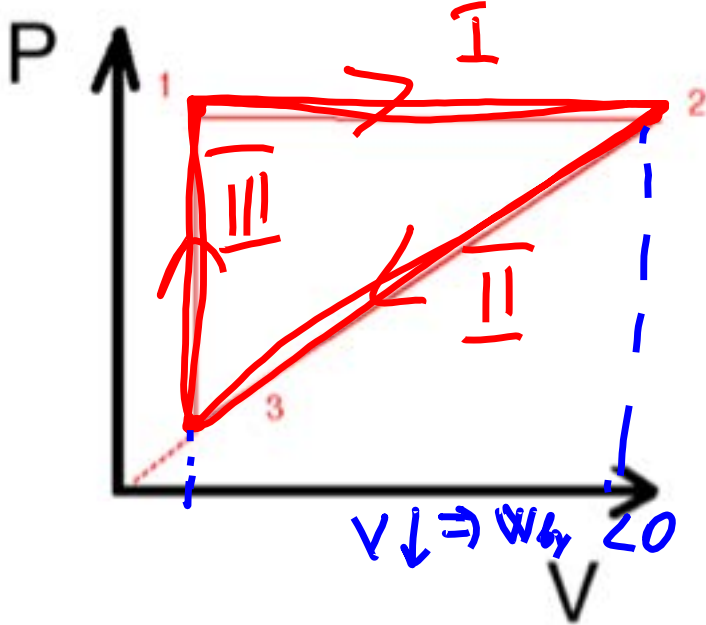
- 1.  $> 62,325 \text{ J}$**
- 2.  $= 62,325 \text{ J}$**
- 3.  $< 62,325 \text{ J}$**

$$Q = \Delta U + W$$

$$Q > 0 ; W = 0 \Rightarrow \Delta U = Q > 0$$

$$\Delta U = Q = 62325 \text{ J}$$

Webassign: L24 Q8



A diatomic gas is a subject of three different processes. The work done on the gas during process 2 -> 3 is ...

1.  $< 0$       2.  $= 0$       3.  $> 0$

- $nR = 300 \text{ J/K}$
- $P_1 = 600 \text{ kPa}$
- $P_3 = 200 \text{ kPa}$
- $V_1 = 40 \text{ L}$
- $V_2 = 120 \text{ L}$

$$PV = nRT$$

$$Q = \Delta U + W_{\text{by system}}$$

$$U = \frac{i}{2} nRT$$

$$U = \frac{i}{2} PV$$

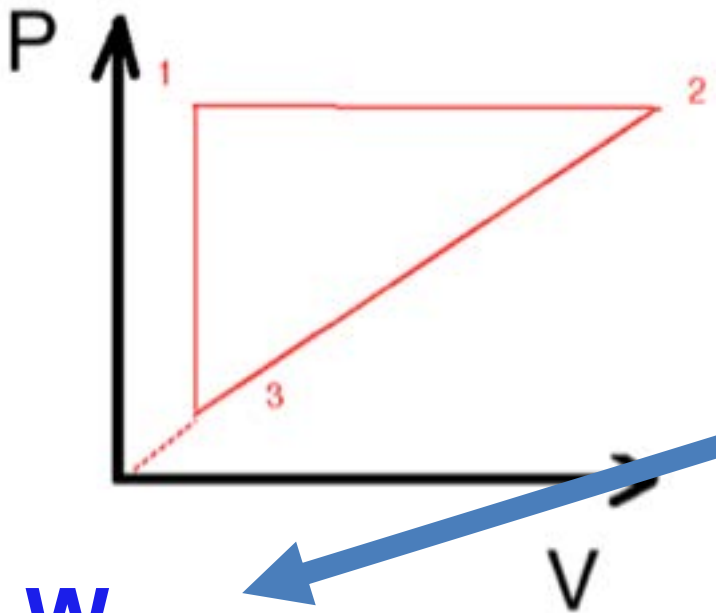
$$n = \frac{m}{M}$$

$$W_{\text{by}} = -W_{\text{on}}$$

$$W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$$



Webassign: L24 Q8



A diatomic gas is a subject of three different processes.

The work done on the gas during process 2 → 3 is ...

