



Good morning!



Lab 10 is in SCI136

For labs 2 – 10 the best 8 scores out of 9 will be used for the final grade calculation

Lab 11a,b (webassign survey) is optional

Please, login into webassing, locate

LectureMCQ_L25 (PY105)

and answer question 1

(but ONLY Q1!).

Thank you!

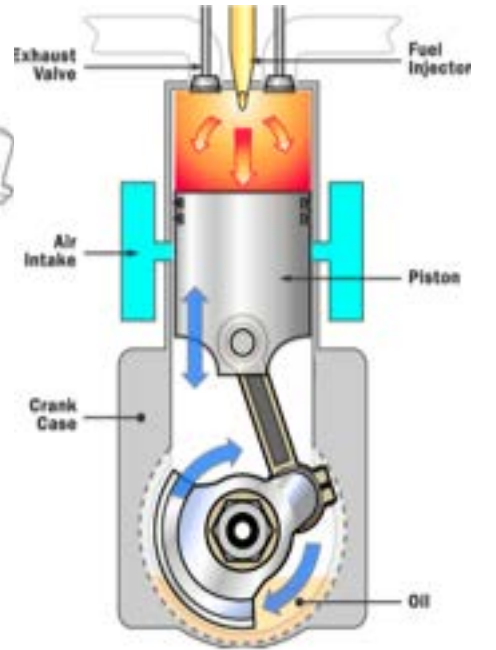
Steam Engines



James Watt and the steam engine



Internal Combustion Engines



96 MAIDEN LANE, NEW YORK

H. O. AGER & H. AGENTS

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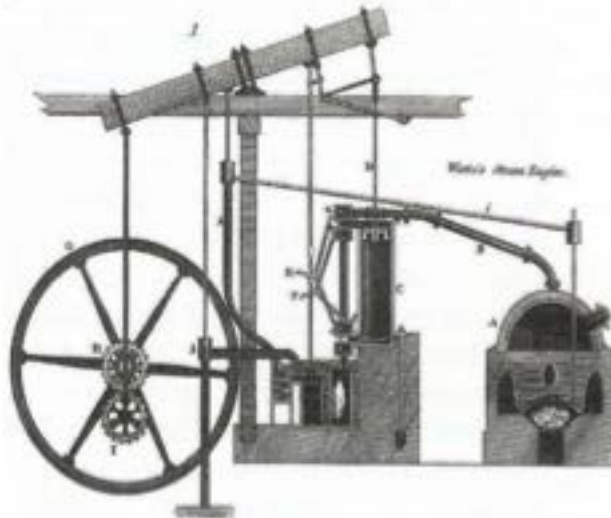
PORTABLE STEAM ENGINES,
OF THE CELEBRATED WATT & BARRY MAKE,
ESPECIALLY ADAPTED FOR DRILLING AND PUMPING OIL WELLS.

For RENTALS and EMPLOYERS, for Workmanship and Material, for Invention Improvements to both Parties and for the result of 25 years' experience in their construction, for general adaptability and economy, and for price and durability, no challenge compares with our other Portable Engines.

EXAMINE AND JUDGE FOR YOURSELF.

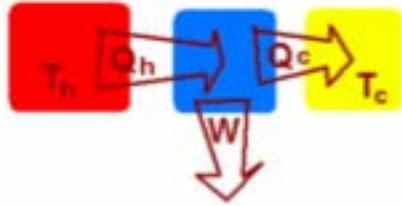
Full information given and orders for all sizes promptly filled by

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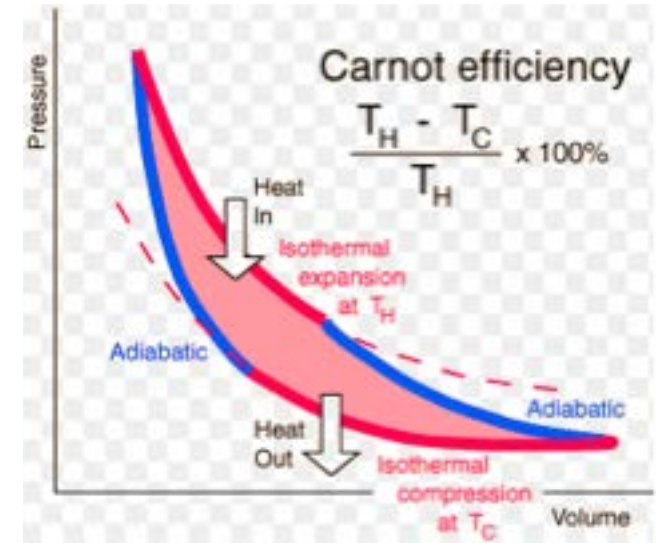
A Heat Engine

The higher temperature causes the system to expand, doing work, and the lower temperature re-sets the engine so another cycle can begin.



In a full cycle of a heat engine, three things happen:

1. Heat Q_h is added at a relatively high temperature T_h .
2. Some of the energy from the input heat is used to do work W .
3. The rest of the energy is removed as heat Q_c at a relatively low temperature T_c .



[Webassign: L25 Q2](#)

For one *complete* cycle:

1. $\Delta U > 0$

2. $\Delta U = 0$

3. $\Delta U < 0$

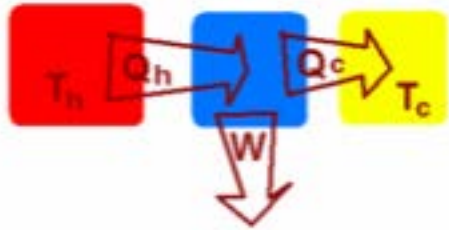
4. It depends on the direction of the cycle

$$U = \frac{i}{2} nRT$$



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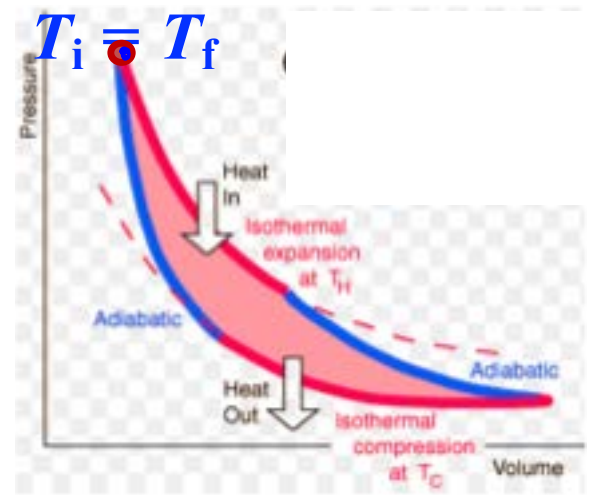
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Webassign: L25 Q2

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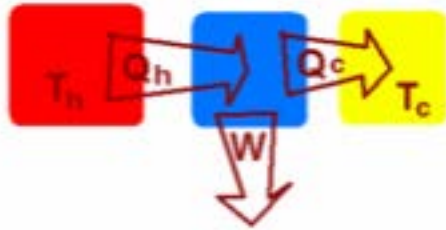


$$P_i = P_f$$

$$\Delta U = \frac{i}{2} nR \Delta P = \phi$$

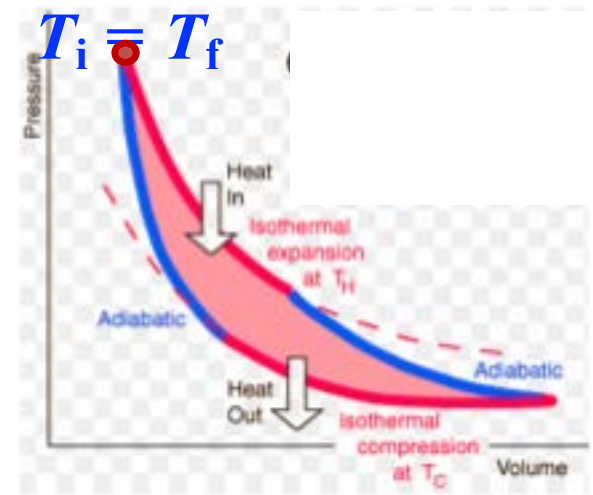
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$$U = \frac{i}{2} nRT$$

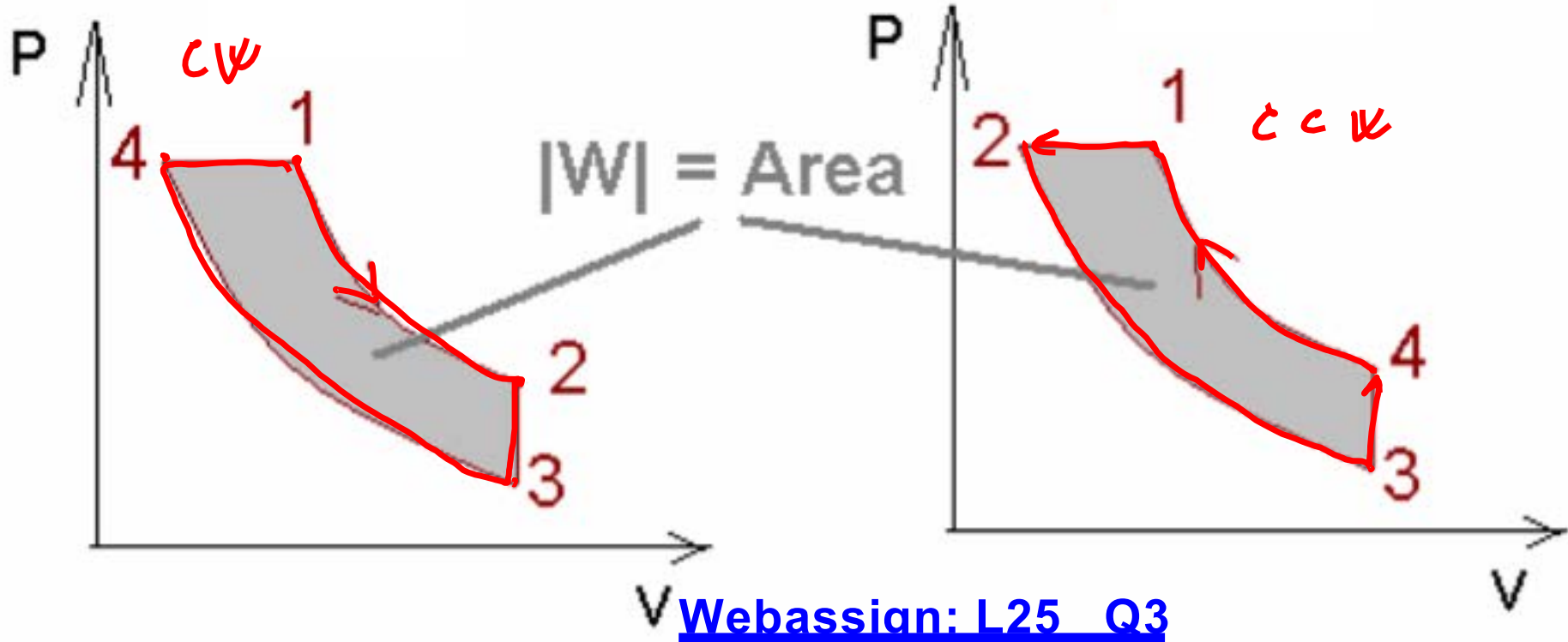
$$T_i = T_f \Rightarrow U_i = U_f$$

$$0$$

For one *complete* cycle:

1. $\Delta U > 0$
2. $\Delta U = 0$
3. $\Delta U < 0$
4. It depends on the direction of the cycle

A cyclic process



Webassign: L25 Q3

The work done by the gas in the cycle on the right is ...

1. > 0
2. 0
3. < 0 .
4. Not enough



A cyclic process

$|W_{cycle}| = ???$

Webassign: L25_Q3

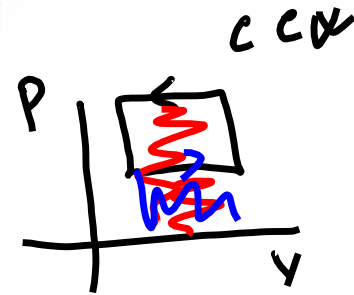
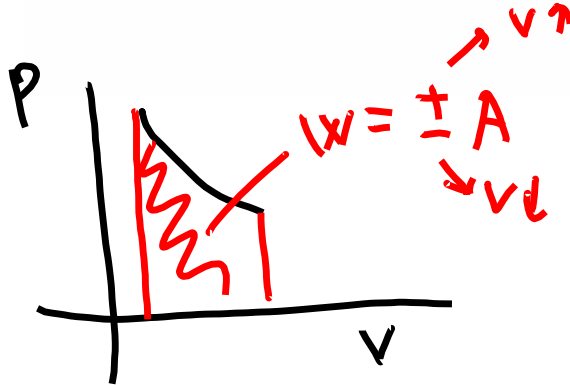
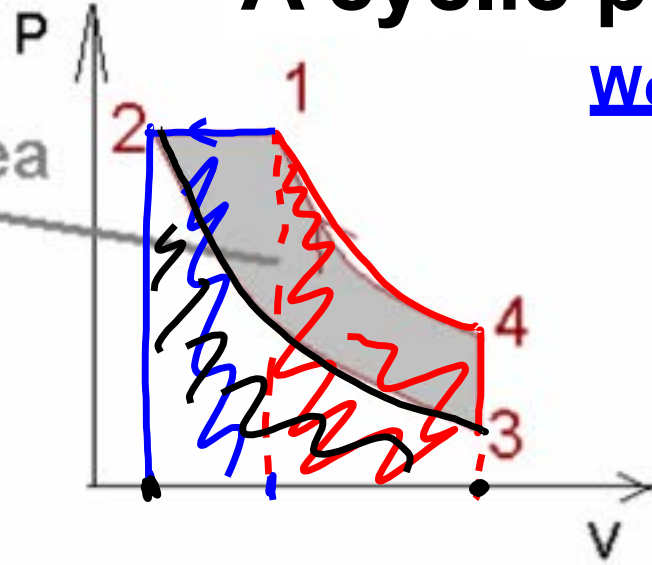
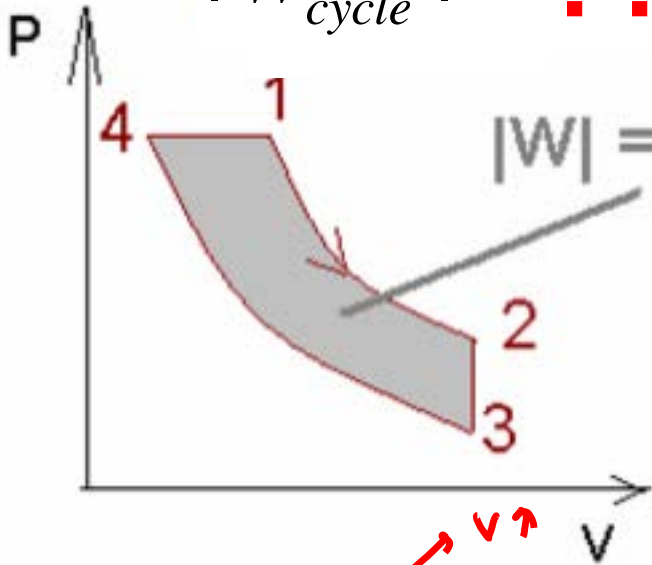
$W_{right_cycle} =$