- 1.  $< 0$
- 2.  $= 0$
- 3.  $> 0$

$W_{\text{on\_gas}} \dots$

$> 0$

$$PV = nRT$$

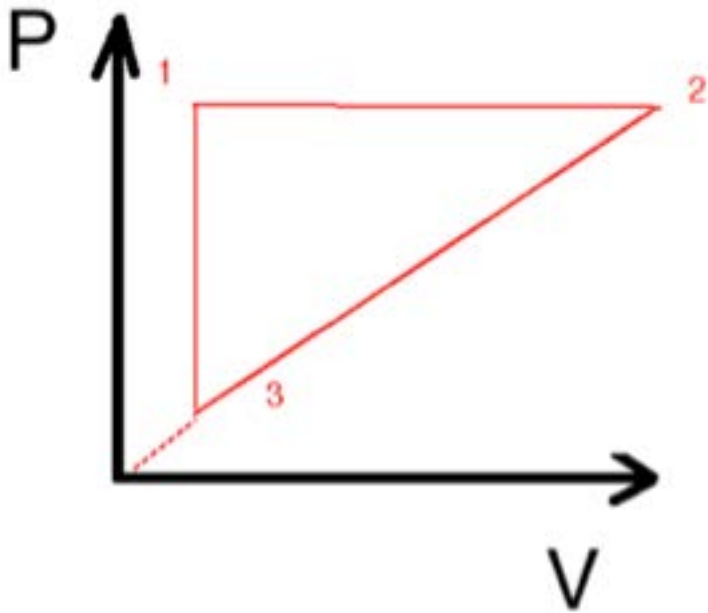
$$Q = \Delta U + W_{\text{by system}}$$

$$U = \frac{i}{2} nRT$$

$$U = \frac{i}{2} PV$$

$$n = \frac{m}{M}$$

$$W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$$



A diatomic gas is a subject of three different processes.  
 Calculate the work done by the gas during process 1-→2

$$PV = nRT$$

$$Q = \Delta U + W_{\text{by system}}$$

$$nR = 300 \text{ J/K}$$

$$P_1 = 600 \text{ kPa}$$

$$P_3 = 200 \text{ kPa}$$

$$V_1 = 40 \text{ L}$$

$$V_2 = 120 \text{ L}$$

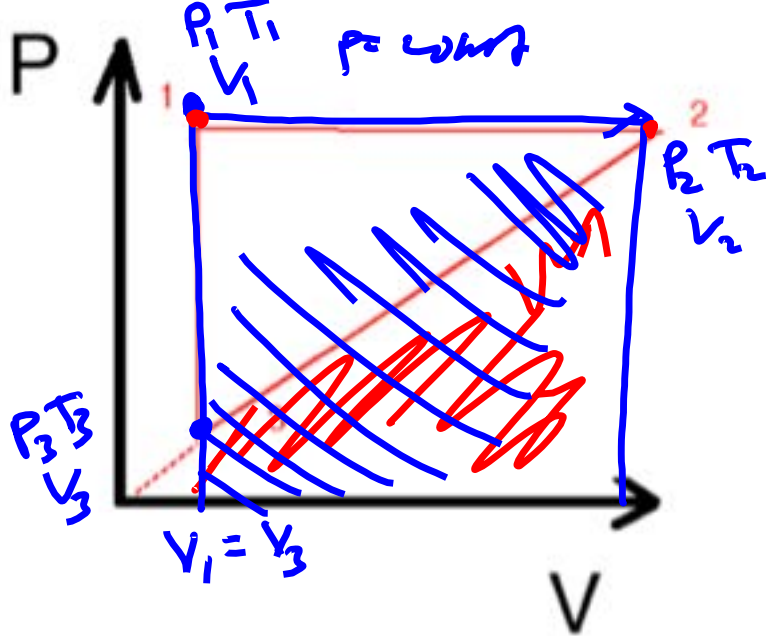
$$U = \frac{i}{2} nRT$$

$$U = \frac{i}{2} PV$$

$$n = \frac{m}{M}$$

$$W = P_{\text{Ave}} * \Delta V = \text{Area (P-V graph)}$$





A diatomic gas is a subject of three different processes. Calculate the work done by the gas during process 1- $\rightarrow$ 2

$$V_{1 \rightarrow 2} \nearrow \Rightarrow \underline{W > 0}$$

$$W_{1 \rightarrow 2} = A = P_1 \cdot \Delta V = P_1 \cdot (V_2 - V_1) =$$

$$= 600 \cdot \text{kPa} \cdot (120 - 40) \text{ L} =$$

$$= 600 \cdot 80 = 48000 \text{ J}$$

$$W_{2 \rightarrow 3} = A_{\square} = -|A_{\square}| ; W_{\text{tot}} = W_{1 \rightarrow 2} + W_{2 \rightarrow 3} + W_{3 \rightarrow 1}$$

$$W_{3 \rightarrow 2} = \emptyset$$

$$nR = 300 \text{ J/K}$$

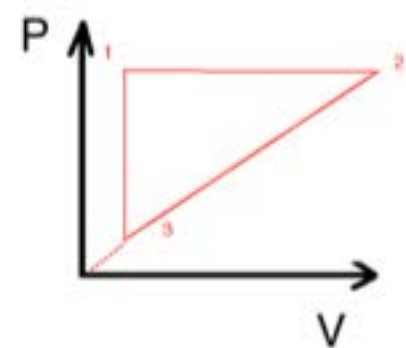
$$P_1 = 600 \text{ kPa}$$

$$P_3 = 200 \text{ kPa}$$

$$V_1 = 40 \text{ L} = V_3$$

$$V_2 = 120 \text{ L}$$





A diatomic gas is a subject of three different processes.