1. > 0

2. 0

3. < 0

4. Not enough



$W_{3 \rightarrow 4} = 0$

$W_{4 \rightarrow 1} < 0$

$W_{1 \rightarrow 2} < 0$

$W_{2 \rightarrow 3} > 0$

$W_{total} = W_c = W =$
 $= -|A_{41}| - |A_{12}| +$
 $+ |A_{23}| < 0$

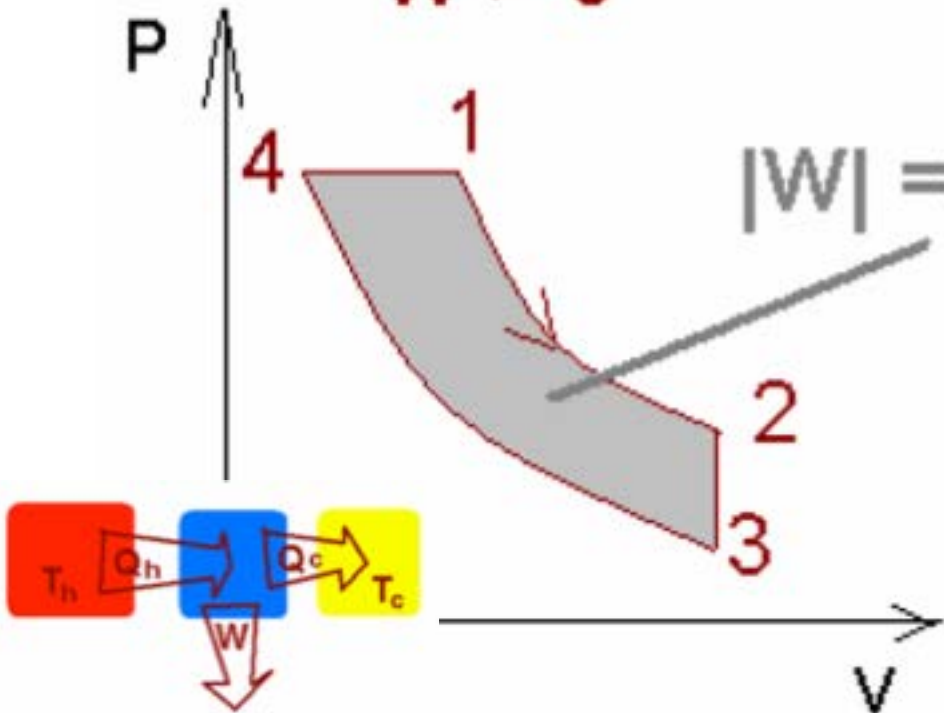
CW cycle

A cyclic process

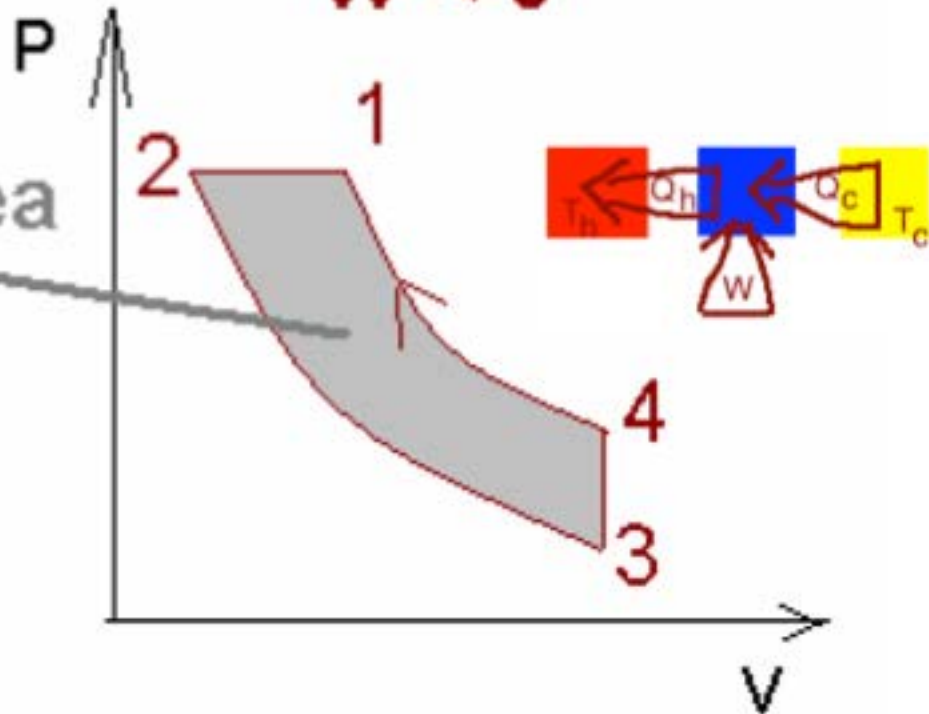
CCW cycle

$W > 0$

$W < 0$



$|W| = \text{Area}$

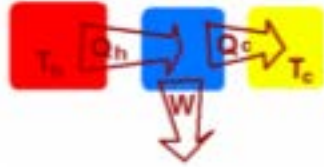


$$|W_{\text{cycle}}| = \text{Area}$$

$$W_{\text{cycle}} = \pm \text{Area}$$

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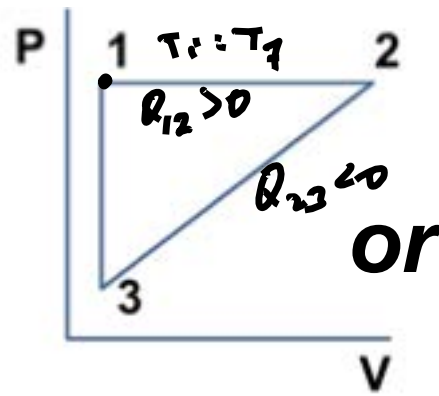
Q, ΔU , W

(1) for each process;

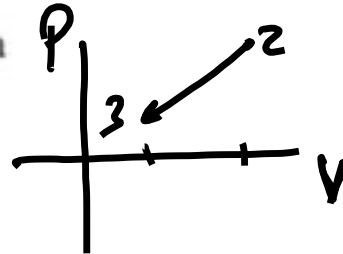
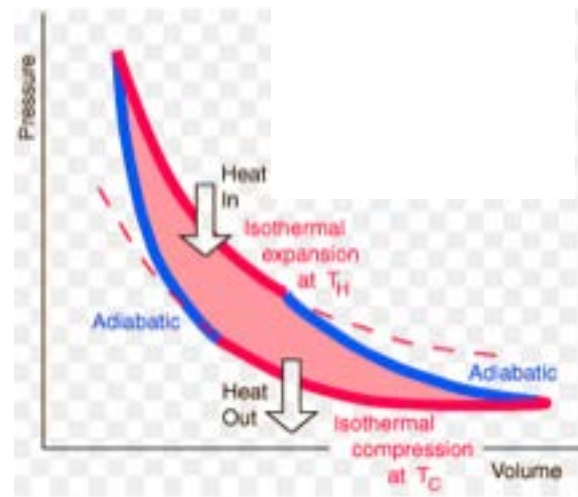
(2) for the cycle.

$$Q_{oh} - |Q_{rec}| = Q_{oh} + Q_{rec} = Q = W \Rightarrow W < Q_{oh}$$

$$\Delta U = \phi ; Q = \Delta U + W$$



Any cycle



$$V \downarrow \Rightarrow W < 0$$

$$P_2 V_2 = n R T_2 ; P_2 V_2 = n R T_3$$

$$P_2 > P_3 ; V_2 > V_3$$

$$\downarrow$$

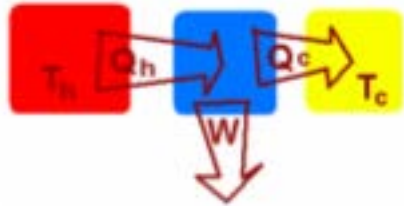
$$P_2 > P_3$$

$$\Delta U = \frac{f}{2} n \Delta T \downarrow$$

$$Q = \Delta U + W < 0 \quad \Delta V < 0$$

A Heat Engine

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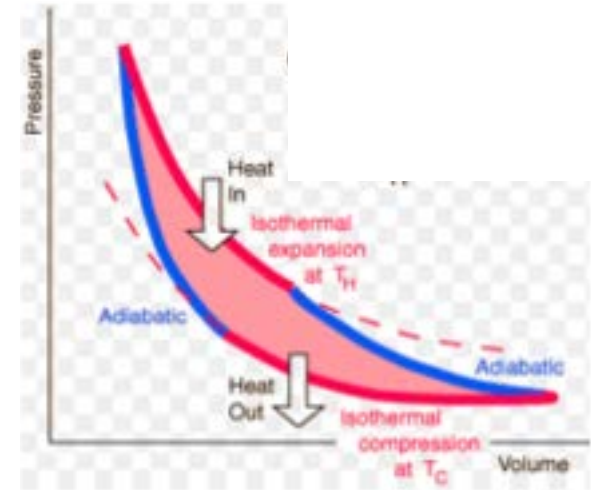


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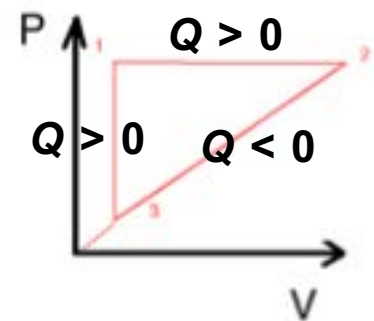
$$Q_{\text{cycle}} = \Delta U_{\text{cycle}} + W_{\text{cycle}}$$

For one complete cycle: $\Delta U_{\text{cycle}} = 0$

1) $Q_{\text{cycle}} = Q_{\text{absorbed}} + Q_{\text{released}}$

2) $Q_{\text{cycle}} = W_{\text{cycle}}$

$\Rightarrow Q_{\text{absorbed}} + Q_{\text{released}} = W_{\text{cycle}}$



320 kJ of heat energy is transferred to a system consisting of 30 moles of an ideal gas.