Calculate ... **everything!**

- $nR = 300 \text{ J/K}$
- $P_1 = 600 \text{ kPa}$
- $P_3 = 200 \text{ kPa}$
- $V_1 = 40 \text{ L}$
- $V_2 = 120 \text{ L}$

$\hookrightarrow \underline{P, T, V} \rightarrow \text{state}$

$\underline{Q, \Delta U, W} \rightarrow \text{Pro} \dots$

$$PV = nRT$$

$$n = \frac{m}{M}$$

$$U = \frac{i}{2} nRT$$

$$U = \frac{i}{2} PV$$

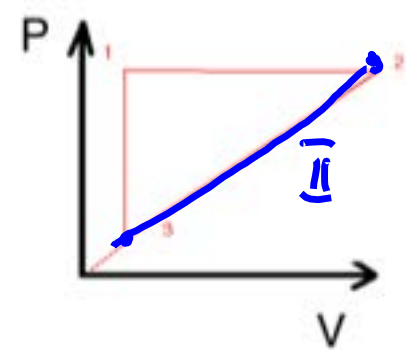
$$Q = \Delta U + W_{\text{by system}}$$

$$W = P_{\text{Ave}} \Delta V = \text{Area (P-V graph)}$$

$$T_1 = \frac{P_1 V_1}{nR} = \frac{600 \cdot 40}{300} = 80 \text{ K}$$

$$T_2 = \frac{P_2 V_2}{nR} = \frac{P_1 V_2}{P_1 n} = \frac{600 \cdot 120}{300} = 240 \text{ K}$$

$$\Delta U_{1 \rightarrow 2} = \frac{i}{2} nR \Delta T = \frac{i}{2} P_1 \Delta V = \frac{i}{2} \cdot W = = \frac{5}{2} \cdot 48000 \text{ J}$$



A diatomic gas is a subject of three different processes.  $nR = 300 \text{ J/K}$   
 $P_2 = P_1 = 600 \text{ kPa}$   
 $P_3 = 200 \text{ kPa}$   
 $V_1 = 40 \text{ L}$   
 $V_2 = 120 \text{ L}$   
 Calculate ... **everything!**

$$PV = nRT$$

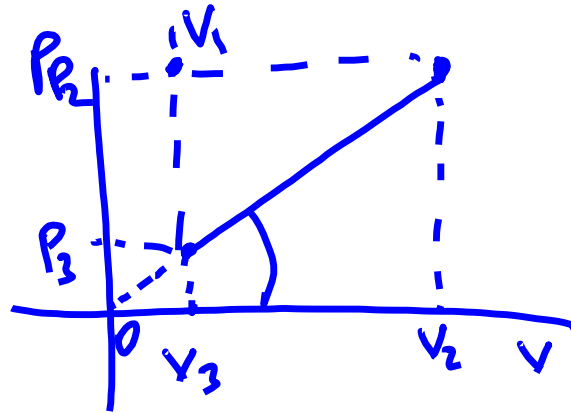
$$n = \frac{m}{M}$$

$$U = \frac{i}{2}nRT$$

$$U = \frac{i}{2}PV$$

$$Q = \Delta U + W_{\text{by system}}$$

$$W = P_{\text{Ave}} \Delta V = \text{Area (P-V graph)}$$



$$\frac{P_2}{V_2} = \frac{P_3}{V_3}$$

---


$$\frac{600}{120} = \frac{200}{40} = 5$$

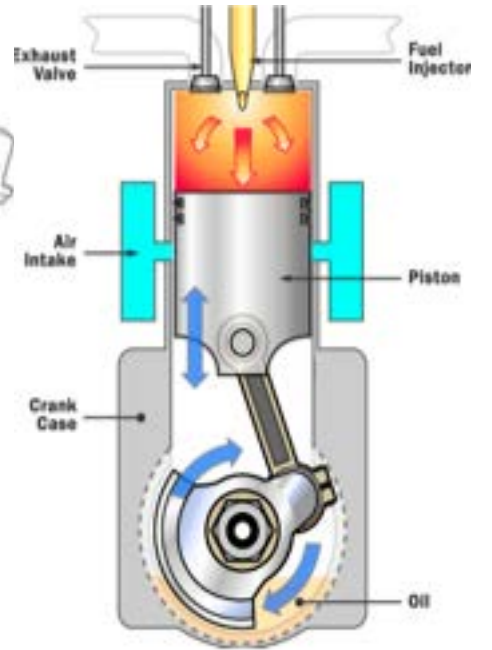
# Steam Engines



## James Watt and the steam engine



# Internal Combustion Engines



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