If the pressure of this gas stays constant at 2000 kPa, and the volume increased from 40 L to 80 L.

Calculate: the change in internal energy of the gas.



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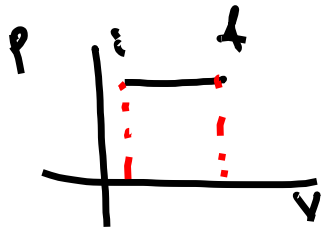
$$Q = 320\,000 \text{ J}$$

$$P = 2000 \text{ kPa}$$

$$V_i = 40 \text{ L}$$

$$V_f = 80 \text{ L}$$

$$n = 30 \text{ mol}$$



$$W = P \cdot \Delta V = 2000 \text{ kPa} \cdot (80 \text{ L} - 40 \text{ L}) = 2000 \cdot 40 = \underline{80\,000 \text{ J}}$$

$$\Delta U = \frac{i}{2} n R_0 T = \frac{i}{2} P_0 V = \frac{i}{2} W = i \cdot \frac{80\,000}{2} = i \cdot 40\,000$$

$$i \begin{matrix} \rightarrow 3 \\ \rightarrow 5 \\ \rightarrow 6 \end{matrix} \text{ (?)}$$

$$Q \begin{matrix} \rightarrow \text{const} \\ \rightarrow \Delta U + W \Rightarrow \end{matrix}$$

$$Q = \Delta U + W$$

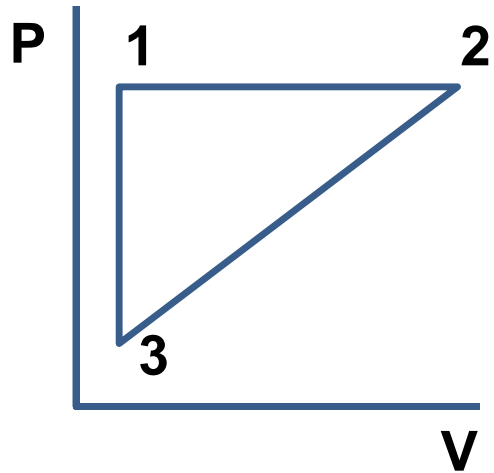
$$320\,000 = i \cdot 40\,000 + 80\,000$$

$$\frac{320\,000 - 80\,000}{40\,000} = i$$

$$\underline{i = 6} \Rightarrow$$

$$\Delta U = 6 \cdot 40\,000 = \underline{240\,000 \text{ J}}$$

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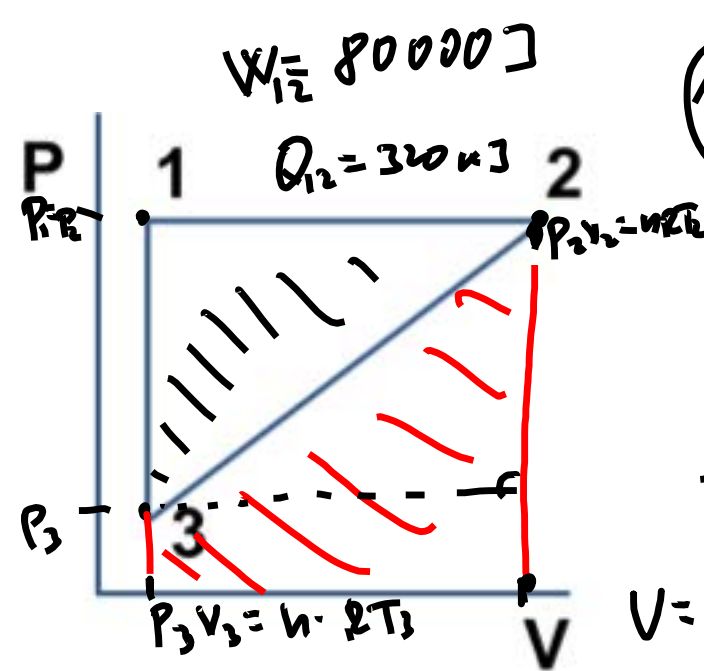


in the diagram, and $P_3 = 1000$ kPa find; how much heat does it absorb, release, and the work done in one cycle.



$Q_{1-2} = 320 \text{ kJ}$; $n = 30 \text{ mol}$; $P_1 = \underline{2000 \text{ kPa}}$, $V_1 = \underline{40 \text{ L}}$; $V_2 = \underline{80 \text{ L}}$
 $P_3 = \underline{1000 \text{ kPa}}$; find; how much heat does it absorb, release, and the work done in one cycle.

$$\Delta U_{\text{cycle}} = 0; \quad Q_{\text{cycle}} = W = \frac{1}{2} \cdot (P_1 - P_3) \cdot (V_2 - V_1) = \frac{1}{2} \cdot 1000 \text{ kPa} \cdot 40 \text{ L} = 20000 \text{ J}$$



2 → 3

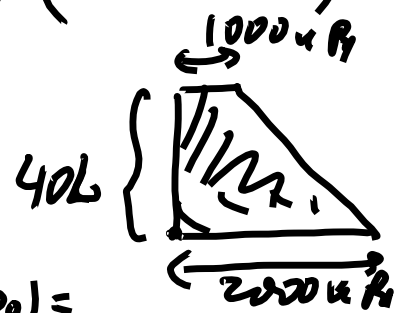
$$Q_{23} = \Delta U_{23} + W_{23}$$

$$W_{23} = -\frac{1}{2} \cdot (V_2 - V_3) \cdot (P_3 + P_2) = -\frac{1}{2} \cdot 40 \text{ L} \cdot (1000 + 2000) = -200000 \text{ J}$$

$$= -200000 \text{ J}$$

$$\Delta U_{23} = \frac{6}{2} (P_3 V_3 - P_2 V_2) = \frac{6}{2} (1000 \cdot 40 - 2000 \cdot 80) = -360000 \text{ J}$$

$$U = \frac{1}{2} n R T = \frac{1}{2} P \cdot V = -3 \cdot 1000 \cdot 120 = -360000 \text{ J}$$

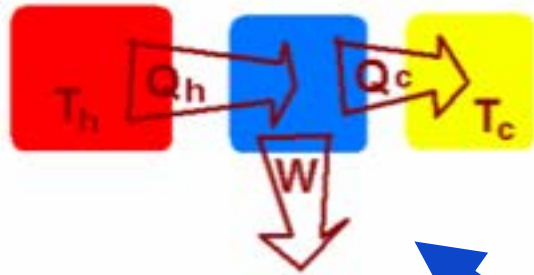


$$W_{\text{cycle}} = W$$

A Heat Engine

$$Q_{\text{cycle}} = Q_{\text{absorbed}} + Q_{\text{released}} = W$$

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The conservation of energy, for a cycle:

$$Q_h = W + |Q_c|$$

$$Q_{\text{absorbed}} > 0$$

$$Q_{\text{released}} < 0$$

$$Q_c = -|Q_c|$$

$$W = Q_h + Q_c = Q_h - |Q_c|$$

Efficiency

$$\underline{Q_h = W + |Q_c|}$$

The efficiency of an engine tells us how much of the input energy ends up doing useful work.

$$W = Q_h - |Q_c| < Q_h$$

ALWAYS!

The efficiency is defined as:

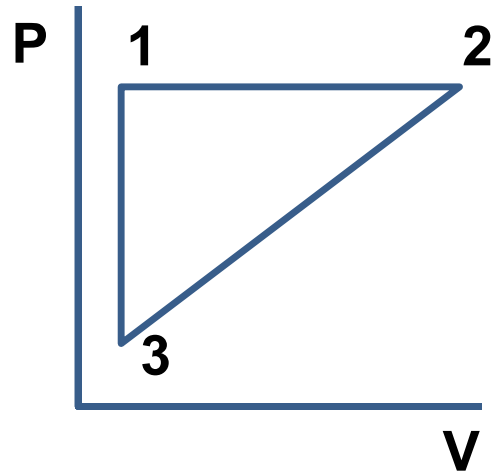
$$\frac{W}{|Q_h|} \cdot 100\% = e$$

$$e = \frac{W}{|Q_h|} = \frac{|Q_h| - |Q_c|}{|Q_h|} = 1 - \frac{|Q_c|}{|Q_h|}$$

For ANY engine

This is the maximum possible efficiency of an engine. In practice losses from friction and other sources reduce the efficiency.

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in the diagram, and $P_3 = 1000$ kPa find; calculate the efficiency of the engine based on this cycle.



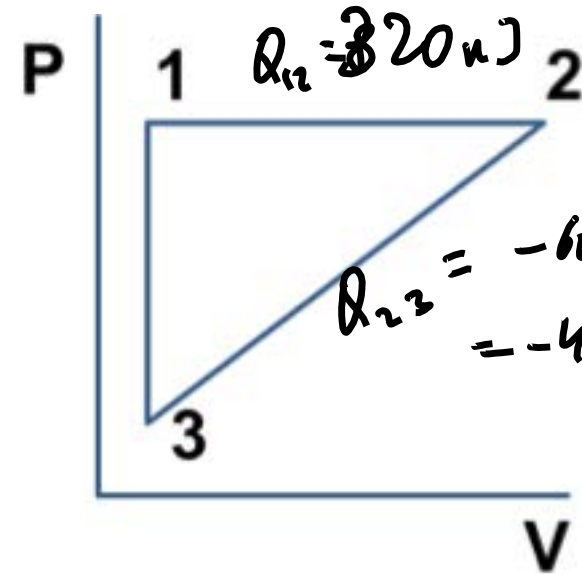
$Q_{1-2} = 320 \text{ kJ}$; $n = 30 \text{ mol}$; $P_1 = 2000 \text{ kPa}$, $V_1 = 40 \text{ L}$; $V_2 = 80 \text{ L}$
 $P_3 = 1000 \text{ kPa}$; find; calculate the efficiency of the engine based on this cycle.

$$Q_h - 420000 = 20000$$

$$Q_h = 420000 + 20000 = 440000 \text{ J}$$

$$e = \frac{20000}{Q_h} ;$$

$$e = \frac{20000}{440000} \cdot 100\% = \frac{200}{44} \% = 4.5\%$$

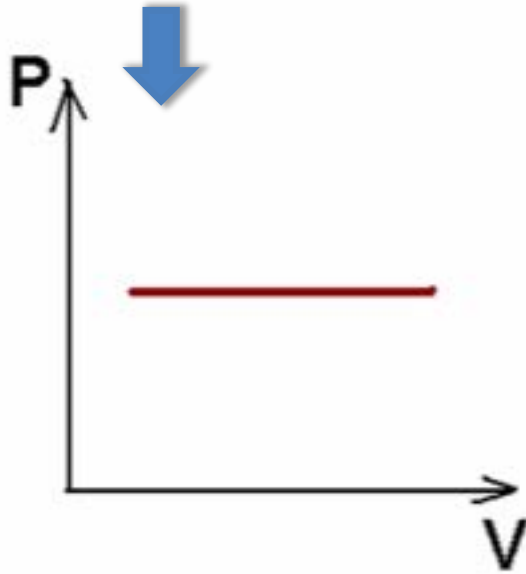


Three standard processes ($n = \text{const}$):

Isobaric

$$P = \text{const}$$

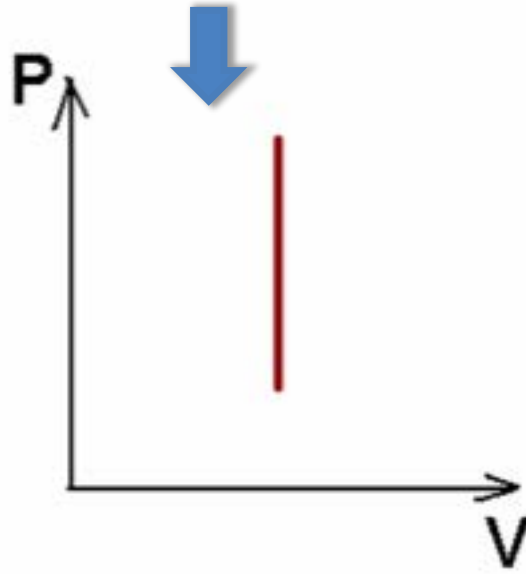
$$V/T = \text{const}$$



Isochoric

$$V = \text{const}$$

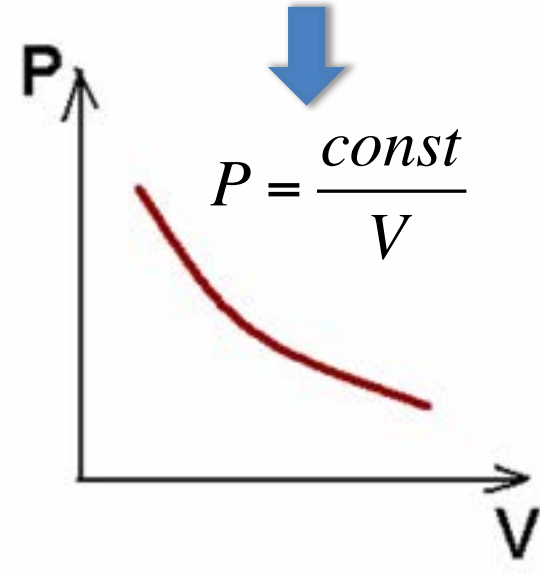
$$P/T = \text{const}$$



Isothermal

$$T = \text{const}$$

$$PV = \text{const}$$



$$n = m/M$$

$$n = \text{const}$$



$$\frac{PV}{Tn} = R = 8.31 \text{ J/(K mole)}$$

(Try to plot graphs for the same processes using PT and VT axes)



Adiabatic process.

Happens without heat exchange with the surrounding

$$Q = 0 \Rightarrow 0 = \Delta U + W_{byS}$$



**(1) An Insulated System
and if $W = 0$**

$$\Rightarrow U_{\text{system}} = \text{const}$$

$$\Rightarrow Q_1 + Q_2 + \dots = 0 \text{ (HBE)}$$

$$\Rightarrow \Delta U = -W_{byS}$$

$$\Rightarrow \Delta U = W_{onS}$$



(2) A very fast process

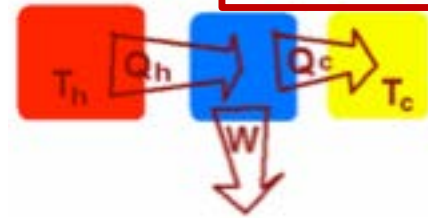
An Ideal (Carnot) Engine

Carnot showed that for an *ideal* (or Carnot) engine, operating between temperatures T_h and T_c , the **efficiency** is:

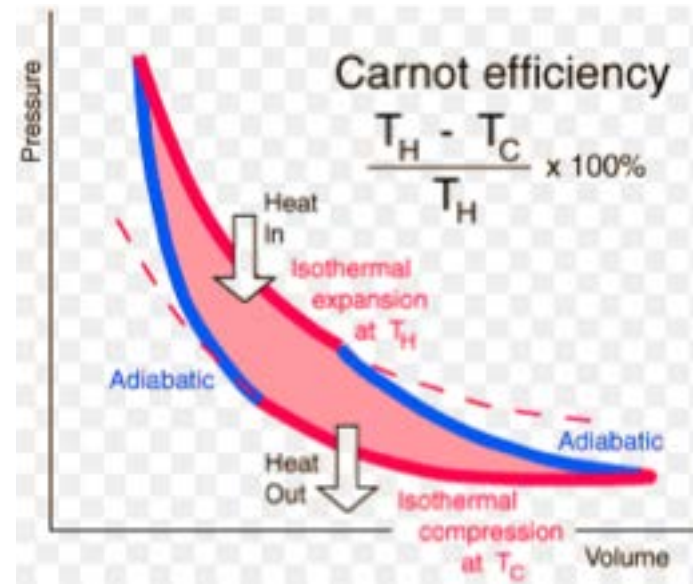
For an ideal (a.k.a. Carnot) engine

$$e_c = 1 - \frac{T_c}{T_h}$$

For ANY engine



$$e = 1 - \frac{|Q_c|}{|Q_h|}$$



Every cycle an ideal engine does 420 kJ of work while releasing 600kJ of thermal energy. If the lowest operating temperature is 27°C , what is the highest temperature?



Every cycle an ideal engine does 420 kJ of work while releasing 600 kJ of thermal energy. If the lowest operating temperature is 27°C, what is the highest temperature?

$$e = \frac{T_h - T_c}{T_h} = \frac{W}{Q_h} \Rightarrow \frac{T_h - 300}{T_h} = \frac{420000}{1020000}$$

Physics is done!

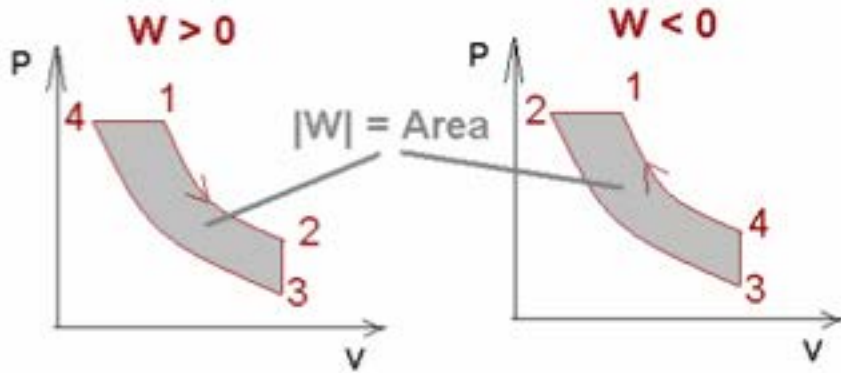
↓

$$T_c = 27 + 273 = 300 \text{ K}$$

$$\begin{aligned} W &= 420000 \text{ J} \\ + Q_c &= 600000 \text{ J} \\ Q_h &= 1020000 \text{ J} \end{aligned}$$

In a cyclic process, the system starts in a particular state and returns to that state after undergoing a few different processes.

The net work involved is the enclosed area on the P-V diagram.



If the cycle goes clockwise, the system does work. This is the case for an engine.

If the cycle goes counter-clockwise, work is done on the

system. An example of such a system is a refrigerator or air conditioner.

When the system returns to its initial state ($T_i = T_f$) there is no change in internal energy after going around the cycle $\Delta U = 0$,

Hence: $Q_{\text{cycle}} = W_{\text{cycle}} = Q_h + Q_c = Q_h - |Q_c| \Rightarrow Q_h = W + |Q_c|$

The summary:

$$e = \frac{W}{|Q_h|}$$

$$e_c = 1 - \frac{T_c}{T_h}$$

Reversible and Irreversible Processes

Let's say you rotate the “entropy jar” 10 times CCW. If you videotaped this and ran the film backwards it would be obvious to you that the film was running backwards. Why?

The process in the backward film violates:

- 1) The second Newton's Law
- 2) The Law of Conservation of Energy
- 3) The Law of Conservation of Momentum
- 4) The First Law of thermodynamics
- 5) None of the above
- 6) All of the above

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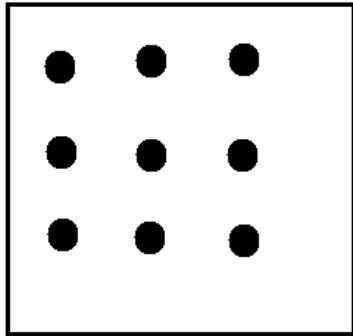
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Entropy

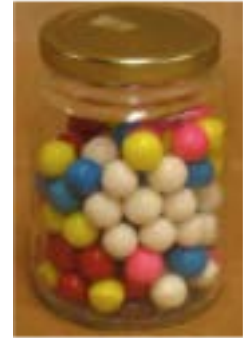
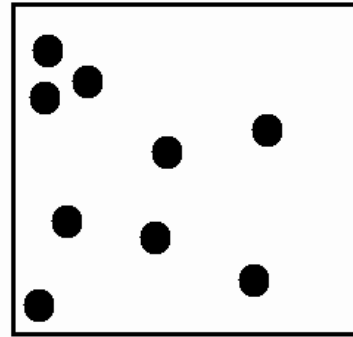
Entropy is a measure of *disorder* in a system.

Entropy is “proportional” to a chaos in the system: the more chaos => the more entropy

Order => low entropy



Chaos => high entropy

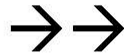


The symbol for entropy is S , and the units are J/K.

Reversible process vs. irreversible process

A *reversible* process is one in which there is *no* change in entropy, and the system *and the surroundings* can be returned to the initial state.

Irreversible process



Chaotic state

Ordered state

or
(slide it carefully!)

Reversible process



A transition from an ordered state to a chaotic state is irreversible!

The entropy of an isolated system NEVER decreases!

The Second Law of Thermodynamics (2LT)

$$\Delta S = \frac{Q}{T_{const}}$$

In *any* process the entropy of a closed system either increases or stays the same, *it never decreases*. Hence, the change in entropy of a closed system is *never* negative!

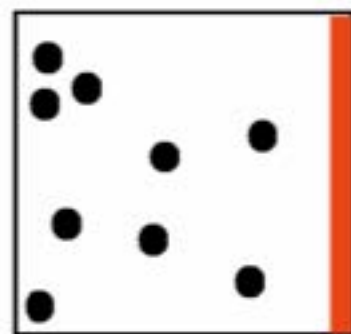
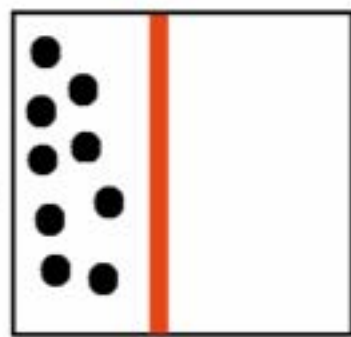
$$\Delta S \geq 0$$

When a closed system is in equilibrium, it is in the *most* chaotic (*least* ordered) state, and the entropy of the system cannot be any higher, hence stays the same: change in entropy is zero:

$$\Delta S = 0$$

For example, a gas in equilibrium has randomly and uniformly distributed particles.

When a closed system is *not* in equilibrium, it is *not* in the *most* chaotic (*least* order) state, and the system tries to reach the most chaotic state, and the entropy of the system is increasing; $S_f > S_i$; $\Delta S > 0$



For example: if we collect all the particles in one half of a container and then release them, the particles eventually fill up the whole

container, and the system will reach the least ordered state.

The opposite process requires *an external force* acting on the system, in that case the system is *not* close.

The entropy of an isolated system NEVER decreases!

The Second Law of Thermodynamics (2LT)

In any *isolated* (closed) system the order never increases; hence either the order remains the same or it decreases, meaning the disorder, or *chaos* increases.

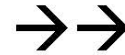
5) Only the Second Law of Thermodynamics would be violated - this is why entropy is sometimes called time's arrow.

Time moves in the direction of increasing entropy (in a physical world).

These are examples of an irreversible process.

In all the examples the transition from an order to a chaos is happening.

A).



B). A process is irreversible if *energy is lost to friction*, or

C). if energy is lost as *heat flows from a hot region to a cooler region*.

Reversible and Irreversible Processes

Let's say you rotate the entropy jar 10 times CCW. If you videotaped this and ran the film backwards it would be obvious to you that the film was running backwards. Why?

The process in the backward film violates:

- 1) The second Newton's Law
- 2) The Law of Conservation of Energy
- 3) The Law of Conservation of Momentum
- 4) The first law of thermodynamics
- 5) **The second law of thermodynamics**

Learning

is

irreversible!

Temperature, heat, gas: $T_K = T_C + 273$



$$Q = cm\Delta T \quad Q = \pm mL \quad \Sigma Q = 0$$

$$\frac{N}{N_A} = \frac{m}{\mu} = n \quad PV = NkT = nRT \quad E_{kav} = \frac{i}{2}kT$$

$$R = kN_A \quad U = \frac{i}{2}kNT = \frac{i}{2}nRT \quad i = 3, 5, 6.$$

$$W = \text{Area}(P_{\text{vs.}}V) \quad V \uparrow \Rightarrow W > 0 \quad V \downarrow \Rightarrow W < 0$$

$$\frac{PV}{nT} = R = \text{const} \Rightarrow n = \text{const} \Rightarrow \frac{PV}{T} = nR = \text{const} \Rightarrow \frac{P_1V_1}{T_1} = \frac{P_2V_2}{T_2}$$

$$Q = W + \Delta U \quad \Delta U_{\text{cycle}} = 0 \quad Q_{\text{cycle}} = W_{\text{cycle}}$$

$$P = \text{const}: \frac{V_1}{T_1} = \frac{V_2}{T_2} \quad W = P\Delta V = nR\Delta T \quad \Delta U = \frac{i}{2}nR\Delta T \quad Q = \frac{i+2}{2}nR\Delta T$$

$$V = \text{const} \Rightarrow \frac{P_1}{T_1} = \frac{P_2}{T_2} \quad W = 0 \quad \Delta U = \frac{i}{2}nR\Delta T \quad Q = \Delta U = \frac{i}{2}nR\Delta T$$

$$T = \text{const} \Rightarrow P_1V_1 = P_2V_2 \quad Q = W \quad \Delta U = 0$$

LectureMCQ_L25 Question_5

On a scale from **1**
(strongly disagree) to **9**
(strongly agree) how
would you assess the
following statement?

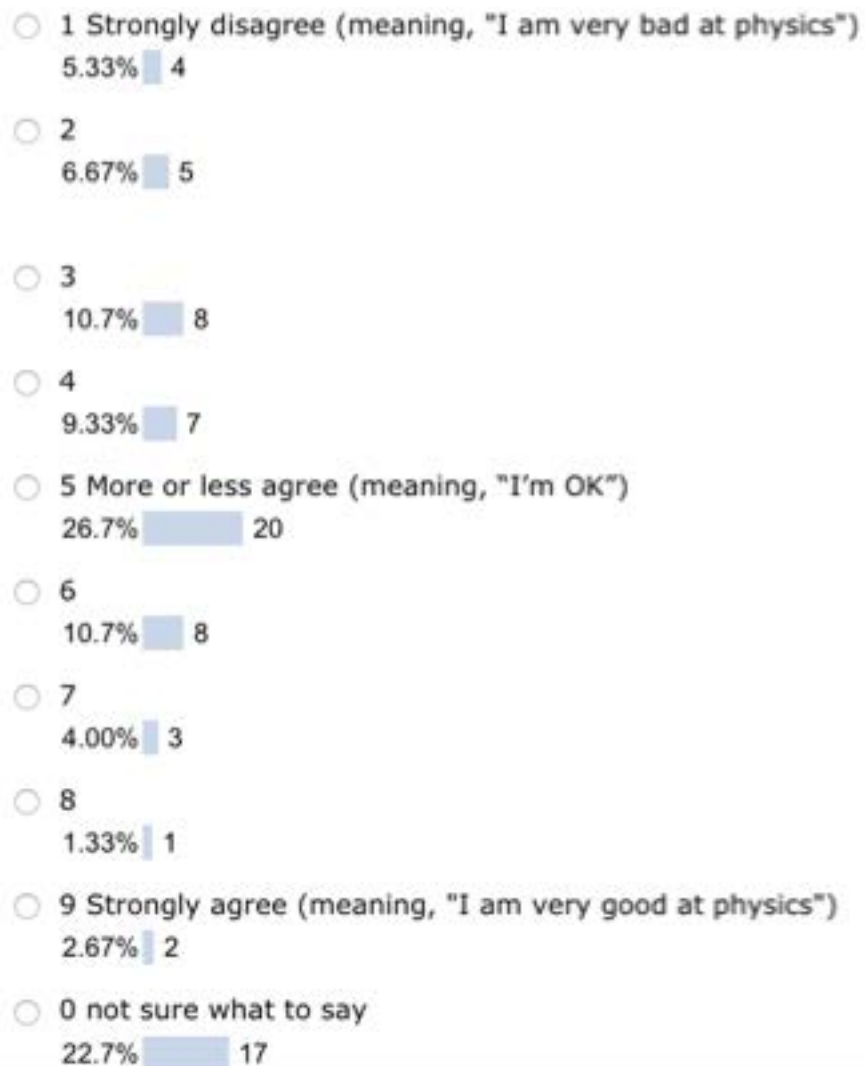
**“I am very good
at physics!”**

or select **0** if you are
not sure.

“I am very good at physics”

1. Strongly disagree
(meaning, “I am very bad
at physics”)
- 2.
- 3.
- 4.
5. More or less agree
(meaning, “I’m OK”)
- 6.
- 7.
- 8.
9. Strongly agree (meaning,
“I am very good at physics”)

The first lecture



The last lecture





Course Evaluations

Session: Boston University Summer Term

Instructor: Valentin Voroshilov

Course: CAS PY105-A1 Elementary Physics 1



1. For only 2 people!
2. Does not provide any information to potential students.

V.

Rate this Professor Show Show Show 1

User Comments and Ratings Professor Rebuttals

DATE	CLASS	RATING	COMMENT
8/20/12	PY106	Good Quality Ease: Helpfulness: Clarity: Rate Interest:	I HATED physics before I took this guy. He made it so interesting, and he had so many good examples and demonstrations that to my disbelief, I actually started liking physics (and I suck at all math). He's awesome, don't let the previous reviews scare you away. Go to office hours, do the hw, and show up to class; you might even learn something! Report this rating
8/19/12	PY106	Good Quality Ease: Helpfulness: Clarity: Rate Interest:	Val made physics easy, relateable and extremely worthwhile. Funny dry humor and great demonstrations. Maybe it was the fact that I took this course over the summer that made it easier then the previous posters portray. Literally just do the weassign problems and the ones on the slide, know them well, and you will do great. Highly recommend. Report this rating



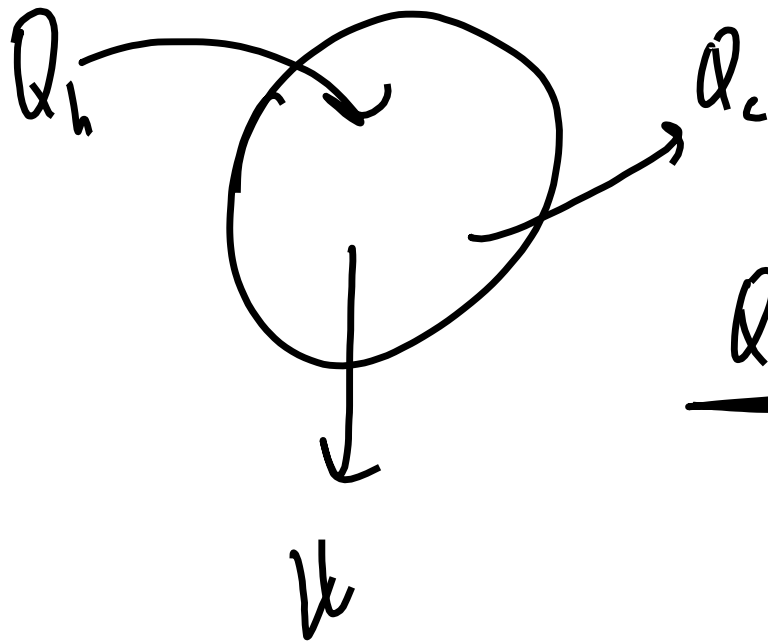
1. For everyone!
2. Give potential students **specific** advices.

The END! ☹️



B50

Q & A



$$\underline{Q_h - |Q_c| = k}$$

HW3 PG #3:

$$T_1 = t_1 + 273.15$$

$$T_2 = t_2 + 273.15$$

$$\Delta T = T_2 - T_1 =$$

$$= (t_2 + 273.15) - (t_1 + 273.15)$$

$$W_{oh} = 303J \rightarrow W_{by} = -303J = \underline{\underline{\Delta J}}$$

$$Q = \Delta U + W_{by}$$

$$\Delta U = \frac{i}{2} n R \Delta T = \frac{i}{2} \Delta(PV)$$

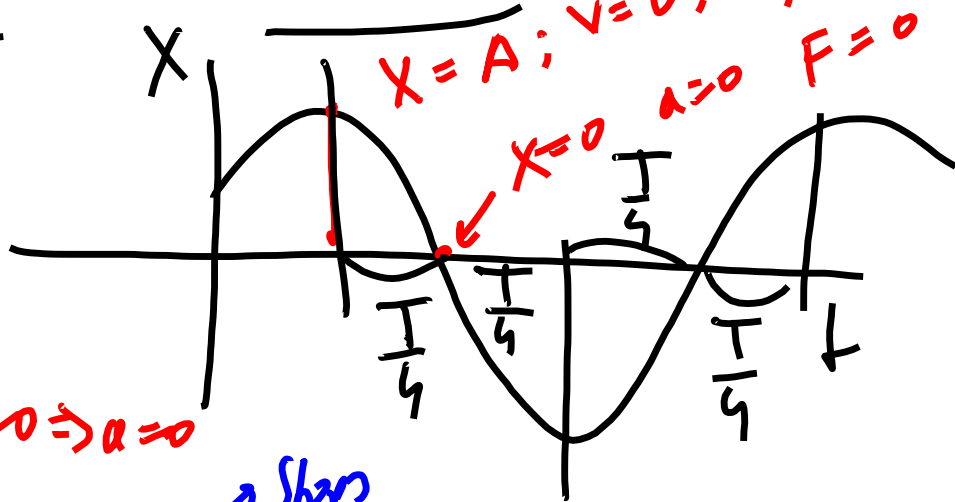
$$n = 8.8$$

$$\Delta P = 145 - 22$$

$$i = 3$$

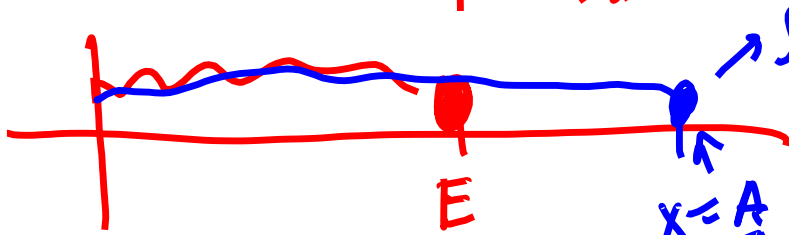
MW3 P1: #7

\int HM:

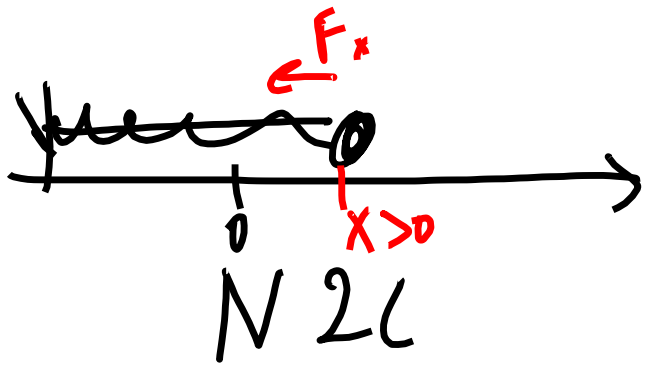


$x=A; v=0; F, a \rightarrow \text{max}$
 $x=0; a=0; F=0; \underline{\underline{v \text{ max}}}$

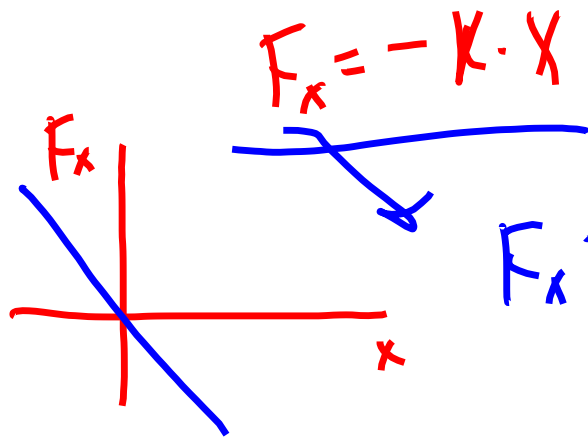
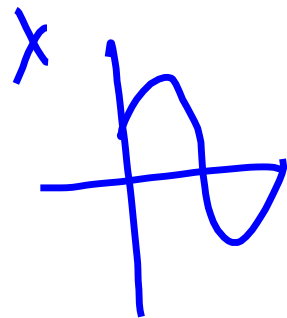
$F=0 \Rightarrow a=0$



Stops
 $v=0$
 $\underline{\underline{x=A}}$
 $|F| = k|x| = \underline{\underline{k \cdot A}}$
 $|a| = \underline{\underline{\omega^2 \cdot A}}$



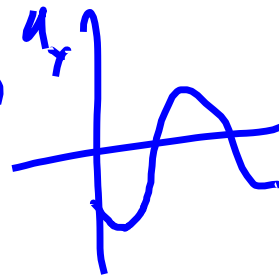
$$|F_x| = k \cdot |x|$$



$$F_x = m a_x$$

$$m a_x = -k x$$

$$a_x = -\frac{k}{m} \cdot x$$



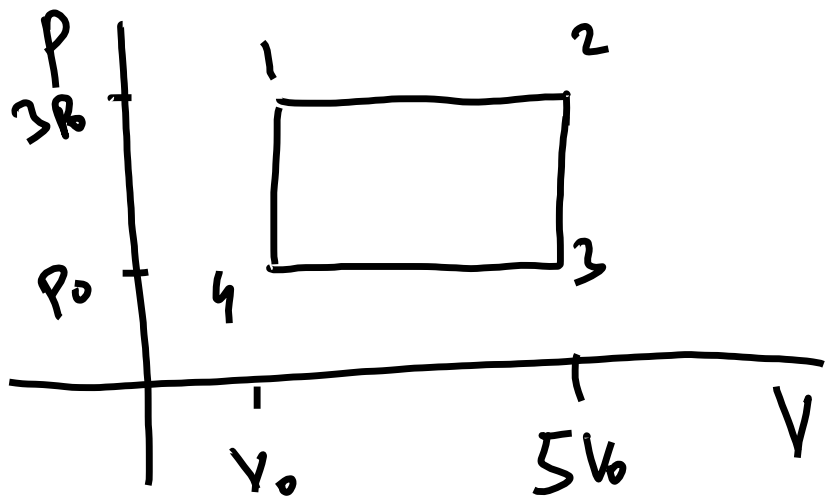
$$X = A \cdot \cos(\omega \cdot t)$$

$[\omega] = \frac{\text{rad}}{\text{s}}$

$$V_m = A \cdot \omega$$

$$a_m = A \cdot \omega^2 = V_m \cdot \omega$$

rad per sec \rightarrow rad



$$P_0 V_0 = \underline{10000 \text{ J}}$$

$$C_V = \frac{3}{2} R \Rightarrow \underline{\underline{i=3}}$$

$$1 \rightarrow 2: \Delta U = \frac{i}{2} n R \Delta T = \frac{i}{2} P_0 \Delta V =$$

$$= \frac{3}{2} 3 P_0 \cdot (5V_0 - V_0) = \frac{9}{2} \cdot 4 \cdot \textcircled{P_0 V_0} =$$

$$= 18000 \text{ J}$$

$$\Delta U_{23} = \frac{i}{2} \Delta (P \cdot V) =$$

$$= \frac{3}{2} 5V_0 \cdot (P_0 - 3P_0) = \frac{3}{2} 5 \cdot (-2) \cdot \textcircled{V_0 P_0}$$